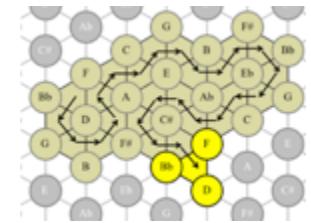
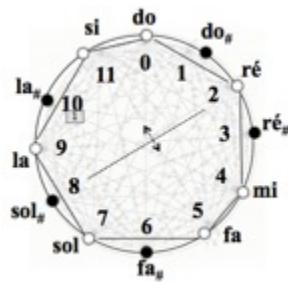


Modèles mathématiques et computationnels dans la chanson

Analyse de la musique et des répertoires III :

Musiques actuelles

(partie IV : modèles mathématiques et computationnels)



Moreno Andreatta

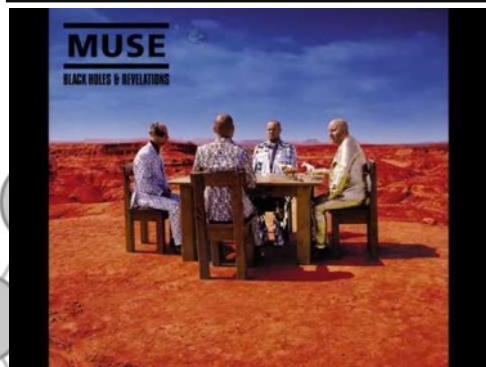
IRMA & ITI CREAA, Université de Strasbourg

Equipe Représentations Musicales

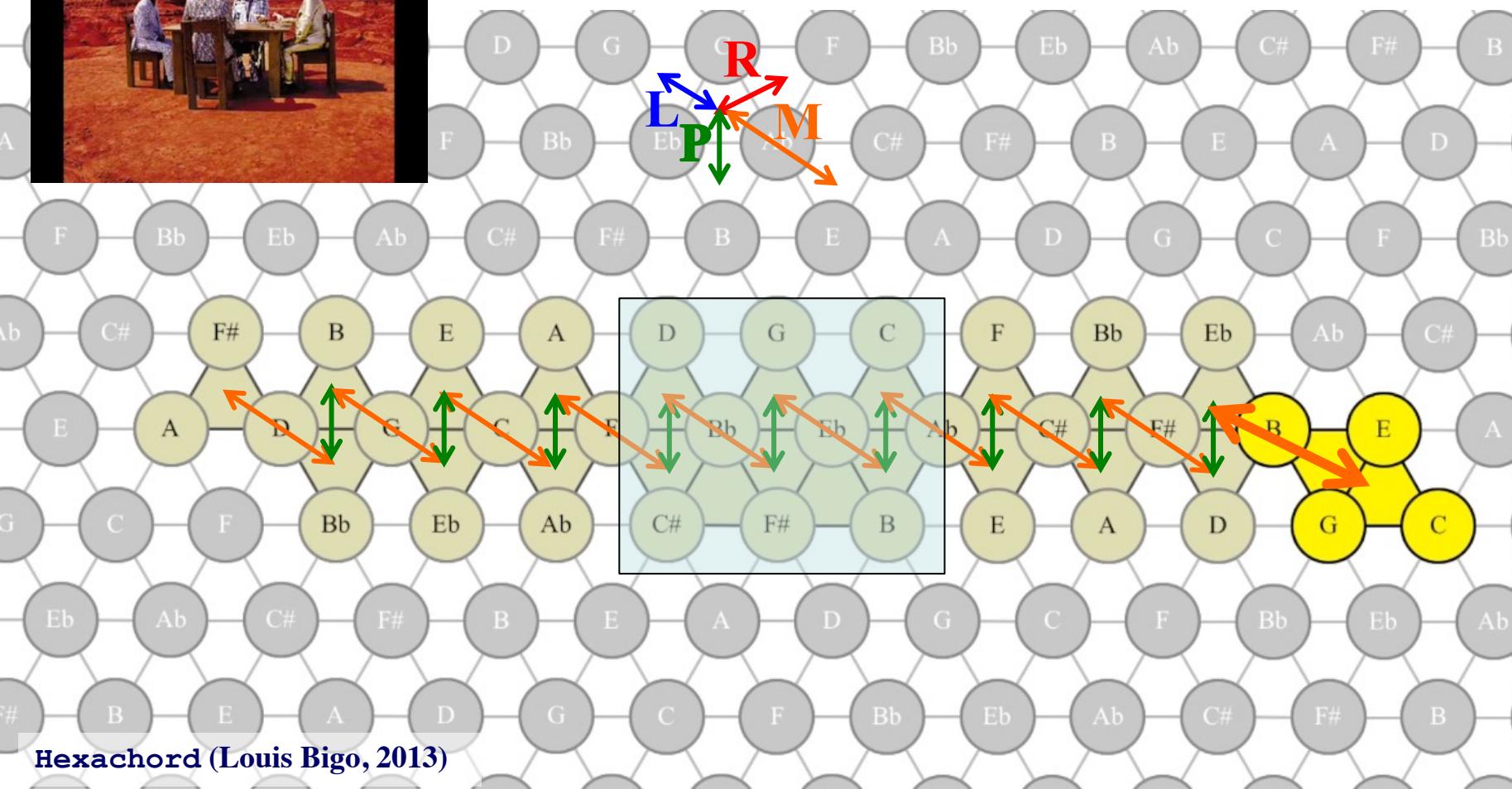
IRCAM / CNRS UMR 9912 / Sorbonne Université



