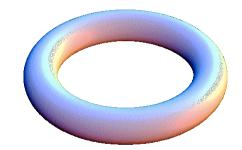


# The Modeling and the Simulation of the Fluid Machines of Systems/Synthetic Biology

Jean-Louis Giavitto
Olivier Michel
Antoine Spicher



http://mgs.spatial-computing.org















#### 1. Introduction

from silicon based information processing to fluid (biological) machines

- 2. What are the good abstractions for fluide machinery? towards the engineering of biological systems
- 3. The MGS project declarative spatial computing
- **4. Modeling morphogenesis** the growth of the meristem
- 5. The iGEM-Paris 2008 device a synthetic « multicellular bacterium »

#### Home message



New kind of computational machines with "dynamic structure" strange loop between structure and processes not new (program = data) but not understood (e.g., type discipline to avoid that)

2. Space matters compartmentalization and beyond

3. Killer app. systems & synthetic biology the nano-world: form=function

4. Usual tools of computer science are relevant but the focus, the questions and the answers are new e.g., termination in rewriting

Versatility of the MGS approachtime evolution = rewriting strategykind of space = kind of objects to be rewritten

# from silicon based information processing to fluid (biological) machines

#### A story that could have been parallel...



1936: the Turing machine

1944 E. Schrödinger: « program » and genetic « code »

• 1947 : the first transistor

• 1958 : first integrated circuit

• 1962 : idea of computer network

1967 ARPANET

1971 : first microprocessor

1972 : electronic mail

89~90 : WWW

• 90 : start of the commercial internet

November 2009 : Cray Jaguar
 1.75 petaflops (10<sup>15</sup> flop/s)

1928 : DNA as the support of the genetic information

• 1953 : DNA structure

72~73: RNA sequencing

75 : DNA sequencing

• 83 : PCR

• 1989 →2001 then 2003 : the human genome project

#### ... but whose initial motivations are greatly different



Some common concerns: concepts of

- storing
- replicating
- communicating
- modifying

(genetic) informations are studied in computer science (biology).

But there is a great difference between computer science and bio:

- Computer science leads to the engineering of artefactual devices everything is developed from scratch, from hardware to software
- Biology is a natural science studying preexisting systems shaped by evolution

However, the *technology* making possible the design and the building or the synthesis of biological machines *now* exists

#### Computing, yes but why?



- Linear algebra with wetware?
   parallelism? Cf. the moral of the DNA computing story!
- Cyberphysical systems
   tight coupling between computational processing
   and physical behavior (i/o)
  - 1<sup>st</sup> generation: embedded systems
     aerospace, automotive, chemical processes, civil
     infrastructure, energy, healthcare, manufacturing,
     transportation, entertainment, consumer appliances, etc.
  - 2<sup>nd</sup> generation: *nanomachines* cells as programmable and replicable chemical plants

### **Technological developments**



1906	Triode (L.D. Forest)
1925	FET transistor (Julius Edgar Lilienfeld)
1947	Bell Labs, John Bardeen, Walter Houser Brattain & William Bradford Shockley: the first contact transistor
1958	First integrated circuit (TI)
1973	PDP8 (DEC)
1971	1 <sup>st</sup> microprocessor (Intel 4004 – 2250 transistors)
1972	Intel 8008 (8 bits)
1978	Intel 8086 (16 bits)





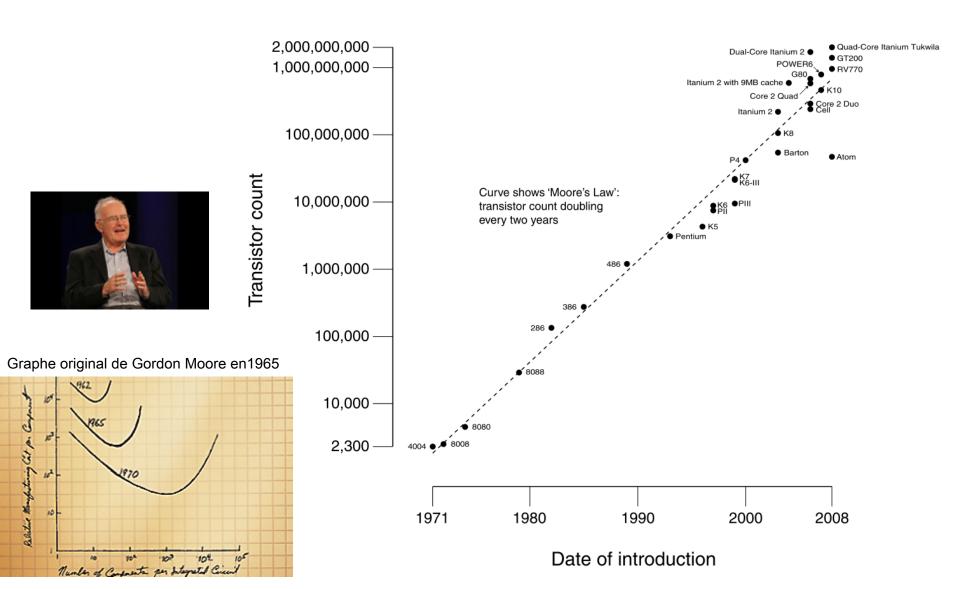
Simulation on Blue Gene (4096 pe, 256Mo RAM - 360 T-flops) of 1 second of half mouse brain functioning



#### The law of Mr. Moore



#### CPU Transistor Counts 1971-2008 & Moore's Law



#### An extraordinary decrease





On the road to a billion transistors per chip, transistors are so small that about 200 million of them could fit on the head of each of these pins.

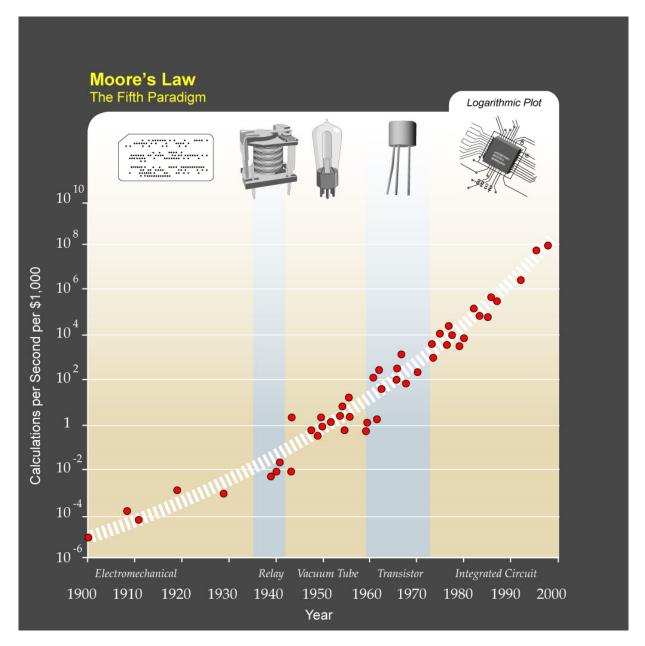
The price per transistor on a chip has dropped dramatically. Some people estimate that the price of a transistor is now about the same as that of one printed newspaper character.

Il lead to such wonders as ninals connected to a central for automobiles, and perequipment. The electronic to be feasible today.

Copyright © 2005 Intel Corporation

# That goes back before the transistor...





# If we compare to molecular biology...

From a computer scientist perspective!

#### The three periods of molecular bio (1)



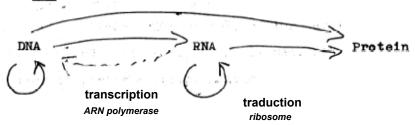
Francis Crick – 1956/58 – The central dogma of mol bio

Ideas on Protein Synthesis (Oct. 1956)

The Doctrine of the Triad.

The Central Dogma: "Once information has got into a protein it can't get out again". Information here means the sequence of the amino acid residues, or other sequences related to it.

That is, we may be able to have



Restated in 1970

NATURE VOL. 227 AUGUST 8 1970

#### 561

#### Central Dogma of Molecular Biology

by FRANCIS CRICK MRC Laboratory of Molecular Biology, Hills Road, Cambridge CB2 2QH

The central dogma of molecular biology deals with the detailed residue-by-residue transfer of sequential information. It states that such information cannot be transferred from protein to either protein or nucleic acid.

### The three periods of molecular bio (2)



- Analysis
  - of the fine structure of DNA
    - topology
    - irregularity of the double Helix
    - ...
  - instability, dynamics
    - Gene transfer

# II: from the DNA structure length genome sequencing & synthesis

- sequence identification
  - qualitative and quantitative analysis of proteines at various phases of the cell
  - genome wide sequencing (yeast(1997), C-elegans (98), humain (2001), ...)

#### Synthesis

- genetic engineering (e.g., yeast producing human proteins)
- Copy and synthesis of DNA
  - Restriction enzymes
  - recombinant DNA (insertion d'un brin d'ADN dans un ADN existant)
  - PCR ([Mullis 86], ...)
  - Gene synthesis: phosphoramidite chemistry [Beaucage & Caruthers 1981] (de 1.25\$/bp, jusqu'à 45 kbp, 2 semaines [2006])

# The three periods of molecular bio (3)



What is missing for bio-engineering?

### The three periods of molecular bio (3)



# The conceptual revolution of « engineerization »

#### Application to biology of engineering principles:

- standardisation (function specification, standardization, libraries, ...)
- abstraction (functionnal levels, organization)
- decoupling (conception / implementation)

"The work on restriction nucleases not only permits us easily to construct recombinant DNA molecules and to analyse individual genes, but also has led us into the new era of 'synthetic biology' where not only existing genes are described and analyzed but also new gene arrangements can be constructed and evaluated."

[Szybalski, W. & Skalka, A. Nobel prizes and restriction enzymes. Gene 4, 181—182 (1978)]



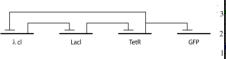
**Synthetic biology** 

#### A realistic vision?



# Proof of concept

- repressilator [Elowitz & Leibler (2000) Nature 403, 335-338]



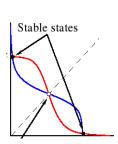
REPRESSOR 1 REPORTER

INDUCER (IPTG)

PROMOTER 1

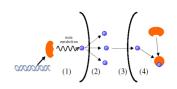
- Flashing E. Coli [Ferber (2004) Science 303, 158-161]
- toggle switch [Gardner & al (2000) Nature 403, 339-342]





#### Sensors

- Sensing chemicals [TNT (Gibbs (2004) Scientific American 75-81], caffeine [iGEM]
- Sensing radiation
   (biofilms [Kobayashi et al. (2004) PNAS 10:8414-841], [iGEM'04])
- cell-cell communications [Weiss & al (2003) Natural Computing 2, 47-84]





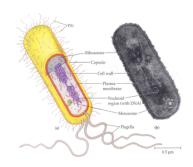


#### A realistic vision?



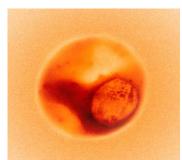
# Bio-medical/Bio-production

- Drugs (Keasling's artemisinin [Martin & al (2003) Nature Biotech 21, 796-802])
- Targeted delivery [Anderson & al (2005) J. Mol Biol 335, 619-627]
- Nanobot [Weiss, Knight DNA06 LNCS 2054, 1-16]
- timed-drug delivery [F. Molina et al.— 2007]