Utilisation inconsciente (?) des symétries chez *Muse*



“Take a bow” (*Black Holes and Revelations*, 2006)

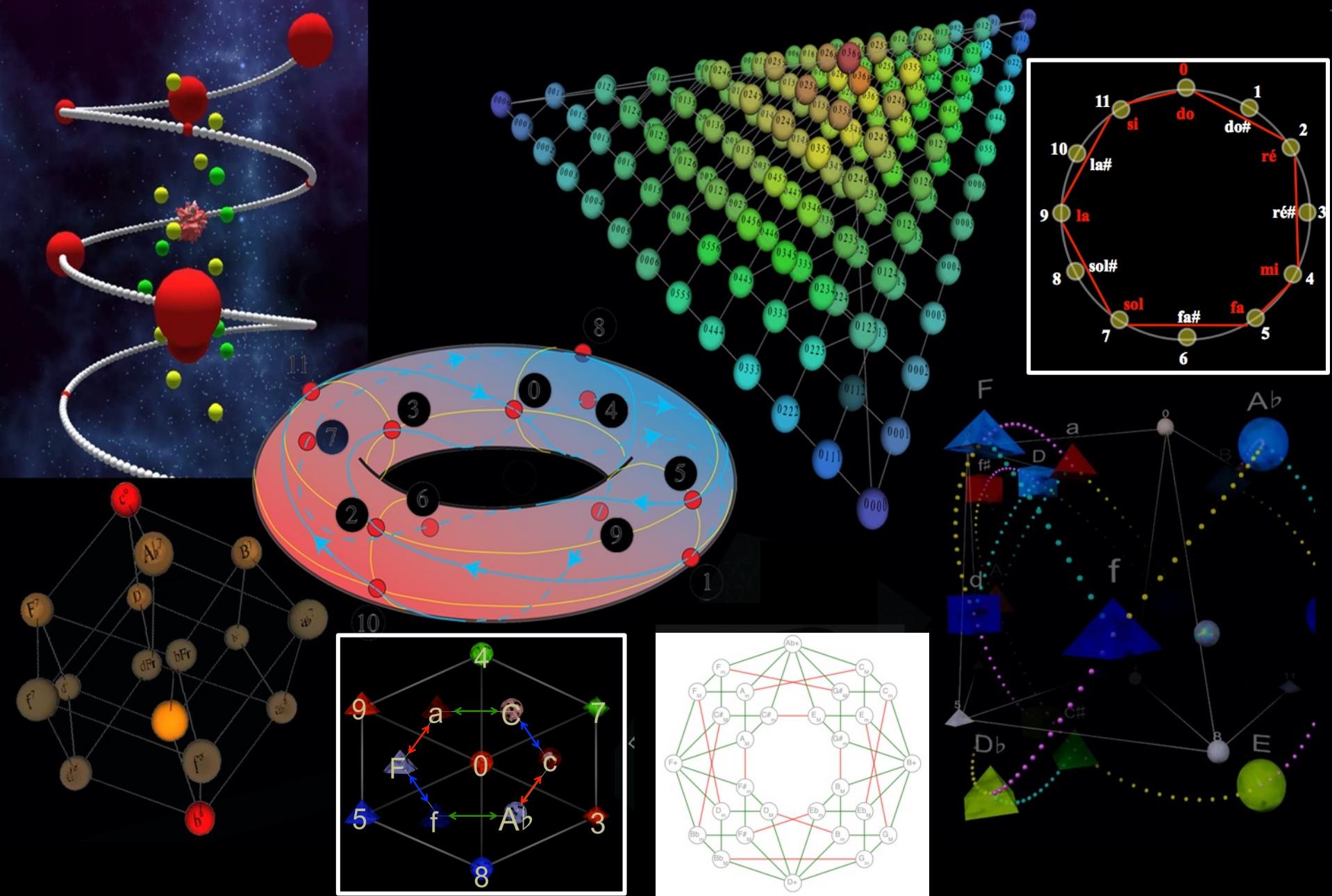


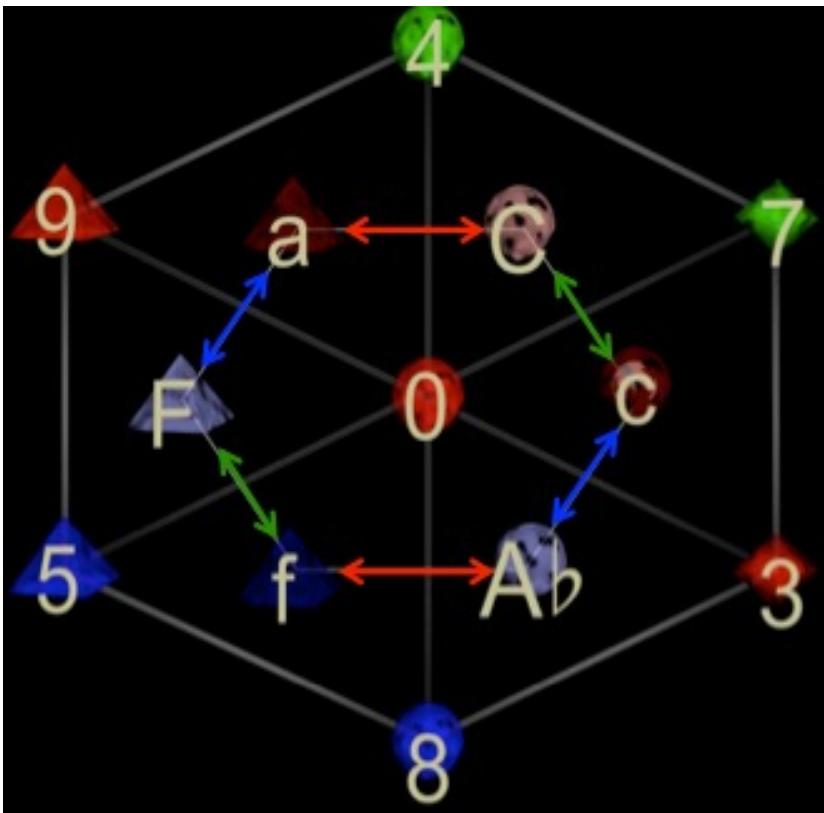
Hexachord (Louis Bigo, 2013)

axe temporel

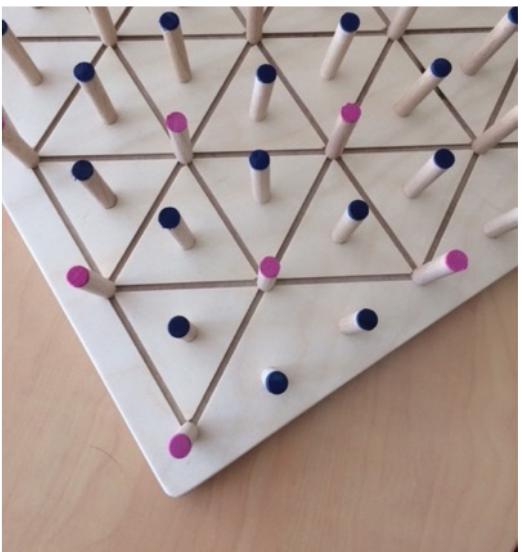
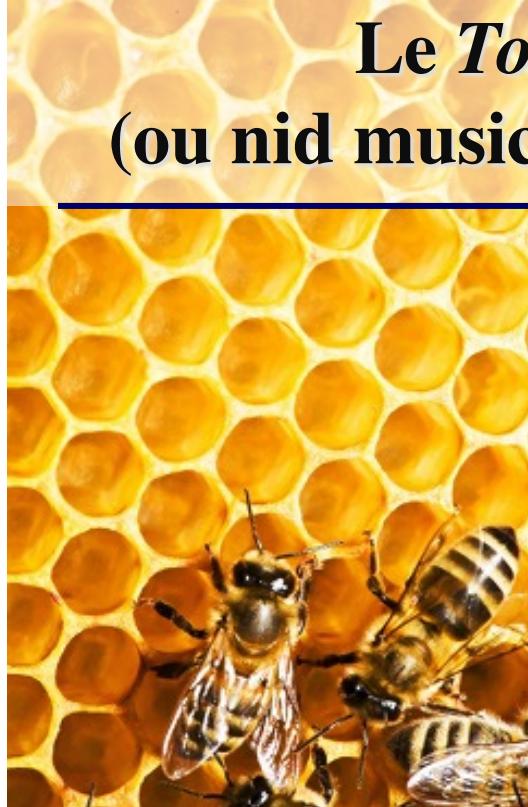
→ https://www.youtube.com/watch?v=NQ7LkWCzKxI&ab_channel=LouisBigo