# Bio-computing

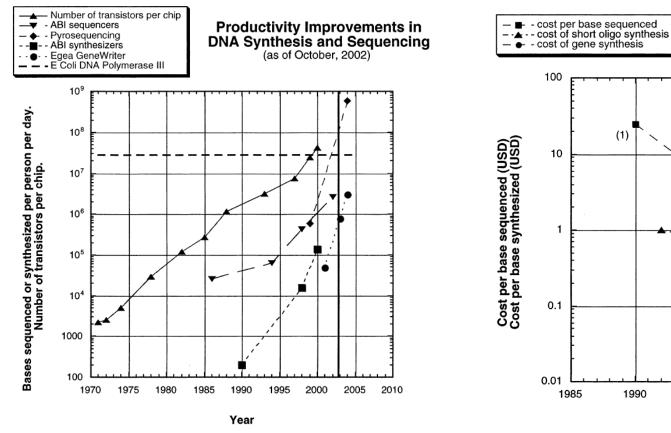
- inverter, nand gate, self-repressor,
   bi-stable switch, oscillators... [R. Weiss]
- cell-cell communication, signal processing [R. Weiss]

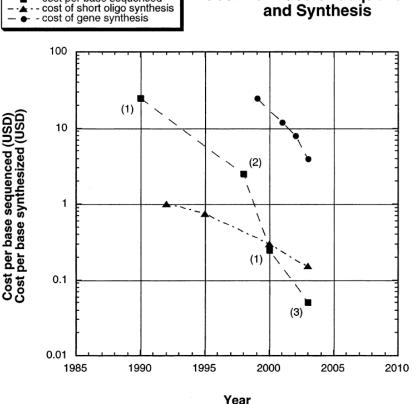


#### From the Moore law to the Carlson law



**Cost Per Base of Sequencing** 





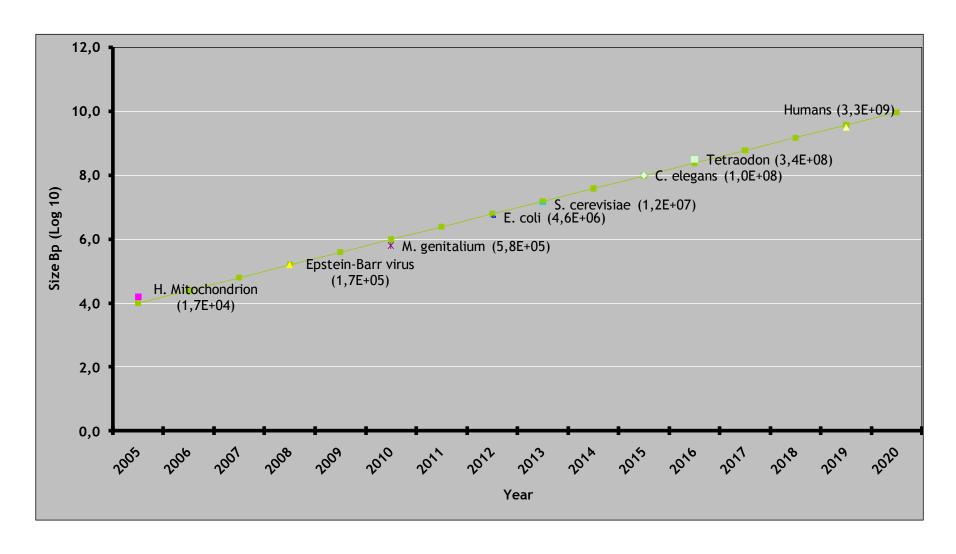
[Carlson, R. (2003).

The pace and proliferation of biological technologies.

Biosecurity and Bioterrorism: Biodefense Strategy, Practice and Science, 1(3), 203-214.]

#### The projections are verified

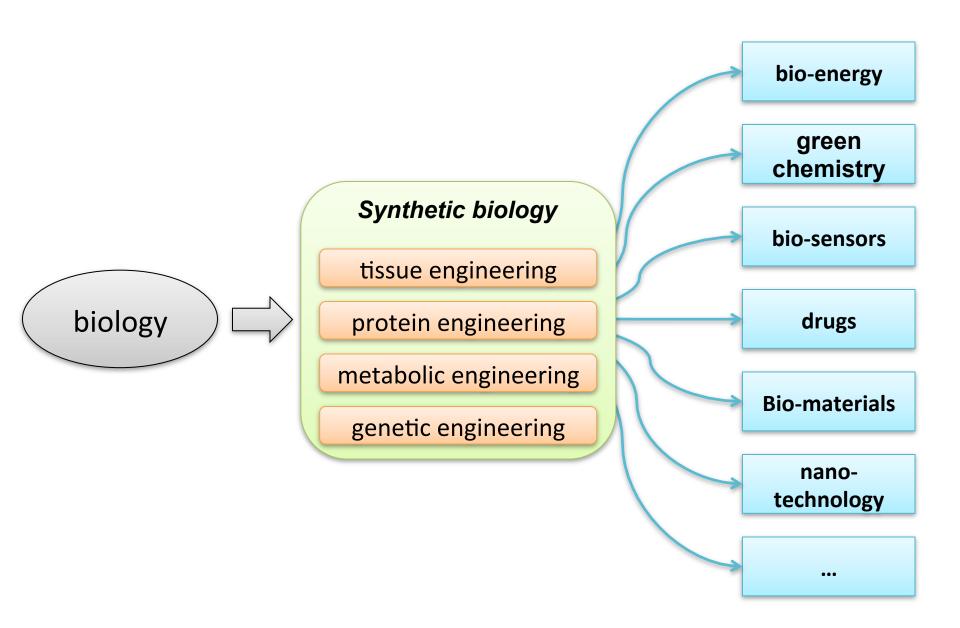




2010 – 2015 : projections for the synthesis of a genome

#### **Applications**





# What are the good abstractions to program a cell?

#### A low level code

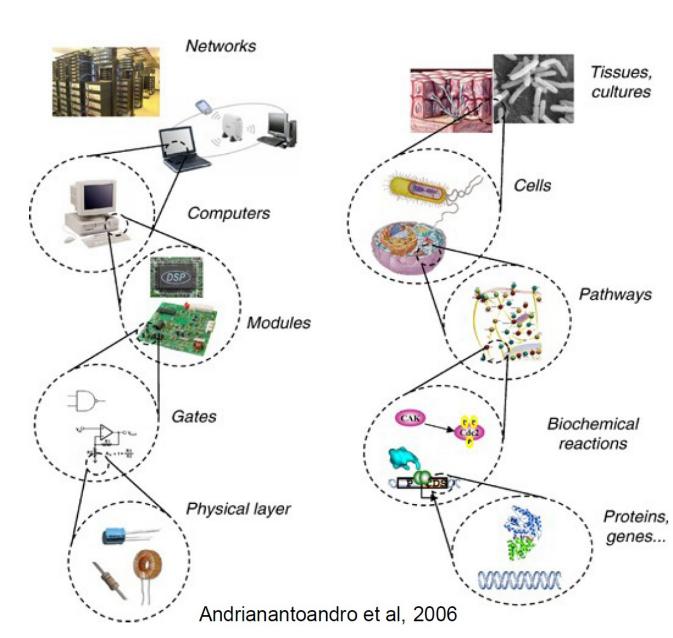


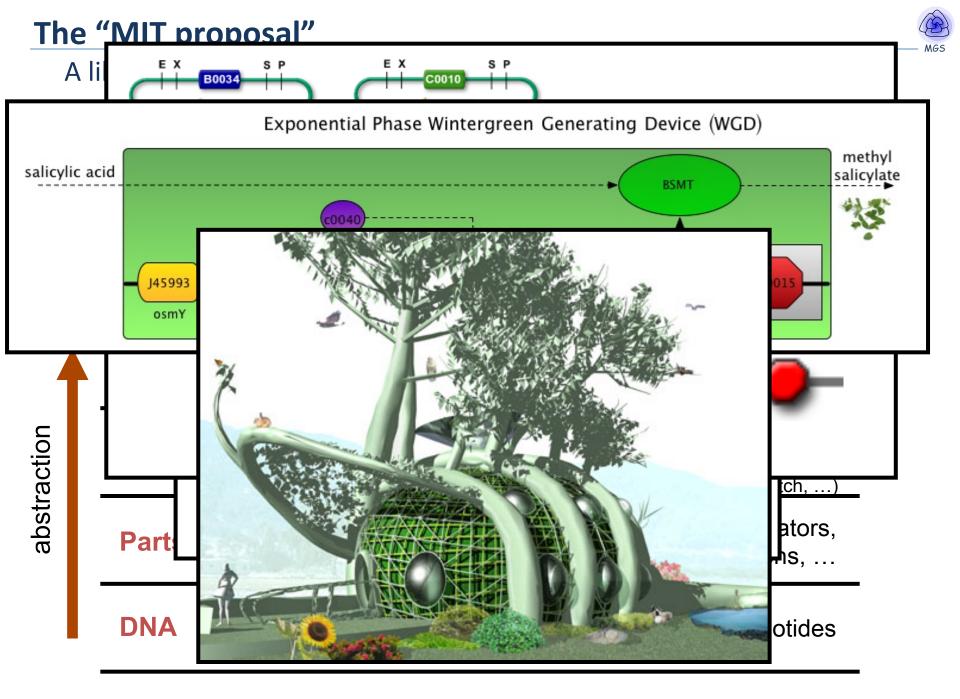
ACAGGGTGACCTAAGACCTTATTGTCTAATTGAGAAGGCTTCGGAATTTGACCTAAG ACCTTATTGTCTAATTGAGAAGGGCCGGTTGAACAGGGCTTCGGAATTTGACCTAAG ACCTTATTGTCTAATTGAGATGACCTAAGACCTTATTGTCTAATTGAGAAGGAGGGCC GGTTGAACAGGTGACCTAAGACCTTATTGTCTAATTGAGAAGGGCTTCGGAATTTGAC CTAAGACCTTATTGTCTAATTGAGAAGGGCCGGTTGAACAGGGCTTCGGAATTTGACC TAAGACCTTATTGTCTTGACCTAAGACCTTATTGTCTAATTGAGAAGGAATTGAGAAGG GCCGGTTGAACAGGTGACCTAAGACCTTATTGTCTAATTGAGAAGGGCTTCGGAATTT GACCTAAGACCTTATTGTCTAATTGAGAAGGGCCGGTTGAACAGGGCTTCGGAATTTG ACTGACCTAAGACCTTATTGTCTAATTGAGAAGGCTAAGACCTTATTGTCTAATTGAGA AGGGCCGGTTGAACAGGGCTTCGGAATTTGACCTAAGACCTTATTGTCTAATTGAGAAG GGCCGGTTGAACAGGTGACCTAAGACCTTATTGTCTAATTGAGAAGGGCTTCGGAATTT GACCTAAGACCTTATTGTCTAATTGAGAAGGGCCGGTTGAACAGGGTGACCTAAGAC ACCTTATTGTCTAATTGAGAAGGGCCGGTTGAACAGGGCTTCGGAATTTGACCTAAG ACCTTATTGTCTAATTGAGATGACCTAAGACCTTATTGTCTAATTGAGAAGGAGGGCC GGTTGAACAGGTGACCTAAGACCTTATTGTCTAATTGAGAAGGGCTTCGGAATTTGAC CTAAGACCTTATTGTCTAATTGAGAAGGGCCGGTTGAACAGGGCTTCGGAATTTGACC TAAGACCTTATTGTCTTGACCTAAGACCTTATTGTCTAATTGAGAAGGAATTGAGAAGG GCCGGTTGAACAGGTGACCTAAGACCTTATTGTCTAATTGAGAAGGGCTTCGGAATTT GACCTAAGACCTTATTGTCTAATTGAGAAGGGCCGGTTG