La galaxie des modèles géométriques au service de la musique

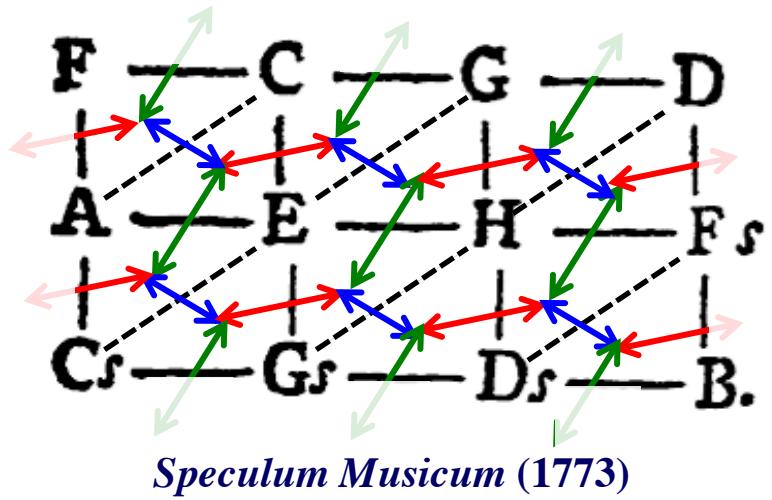




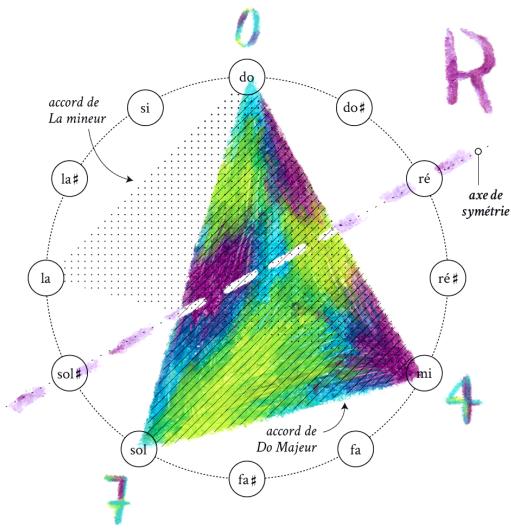
Le Tonnetz (ou nid musical d'abeilles)