# **Breaking the complexity barrier**



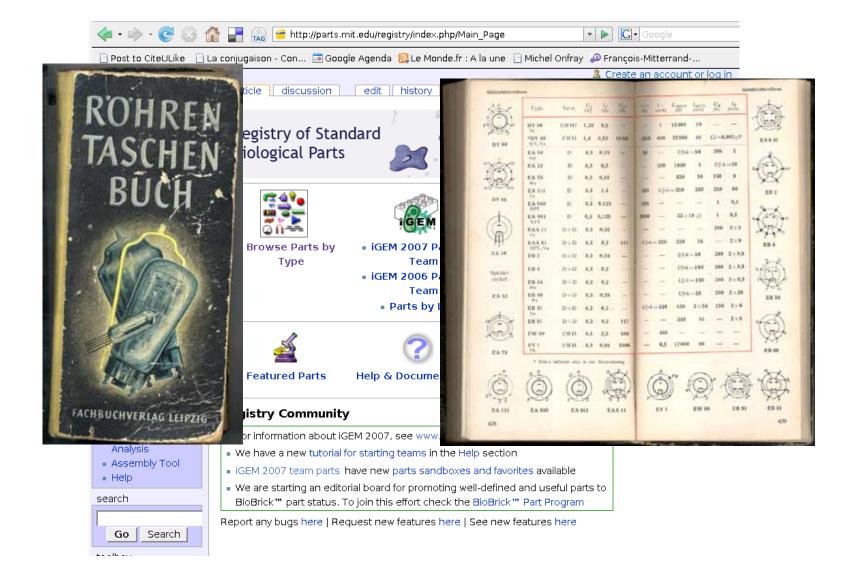
- Levels of abstraction
- Hierarchy
- Decoupling
- Modularity
- I/O





#### A library of standardized componants





#### **Several kind of componants**



#### **Systems**

Project Projects

**-**-**∑-** Measurement 🔹

——— Measurement (Under Development) 2

#### Devices

🤷 Reporters 🛭

Inverters 2

→ Fignalling 2

🗽 Protein Generator 🛭

🎹 - Composite Devices 🛭

🗝 Measurement 🛚

#### **Parts**

Ribosome Binding

Sites ?

Regulatory 2

RNA ?

DNA ?

- Protein Coding 2

Protein Coding (Under

Development) 2

— Terminators 🛽

🦴 Conjugation 🛭

#### Chassis

瓣 E.coli Strains 🔞

Mammalian

#### Vectors

% Plasmids ?

#### Other

Yeast Parts ?

A.B Construction
Intermediate ?

📤 PCR Primer 🔞

🕮 Tags 🛭

Bacteriophage T7





#### Reporters

For information on reporter coding regions, click here.

#### Available constitutive reporters

Edit

-?-	Name	Description	Tag -?-	Excitation	Output	Length
ΑW	BBa_I13521	Ptet mRFP, switch off by tetracycline	None		RFP	923
ΑW	BBa_I13522	pTet GFP	None		GFP	937
ΑW	BBa_I13600	Tet with CFP reporter (without LVA tag)	None		CFP	940
ΑW	BBa_I13602	Tet operator with CFP reporter (with LVA tag) [R/Tc+]	LVA		cyan	979
ΑW	BBa_I13604	Reporter construct for constitutive YFP and inducible CFP	None		YFP, CFP	1888
	BBa_I13 <b>6</b> 05	Reporter Construct (Ly-Tc-) for constitutive CFP and inducible YFP	None		CFP, YFP	1888
AW	BBa_J04430	GFP coding device switched on by IPTG	None		GFP	1083
ΑW	BBa_J04450	RFP Coding Device switched on by IPTG	None		RFP	1069

#### Other constitutive reporters

Edit

-?-	Name	Description	Tag -?-	Excitation	Output	Length

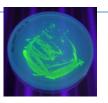
#### Available other reporters

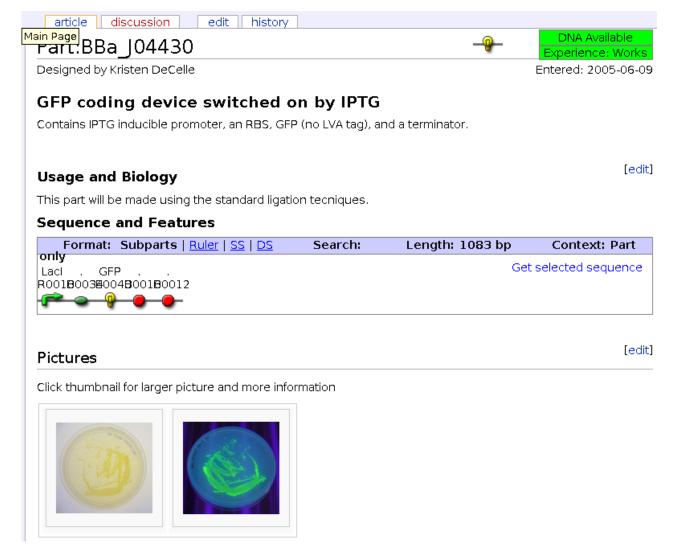
Edit

-	?-	Name	Name Description		Excitation	Output	Length
Α	W	BBa_E0241	PoPS to GFP converter	None		Green	7 <b>9</b> 5
Α	W	BBa_E0430	EYFP (RBS+ LVA- TERM) (B0034.E0030.B0015)	None		Yellow	878
Α	W	BBa_E0840	B0030.E0040.B0015	None		Green	878
Α	W	BBa_E7104	GFP Reporter Device for Dedicated Transcription Systems	None		Green	826
Α	W	BBa_I13601	Lac operator with CFP reporter (without LVA tag) [R/Lc-]	None		cyan	940
A	W	BBa_I13607	Reporter Construct (Ly+Tc+)	LVA		cyan, yellow	1966
Δ	W	RRa USOLA	ROOSS ECEP	Mone		cvan	742













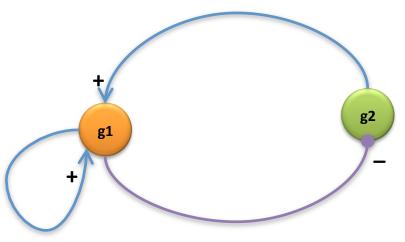
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C		1	1	1	21	31	41	51	61	71	81	Set selected sequence 91
Sequen	,  1	caatacg	caa a	ccgcctctc	cccgcgcgtt	ggccgattca		tggcacgaca	ggtttcccga	ctggaaagcg	ggcagtgagc	gcaacgcaat
Form							R0010			~~	CAP	:
1 1	101	taatgtg	agt t	agctcactc	attaggcacc	ccaggcttta	cactttatgc	ttccggctcg	tatgttgtgt	ggaattgtga	gcggataaca	atttcacaca
		+~~~		CAP	<b>~~~</b>	-35	R0010	-10	•	Lacl	~~~~~	
	201	tactaga	gaa a	gaggagaaa	tactagatgc	gtaaaggaga	agaacttttc	actggagttg	tcccaattct	tgttgaatta	gatggtgatg	ttaatgggca
			E	300 <mark>34</mark>				E0040				
	301	caaattt	tct g	tcagtggag	agggtgaagg	tgatgcaaca	tacggaaaac	ttacccttaa	atttatttgc	actactggaa	aactacctgt	tccatggcca
							E0040					
	401	<b>→</b> acacttg	tca c	tactttcgg	ttatggtgtt	caatgctttg		agatcatatg	aaacagcatg	actttttcaa	gagtgccatg	cccgaaggtt
	E01	.+=+			++++	.+====	E0040		+++		.++=+++.	
	501	→ atytaca	yya a	ayaactata	ttttttaaay	atyacyyyaa	E0040	cgtgctgaag	tcaaytttya	ayytyatacc	ttigitaata	yaatcyaytt
	601	aaaaggt	att g	attttaaag	aagatggaaa	cattcttgga	cacaaattgg	aatacaacta	taactcacac	aatgtataca	tcatggcaga	caaacaaaag
		+					E0040				•	
	701	∍aatggaa	tca a	agttaactt	caaaattaga	cacaacattg	aagatggaag	cgttcaacta	gcagaccatt	atcaacaaaa	tactccaatt •	ggcgatggcc
							E0040					
	801	otgtcct	ttt a	ccagacaac	cattacctgt	ccacacaatc	tgccctttcg F0040	aaagatccca	acgaaaagag	agaccacatg	gtccttcttg	agtttgtaac
	901	agctgct	aaa a	ttacacatq	acatadataa	actatacaaa		agagccaggc	atcaaataaa	acqaaaqqct	cagtogaaag	actoggcctt
	001	+	999 ~		0040				B001			3019990011
	1.00	1 toattt	ato t	attattat	cantassono	tototactan	antcacactn	gctcaccttc	agatagaeet	++c+aca+++	ata	
	100.	+		B0010	cygryaacyc	tetetactag		B0012	gggrgggccr		aca	
		+00000000	Ð				=======================================	T7 TE	Stop	AAAAAA		
									PolyA			

# The underlying model

Finding circuits







promoter start RBS protein code stop

TGC CAGGAC TTGCCAGGAAG CCCAGATGCAGTCTTTTACGTGCCGAAAC









promoter

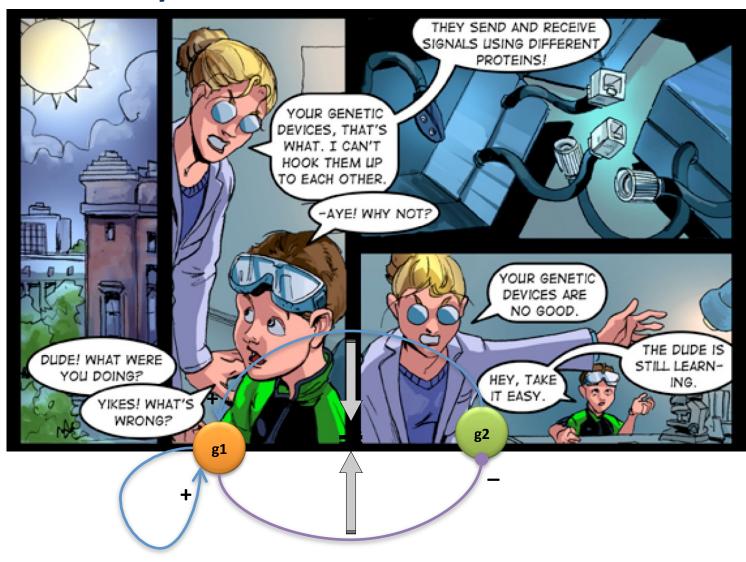
ribosome binding site

sequence coding for the protein

stop codon

#### **Compositionality?**

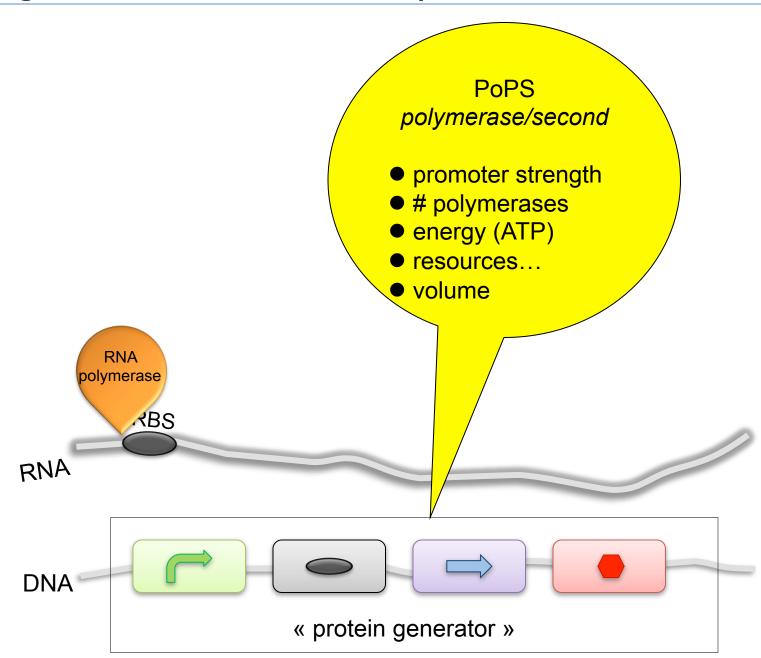


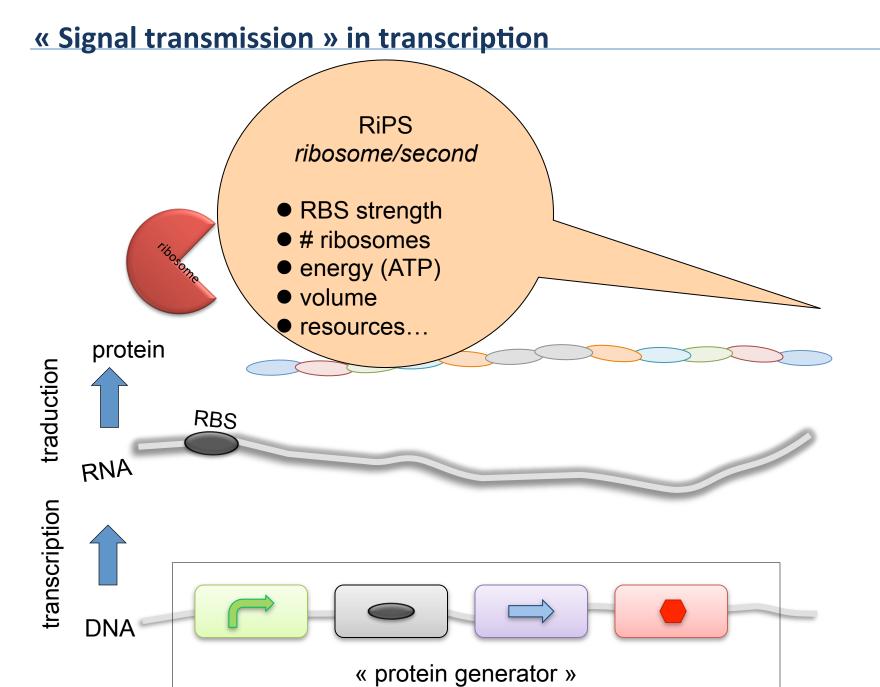


# → compartmentalization

#### « Signal transmission » in transcription







(	(B)
L	MGS

	Computational tool Use		Website <sup>‡</sup>
	21U-RNA	Scoring 21U-RNA-associated upstream motifs	Bartel laboratory introduction to 21U-RNAs
	Antimony*	Programming language describing synthetic biological devices	Deepak laboratory syntax guide
	Athena*	Build and simulate genetic circuits (implemented in C++)	Deepak laboratory downloads
	BioJade*	Synthetic biology design and simulation (implemented in Java)	Biolade
	CAD of modular protein devices	Modular protein device algorithm using a backbone of scaffold proteins <sup>82</sup>	None
	ESSA	RNA secondary structure analysis	ESSA
	Evolutionary design of genetic networks in silico	Algorithm to evolve small gene networks (modules) that perform basic tasks, such as toggle switches or oscillators <sup>§1</sup>	None
	GeneDesign*	Editing protein sequences and generating oligos for protein construction (implemented in Perl)	Gene Design
	GeNetDes*	Transcriptional network design tool using simulated annealing optimization	<u>Genetdes</u>
	GenoCAD*	Design of complex genetic constructs from standard parts library	GenoCAD
	MiRscan	Scoring of hairpins versus some experimentally verified microRNAs from Caenorhabditis elegans or Caenorhabditis briggsae	MiRscan
	OptCircuit	Identifies circuit components and suggests circuit topologies to attain desired outcome <sup>85</sup>	None
	PCEnv*	$Environment for simulating \ various \ types \ of \ Cell ML \ models$	<u>OpenCell</u>
	PROTDES*	Computational protein design	<u>PROTDES</u>
	Random Sampling-High Dimensional Model Representation	Global sensitivity analysis algorithm that is useful in optimizing genetic circuit properties not available from experiments or modelling <sup>86</sup>	None
	Registry of Standard Biological Parts and Clotho*	Creation, cataloguing and public availability of modular biological parts that are extensively characterized; Clotho is a database for managing these parts	Registry of Standard Biological Parts and Clotho Development
	RNA world website	Compendium of RNA software	RNA world
	RNAdraw	RNA secondary structure analysis	RNAdraw
	RNAMotif	Database search for RNA sequences that match a secondary structure motif	Rutgers Case Group
	RNAstructure	RNA secondary structure analysis	RNAstructure
	RnaViz	RNA secondary structure images	<u>RnaViz</u>
	Rosetta package	Design of protein-binding peptide sequences and protein engineering	Rosetta @ home and Rosetta Commons
	RoVerGeNe*	Tool to analyse and tune gene networks	<u>RoVerGeNe</u>
	SynBioSS*	Suite of programs to generate and simulate synthetic biological networks	<u>SynBioSS</u>
	Tinkercell	Synthetic biology CAD program	Tinkercell
	UNAFold software	Nucleic acid folding and hybridization	<u>UNAFold software</u>
	Vienna RNA package	RNA secondary structure	<u>Vienna RNA package</u>

Purnt & Weiss, Nature Reviews, June 2009.

# Analysis & Design of Fluid Machines as Non Conventionnal Programing

What is the "VHDL" for molecular interaction network and beyond?

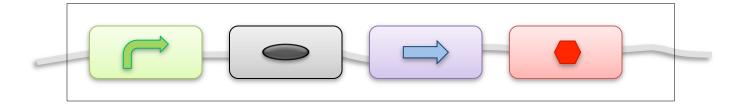
# The general picture



- 1 Design requires a model synthetic biology as the constructive part of systems biology a model is a program in some programing language
- (2) Abstraction level: alternation of
  - deterministic / stochastic
     (noise, chemical fluctuation, etc.)
  - continuous / discrete
     aggregate versus agent-based models
- 3 The structure of fluid machines changes in time:
  - dynamical systems with a dynamic structure (DS)<sup>2</sup>
  - Think globally, program locally:
    - datasheet (static) vs. rules set
    - space matters

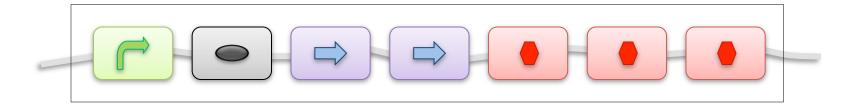






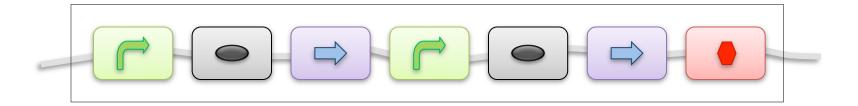
# Valide or not?





# Valide or not?





# Valide or not?



### Can we restrict the construction

- a priori (syntax/type discipline)
- a posteriori (verification, validation, test)

### Such that compositions of biobricks:

- have the expected functional properties
- make an autonomous system (modularity)
- Can themselves be composed (reuse)
- → This are problems addressed in a programming language example: register allocation by a compiler and choice of genes

Is this language a "Biobricks composition language"?



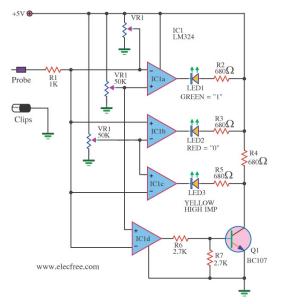
# The composition of biobricks does not address all problems:

- Which semantics for/characterization of the biobricks?
- Cell vs. population

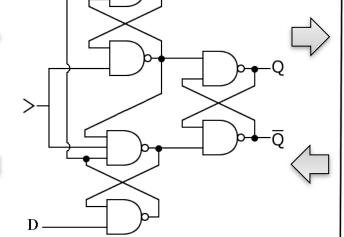
Bioprocesses as a special kind of dynamical systems

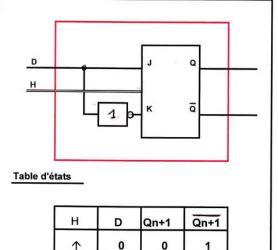
# 2 A tower of languages











Qn

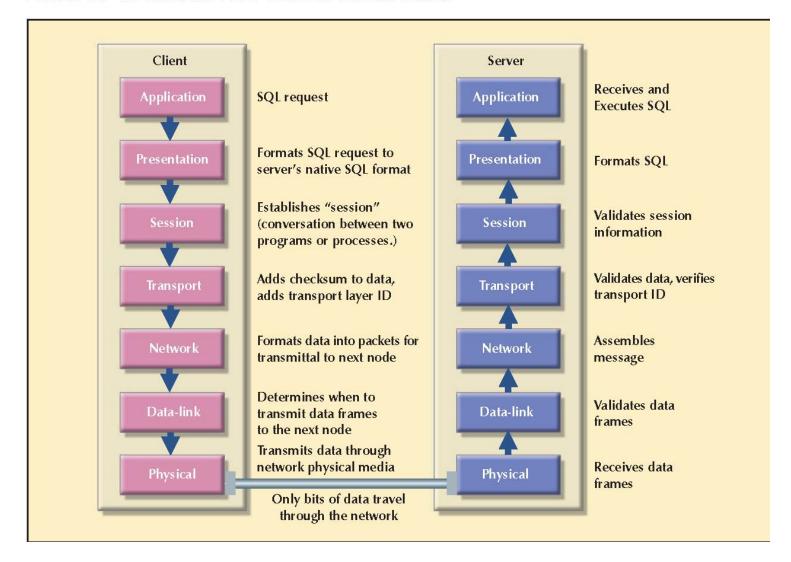
940508-2

electronic (electric currents) [spice] logic (gates) [sequential logic] function (register) [transition system]

# 2) A tower of languages with a lot of levels



FIGURE F.7 INFORMATION FLOW THROUGH THE OSI MODEL





Vertical abstraction *or* horizontal compositionality ?

**Systems** 

Devices x

Assembly of biobricks implementing a function (inverters, oscillateurs, switch, ...)

**Parts** 









**BIOBRICKS** 

Long term

Applications

**DNA** 

ACCTGCCAGGAATGCAGTCCCTTTT

Sequences of nucleotides





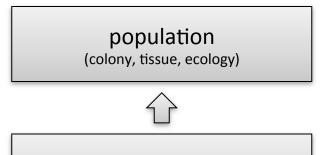
# The composition of biobricks does not address all problems: Which semantics for the biobricks?

- Chemical interactions are fundamentally stochastic
  - → stochastic modeling
  - amorphous computation
- Some bioprocesses implies only few entities:
  - discrete, agent-based modeling
- Some processes are aggregation of a lot of lower level processes
  - continuous modeling

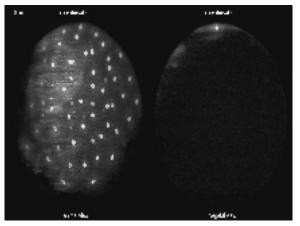


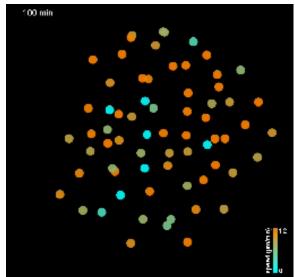
The composition of biobricks does not address all problems:

- cell vs. population: colony, biofilm, tissue, organism, ecology
- → global behavior vs. local behavior
- → spatial abstraction
- → morphogenesis



bionetwork (regulation, signalization, metabolic, ...)

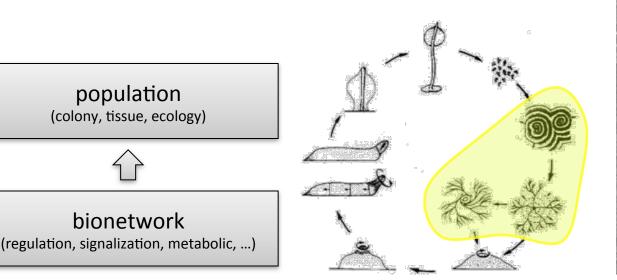




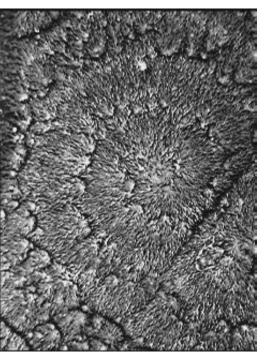


The composition of biobricks does not address all problems:

- cell vs. population: colony, biofilm, tissue, organism, ecology
- → global behavior vs. local behavior
- → spatial abstraction
- → morphogenesis



Dictyostelium discoideum



Marcus Hauser



The composition of biobricks does not address all problems:

- cell vs. population: colony, biofilm, tissue, organism, ecology
- → global behavior vs. local behavior splitting a function over a population of bacteria
  - to reduce the cell overload
  - because some sub-functions are chemically incompatibles
  - because some sub-functions are sequential
  - for resources mapping (compiler)
  - for reuse (modularity at bacteria level)
  - for security (auxotrophic device)
  - etc.



The composition of biobricks does not address all problems:

Bioprocesses as dynamical systems?

C: continuous D: discrete	PDE	ODE	Iterated Mappings	Finite Automata
State	С	С	С	D
Time	С	С	D	D
Space	С	D	D	D



### The composition of biobricks does not address all problems:

- Bioprocesses as dynamical systems?
  - Entities involved are dynamic and cannot be listed a priori chemical complex (EGF with receptor network = 10<sup>33</sup> species) cellular duplication, apoptosis, reproduction, ...
  - Interactions are localized (compartment) (vesicle, cargo, membrane, etc.) and compartments are dynamically created
- → Dynamical systems with a dynamic structure : the state space is build with the process itself
  - → <u>no</u> *a priori* global description
  - evolution rules must be local
  - → the global evolution is the "integration" of local evolutions





### THE CHEMICAL BASIS OF MORPHOGENESIS

By A. M. TURING, F.R.S. University of Manchester

(Received 9 November 1951—Revised 15 March 1952)

In determining the changes of state one

should take into account

- (i) The changes of position and velocity as given by Newton's laws of motion.
- (ii) The stresses as given by the elasticities and motions, also taking into account the osmotic pressures as given from the chemical data.
  - (iii) The chemical reactions.
- (iv) The diffusion of the chemical substances. The region in which this diffusion is possible is given from the mechanical data.

# The need for (DS)<sup>2</sup>?



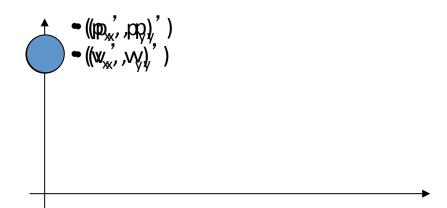


### THE CHEMICAL BASIS OF MORPHOGENESIS

By A. M. TURING, F.R.S. University of Manchester

(Received 9 November 1951—Revised 15 March 1952)

### a falling ball



at any time a state is a position and a speed

A dynamical system (DS)

### The need for (DS)<sup>2</sup>?





### THE CHEMICAL BASIS OF MORPHOGENESIS

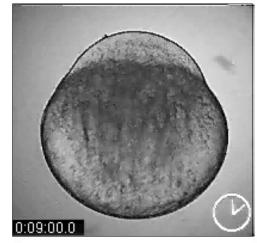
By A. M. TURING, F.R.S. University of Manchester

(Received 9 November 1951—Revised 15 March 1952)





### a developing embryo



at any time a state is a position and a speed

A dynamical system (DS)

the structure of the state
(chemical and mechanical state of each cell)
is changing in time
namical system with a dynamical structure

A dynamical system with a dynamical structure (DS)<sup>2</sup>

### The interplay between state and form





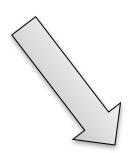
### a developing embryo

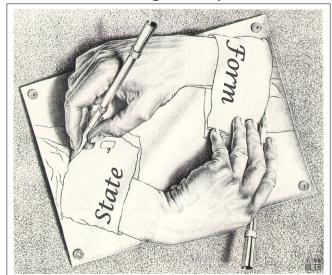
the state **as well as the structure of the state** is changing in time

(chemical and mechanical state of each cell **as** well as the arrangement of the cells)

"Strange loop"







### **Dynamics OF form**



A dynamical system with a dynamical structure (DS)<sup>2</sup>

### The need for (DS)<sup>2</sup>?





### THE CHEMICAL BASIS OF MORPHOGENESIS

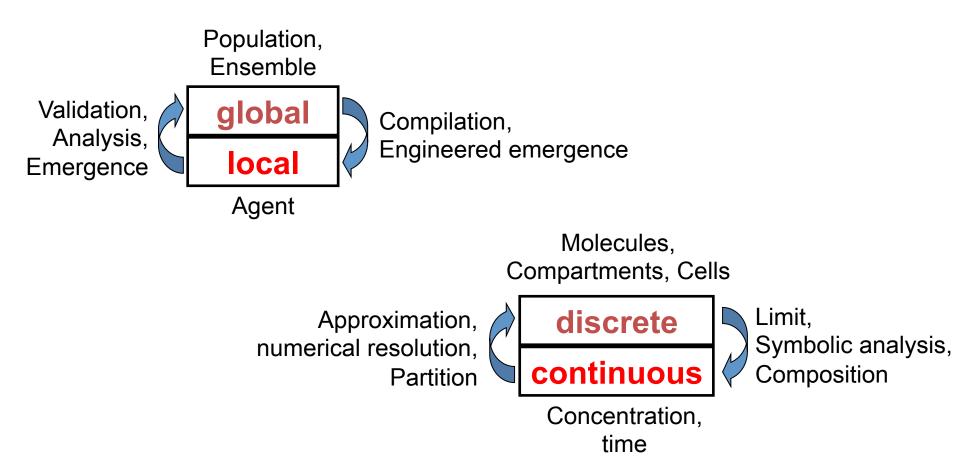
By A. M. TURING, F.R.S. University of Manchester

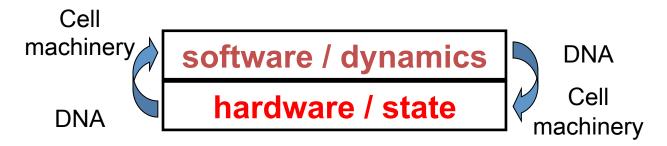
(Received 9 November 1951—Revised 15 March 1952)

It might be possible, however, to treat a few particular cases in detail with the aid of a digital computer. This method has the advantage that it is not so necessary to make simplifying assumptions as it is when doing a more theoretical type of analysis. It might even be possible to take the mechanical aspects of the problem into account as well as the chemical, when applying this type of method. The essential disadvantage of the method is that one only gets results for particular cases. But this disadvantage is probably of comparatively little importance.

### Three other challenges for a BS language







# The MGS project

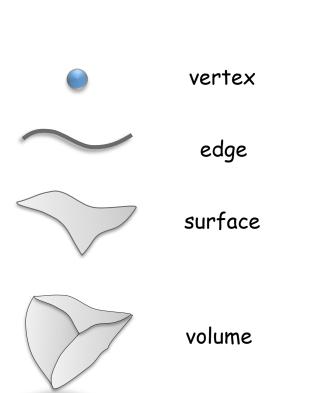
- Language dedicated to the simulation of (DS)<sup>2</sup>
- Declarative (declarative simulation vs procedural)
- Abstract rewriting of complex spatial structures:
  - Data structure = topological collections
     sequence, generalized array, (multi-)set, arbitrary graph, Delaunay
     triangulation, g-map, ..., cell complexes
  - Control structure = transformation
    - two powerful languages to specify sub-collections (elements in interaction)
    - Various rule application strategies: maximal parallel, asynchronous, stochastic, Gillespie-like, ...

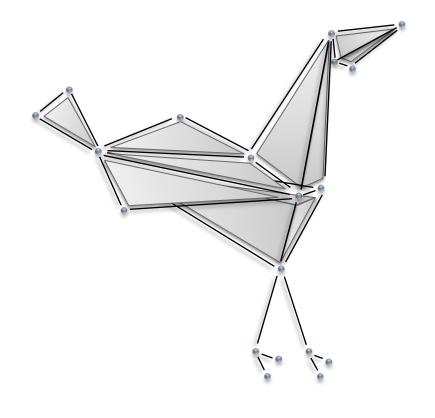
# **Topological collections**



### • Structure

- A collection of topological cells
- An incidence relationship



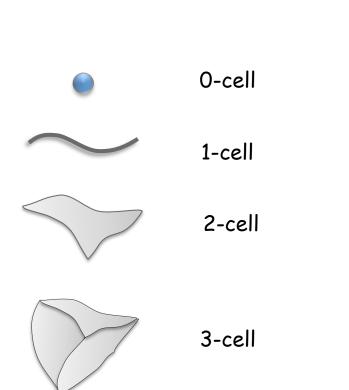


# **Topological collections**



### Structure

- A collection of topological cells
- An incidence relationship
- Data: association of a value with each cell





# Higher dimensional objects for complex simulations



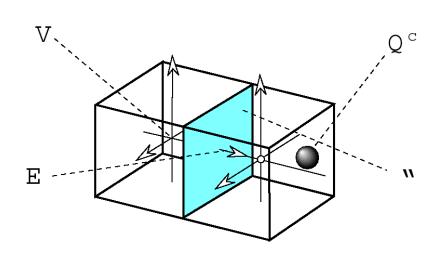
### Example of electrostatic Gauss law [Tonti 74]

- Electric charge content ρ : dimension 3
- Electric flux Φ: dimension 2
- Law available on a arbitrary complex domain

$$\phi = \iint w \cdot dS = \frac{Q^{c}}{\varepsilon_{0}} = \iiint_{(V)} \frac{\rho}{\varepsilon_{0}} d\tau$$

### electric field in space:

- V: electric potential (dim 0)
- E: voltage (dim 1)
- w: electric flux (dim 2)
- Qc: electric charge (dim 3)



A Direct Discrete Formulation of Field Laws: The Cell Method

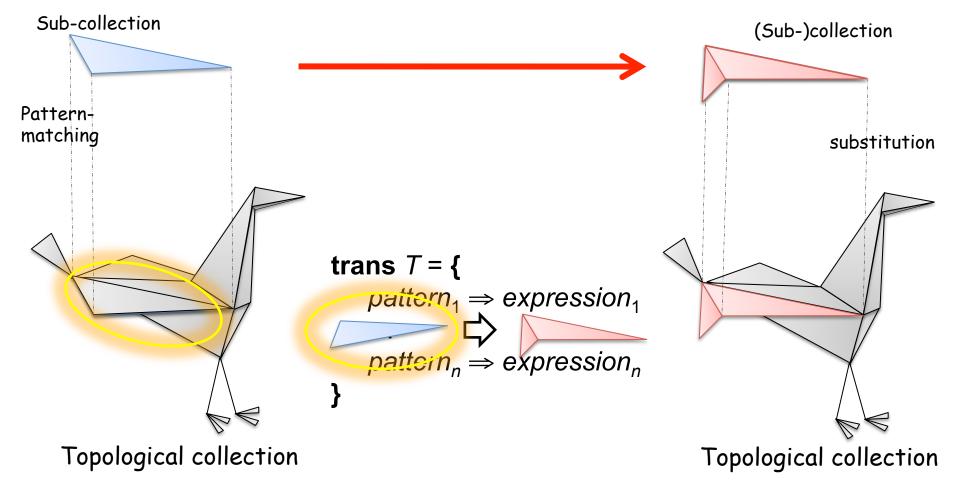
### **Transformations**



- Functions defined by case on collections
   Each case (pattern) matches a sub-collection
- Defining a rewriting relationship: topological rewriting

```
trans T = \{
pattern_1 \Rightarrow expression_1
...
pattern_n \Rightarrow expression_n
}
```



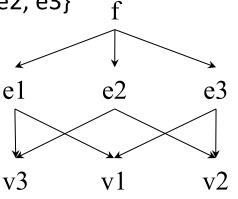


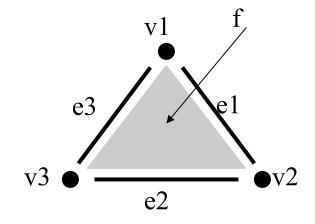
# **Abstract Simplicial Complex and simplicial chains**

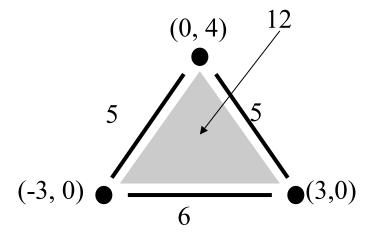


### *Incidence relationship and lattice of incidence:*

- boundary(f) =  $\{v1, v2, v3, e1, e2, e3\}$
- $faces(f) = \{e1, e2, e3\}$
- $cofaces(v1) = \{e1, e3\}$







### Topological chain

- coordinates with vertices
- lengths with edges
- area with f

$$\binom{0}{4} \cdot v_1 + \binom{3}{0} \cdot v_2 + \binom{-3}{0} \cdot v_3 + 5 \cdot e_1 + 6 \cdot e_2 + 5 \cdot e_3 + 12 \cdot f$$

# **Topological rewriting = transformation**



$$1 + 2 \rightarrow ...$$
 (arithmetic) term rewriting

string concatenation:  $\mbox{\tt w}$  .  $\mbox{\tt w}$  is a formal associative operation

$$2H + O \rightarrow H_2O$$
 multiset rewriting (~ chemistry)  
multiset concatenation (= the chemical soup): « . » is AC

$$v_1.\sigma_1 + v_2.\sigma_2 \rightarrow \dots$$
 topological rewriting (MGS)

gluing cell in a cell complex: ... (AC and algebraic machinery)

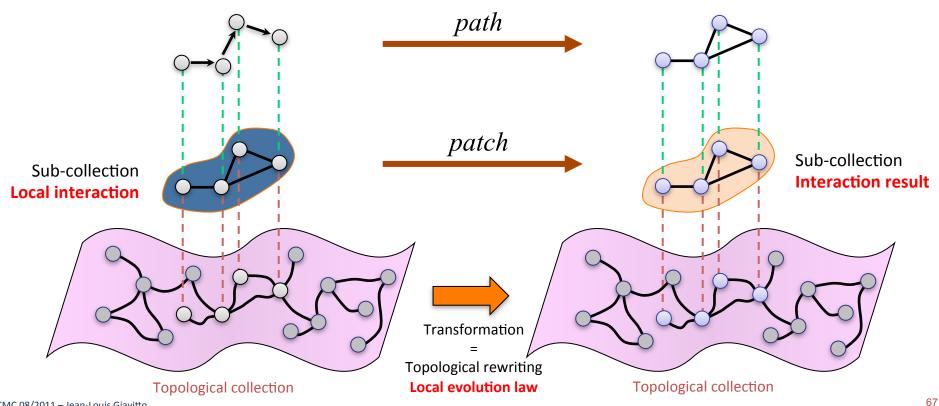
### **Transformation**



### Pattern matching: specifying a sub-collection of elements in interaction

- Path transformation (path = sequence of neighbor elements)
  - Concise but limited expressiveness
- Patch transformation (arbitrary shape)
  - Longer but higher expressiveness

Rule application strategy: maximal parallel, asynchronous, stochastic, etc.



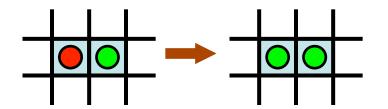
# **Example: Diffusion Limited Aggregation (DLA)**

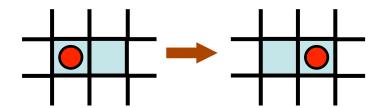


- Diffusion: some particles are randomly diffusing; others are fixed
- Aggregation: if a mobile particle meets a fixed one, it stays fixed

```
trans dla = {
   `mobile , `fixed => `fixed, `fixed;
   `mobile , <undef> => <undef>, `mobile
}

NEIGHBOR OF
```





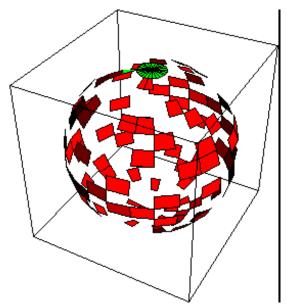
# **Example: Diffusion Limited Aggregation (DLA)**

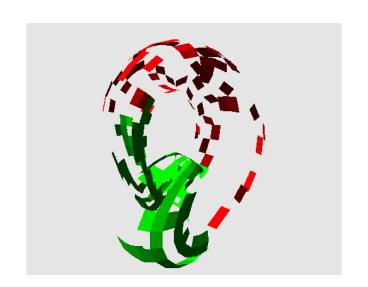


- Diffusion: some particles are randomly diffusing; others are fixed
- Aggregation: if a mobile particle meets a fixed one, it stays fixed

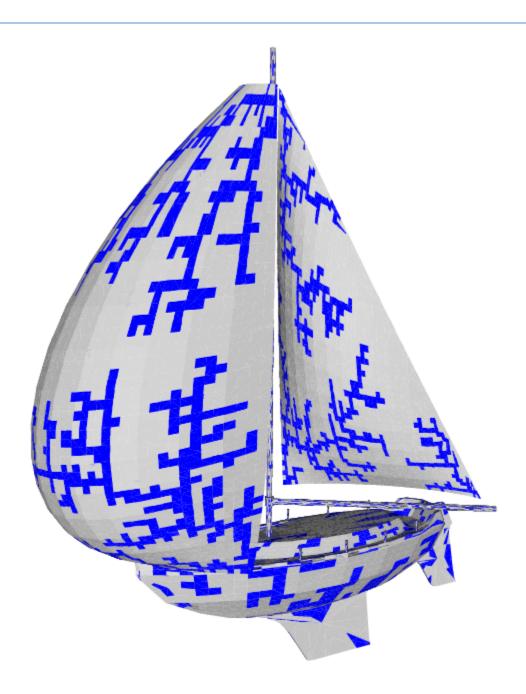
```
trans dla = {
    `mobile , `fixed => `fixed, `fixed ;
    `mobile , <undef> => <undef>, `mobile
}
```

this transformation is an abstract process that can be applied to any kind of space



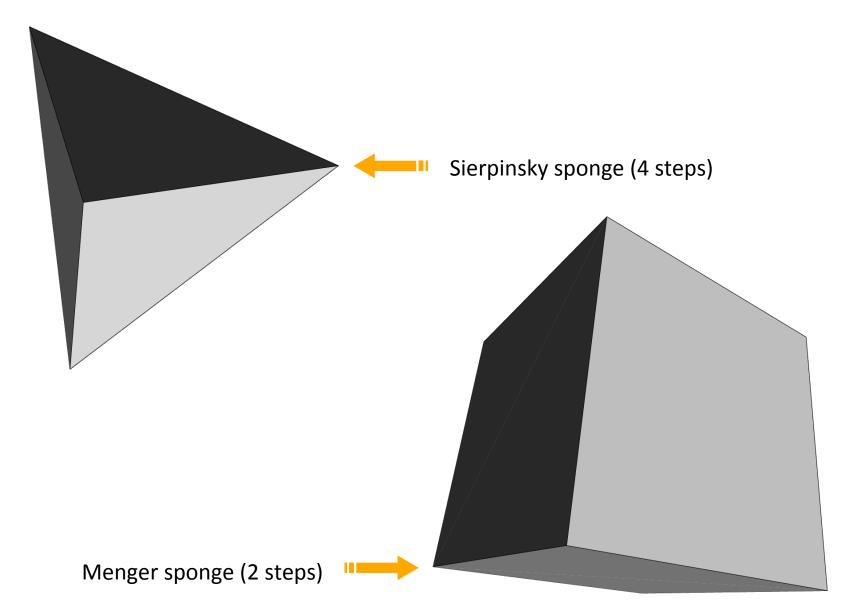






# Fractal construction by carving





# Two examples

- 1. Meristem growth
- 2. An iGEM project



#### Pierre Barbier de Reuille

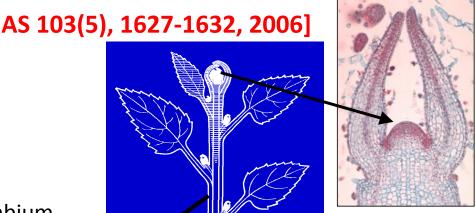
Mikaël Lucas Jan Traas Christophe Godin CIRAD/INRA/INRIA







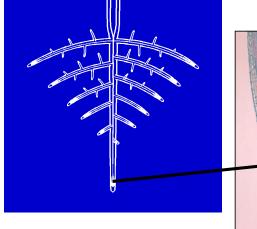
The Growth of a Meristem



Shoot apical meristem

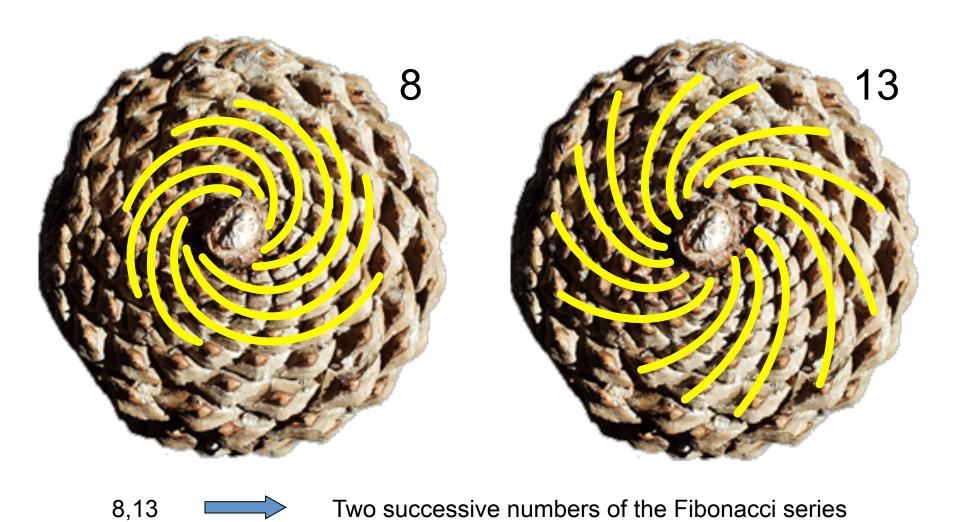




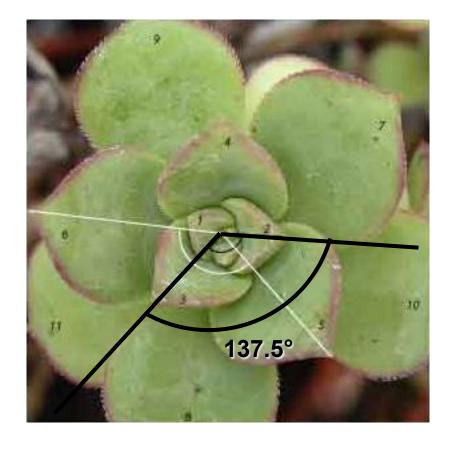








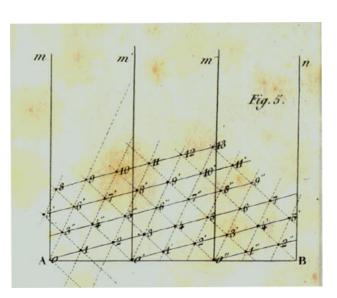




### Phyllotaxis models: three kinds of approaches

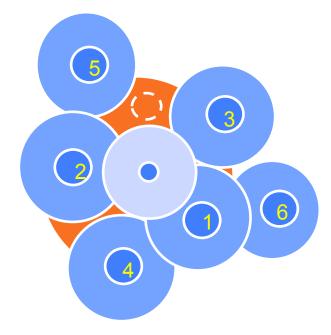


Geometrical



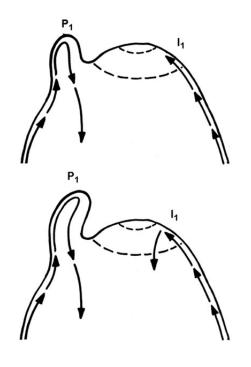
(Bravais & Bravais, 1837)

**Dynamical** 



(Hofmeister, 1868) (Snow and Snow, 1962)

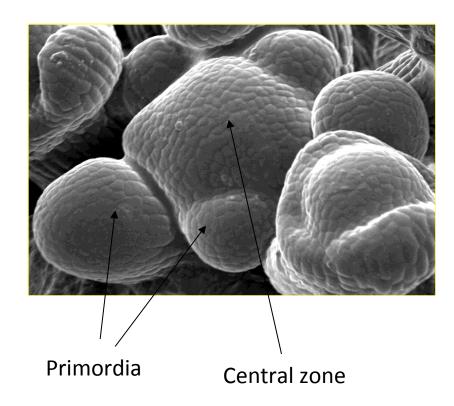
**Physiological** 



(Reinhardt et al., 2000)

## A shoot apical meristem





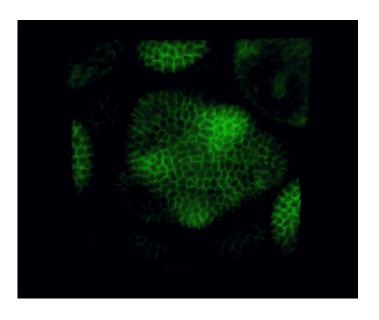
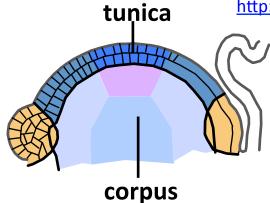


Image sequence showing cell division patterns via membrane-bound PIN1, in Shoot Apical Meristem (SAM), nearby floral meristems, and the boundaries between them (M. Heisler). <a href="http://computableplant.ics.uci.edu/">http://computableplant.ics.uci.edu/</a> (E. Mjolness)



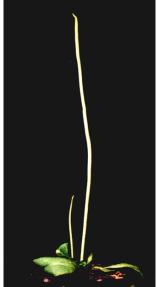
## **Active transport of auxine**

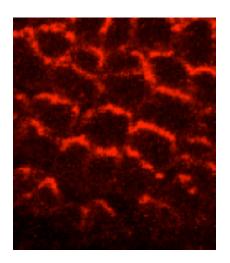


wild type

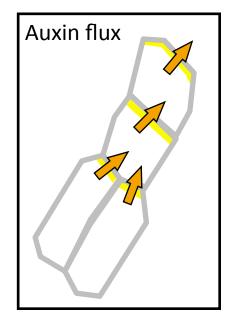


pin-1 mutant





Immunolabelling of PIN-FORMED1 protein

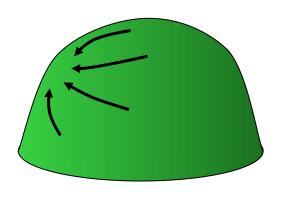




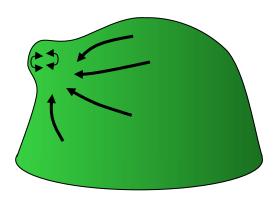
high concentration of auxine induces organ initiation



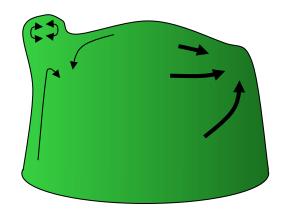




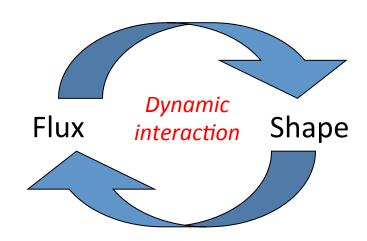




changes form...



which changes flux...



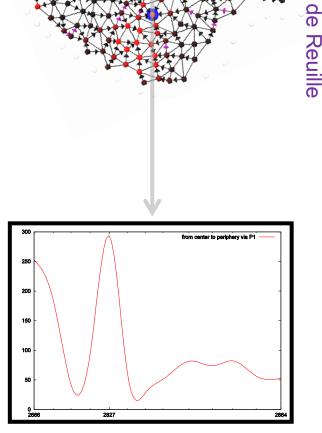
#### Model

MGS

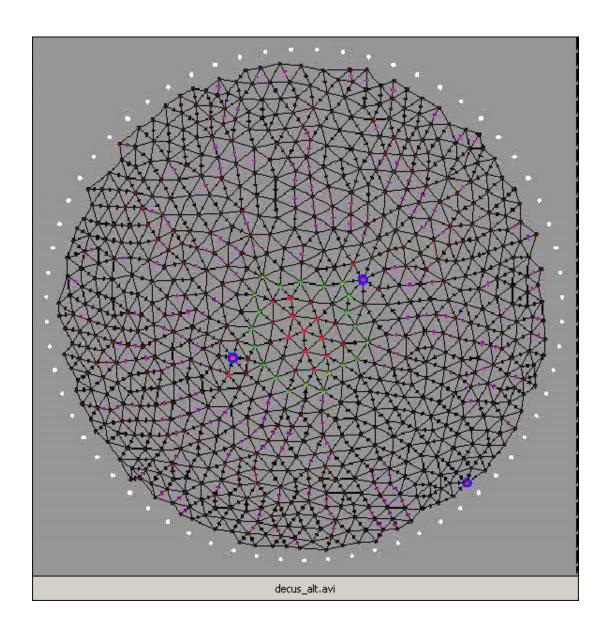
- Cell internal state and processes
  - capacity of division, springs relaxed length, primordium/center, concentration of auxin, auxin degradation / evacuation, inhibitor promotion to primordium, "pump magnetism"
- Movement (due to cell growth)
- Growth: increase of spring relaxed length
- Division: when size > threshold
- Cell interaction

Passive diffusion of auxin, active pumping of auxin

```
trans Auxin = {
    x, y / pump(x,y)
    \rightarrow x+{x.auxin -= \delta}, y+{y.auxin += \delta}
}
```

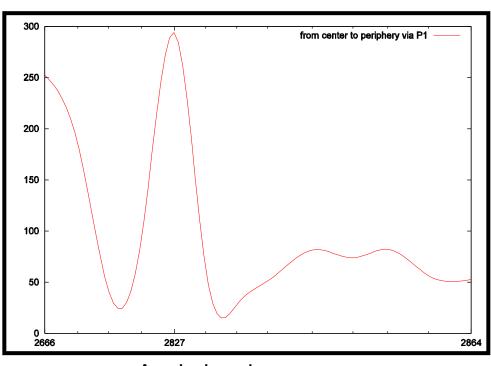








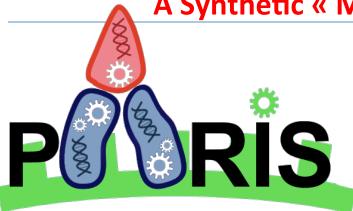




Auxin level

#### A Synthetic « Multicellular Bacterium »





View Part BBa\_

CIVIC UO/2011 - Jean-Louis Giavillo

#### Synthetic Biology is

- A) the design and construction of new biological parts, devices, and systems, and
- B) the re-design of existing, natural biological systems for useful purposes.

(Español)

Synthetic Biology Logo

Home About Conferences Labs

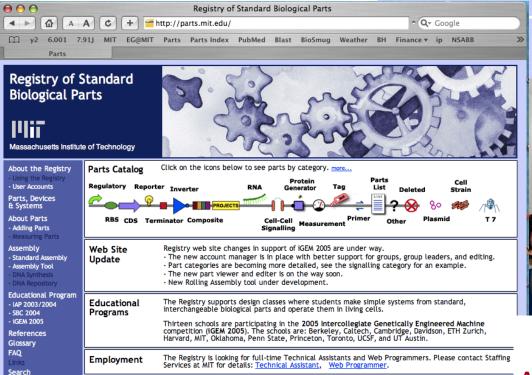
s Courses

Resources

FAQ

#### Community news

- IET Synthetic Biology first issue includes iGEM 2006
- Synthetic Biology 3.0 Zurich proceedings. Download here.
- BioBricks Foundation first membership drive.
- Synthetic Biology: Caught between Property Rights, the Public Domain, and the Commons
- US HSPD-18. Guidance on openness and international transparency in biodefense work still needed.



#### Resources

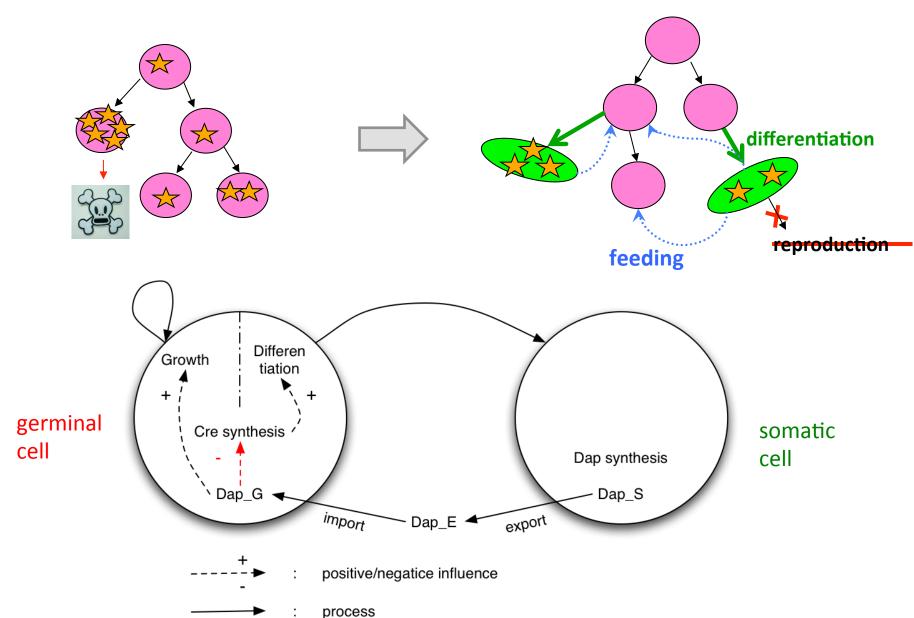
- Press articles
- · Publications: citeulike, connotea, PubMed



David Bikard, Thomas Landrain, David Puyraimond, Eimad Shotar, Gilles Vieira, Aurélien Rizk, David Guegan, Nicolas Chiaruttini, Thomas Clozel, Thomas Landrain

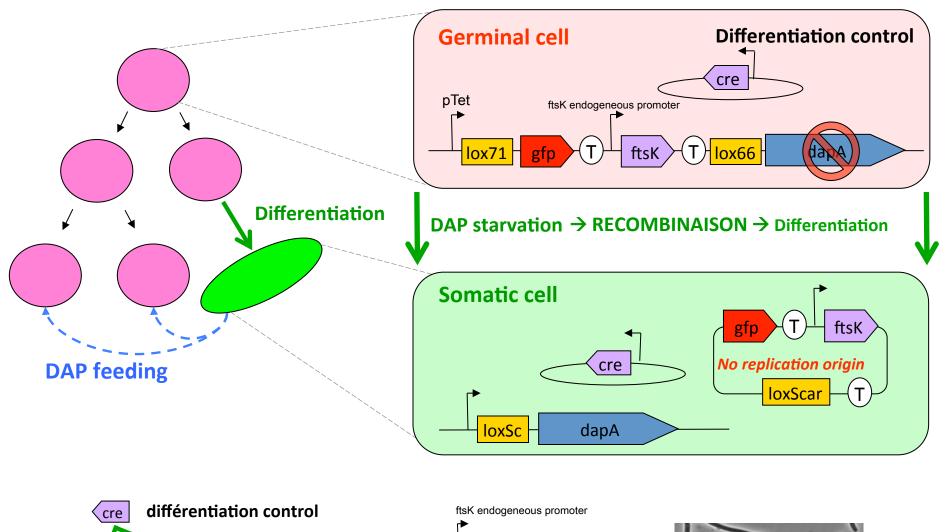
# The Paris iGEM project: a « multicellular bacteria » to decouple growth and transgene expression

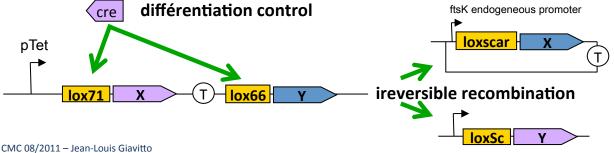


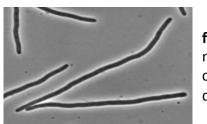


### **Design principle**









ftsK needed for cellular division

### **Anime**

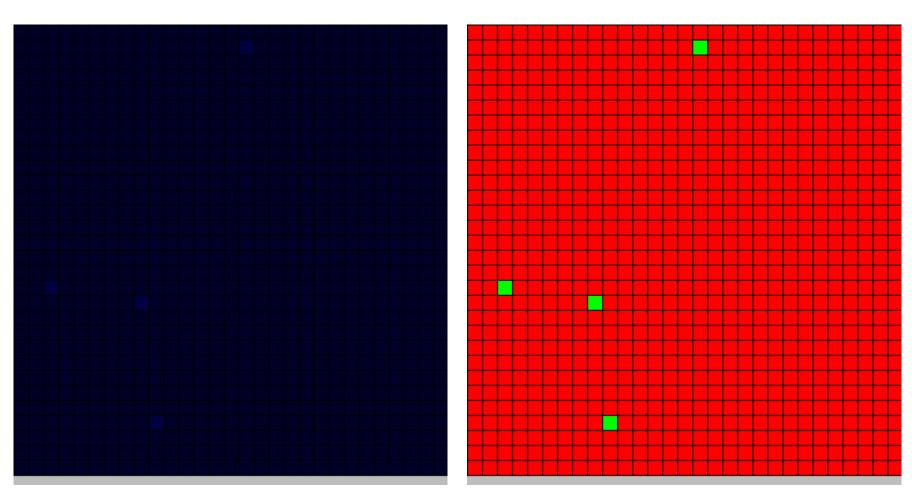




© David Bikar & the 2007 Paris iGEM team



How does differentiation induces feeding? (proof of concept)
 cellular automaton (in MGS)



diffusion of DAP

somatic and germ cell



- How does differentiation induces feeding? (proof of concept)
   cellular automaton (in MGS)
- How do spatial organization and distribution evolve? agents based system (in MGS)



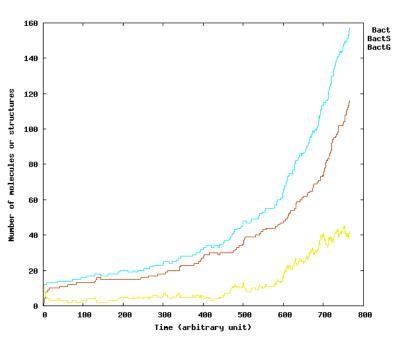


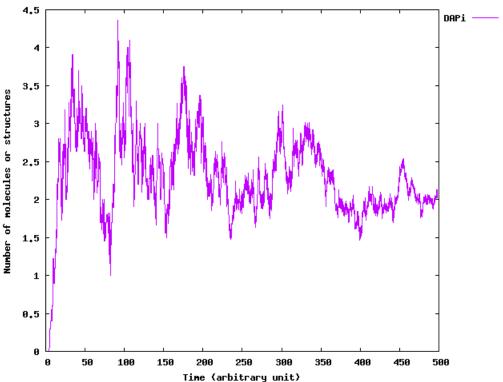
- How does differentiation induces feeding? (proof of concept) cellular automaton (in MGS)
- How do spatial organization and distribution evolve?
   agents based system (in MGS)
- How robust and tunable is the model?
   ODE kinetics (matlab)



- How does differentiation induces feeding? (proof of concept)
   cellular automaton (in MGS)
- How do spatial organization and distribution evolve?
   agents based system (in MGS)
- How robust and tunable is the model?
   ODE kinetics

How sensitive is the system to noise?
 Gillespie based simulation (in MGS)



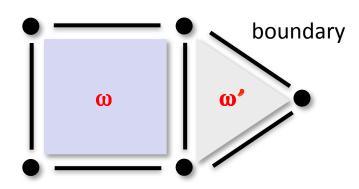


## Blurring the discrete/continuous barrier

#### **Cochains as (a special kind of) Transformations**



- The Boundary Operator  $\partial$ 
  - Starting point of the elaboration of a discrete diff. calculus
  - Transport of data from cells to their faces



Cochains notation

The boundary operator is a cochain cochain = chain  $\rightarrow$  chain

$$\partial = \sum_{\sigma \in \mathcal{K}} \partial_{\sigma} . \sigma \quad \text{with} \quad \forall \sigma \in \mathcal{K}, \ \partial_{\sigma}(g) = \sum_{\tau < \sigma} o_{\sigma\tau}(g) . \tau$$

MGS notation

trans Boundary = { 
$$x => CofacesFold(fun y acc -> o_{y^x}(y) +_G acc, 0_G, x) }$$

#### **Cochains as Transformations**



#### Derivative Operator d

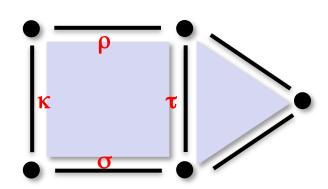
Defined w.r.t. the discrete Stockes' Theorem

$$[\mathbf{d}T, c] = [T, \partial c]$$

Cochains Notation
 One can show that the derivative verifies

$$\mathbf{d} = \sum_{\tau \in \mathcal{K}} \mathbf{d}_{\tau} . \tau \quad \text{with} \quad \forall \tau \in \mathcal{K}, \ \mathbf{d}_{\tau}(f) = \sum_{\tau < \sigma} (f \circ o_{\sigma\tau}) . \sigma$$

MGS Notation
 We directly use the Stockes' Theorem



let Derivative T = fun c -> T (Boundary c)

#### **Cochains as Transformations**



- Illustrative example : the Laplacian Operator  $\Delta$ 
  - The Laplacian in terms of ★ and d [Desbrun et al., 2006]

$$\Delta = \delta \mathbf{d} + \mathbf{d}\delta$$
 where  $\delta = (-1)^{n(k-1)+1} \star \mathbf{d} \star$ 

MGS notation

Big assumption: here the Hodge star ★ is the co-derivative d<sup>co</sup> assuming uniform geometry

#### **Cochains as Transformation**

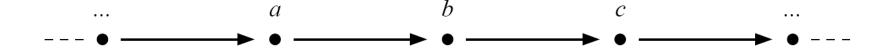


- Illustrative example : the Laplacian Operator  $\Delta$ 
  - Corresponding Data Transport (case of dimension 1)  $\Delta = \mathbf{d}^{co}\mathbf{d}$ 
    - Dimension 1:

 $\partial \circ \partial^{co}$ 

• Stockes' Theorem:

équivalence with

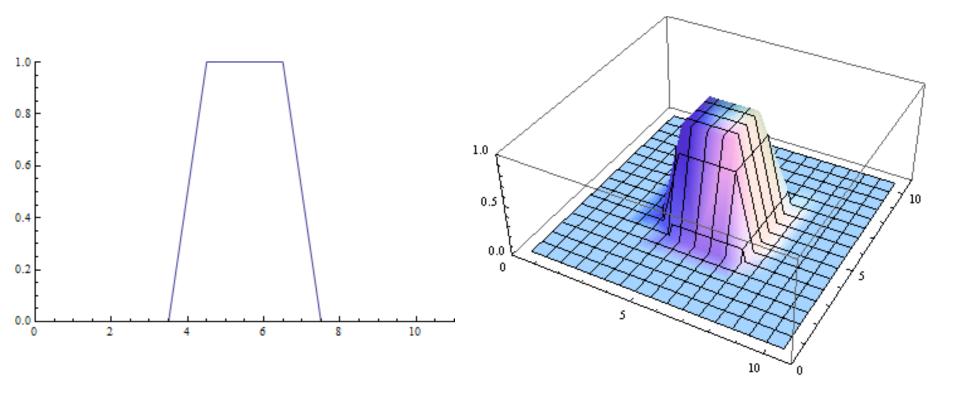


#### **Cochains as Transformation**



- Illustrative example : the Laplacian Operator  $\Delta$ 
  - Simulation of diffusion

$$\frac{\partial u}{\partial t} = D\Delta u \qquad \text{fun diffusion[D,orient](u) =} \\ u + D*Laplacian[orient=orient](Id)(u) ;;$$



#### Home message



New kind of computational machines with "dynamic structure" strange loop between structure and processes not new (program = data) but not understood (e.g., type discipline to avoid that)

2. Space matters compartmentalization and beyond

3. Killer app. systems & synthetic biology the nano-world: form=function

4. Usual tools of computer science are relevant but the focus, the questions and the answers are new e.g., termination in rewriting

5. Versatility of the MGS approach time evolution = rewriting strategy kind of space = kind of objects to be rewritten

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