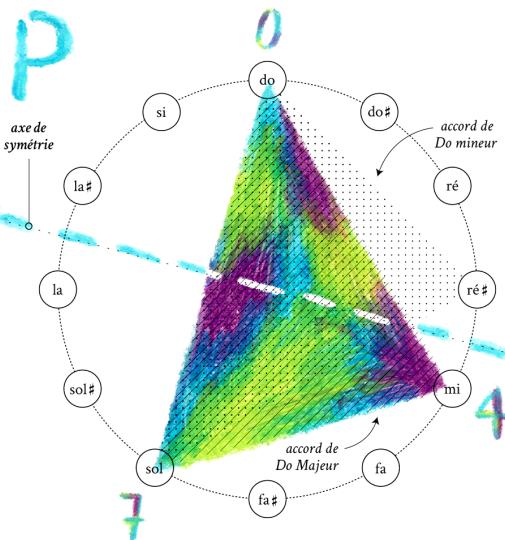
Leonhard Euler



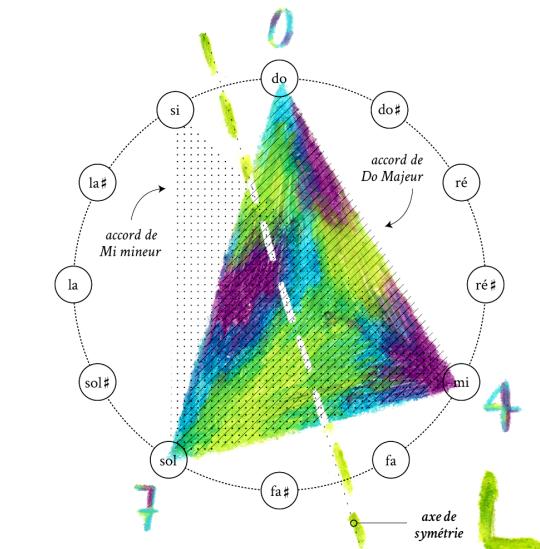
Les trois symétries néo-riemannniennes



R = RELATIF



P = PARALLÈLE



**L = LEADING-TONE
(EXCHANGE)**

C majeur



A mineur

C majeur



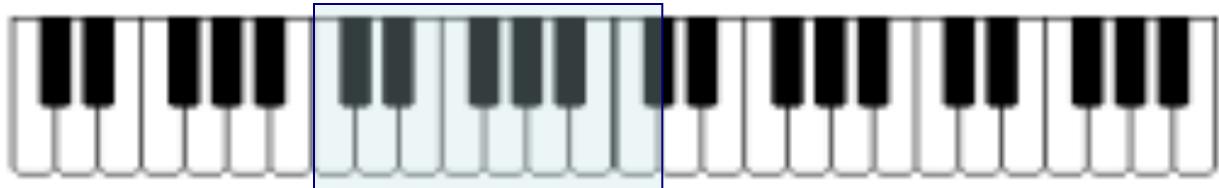
C mineur

C majeur



E mineur

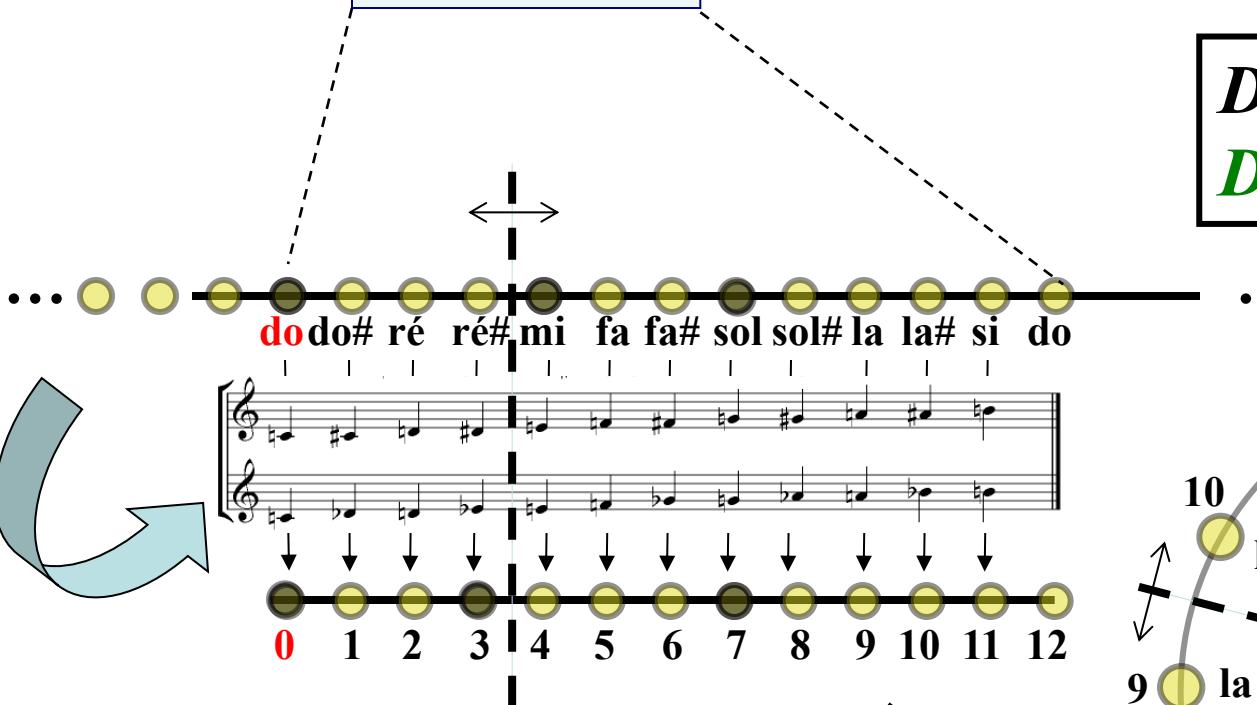
Les inversions sont des symétries axiales

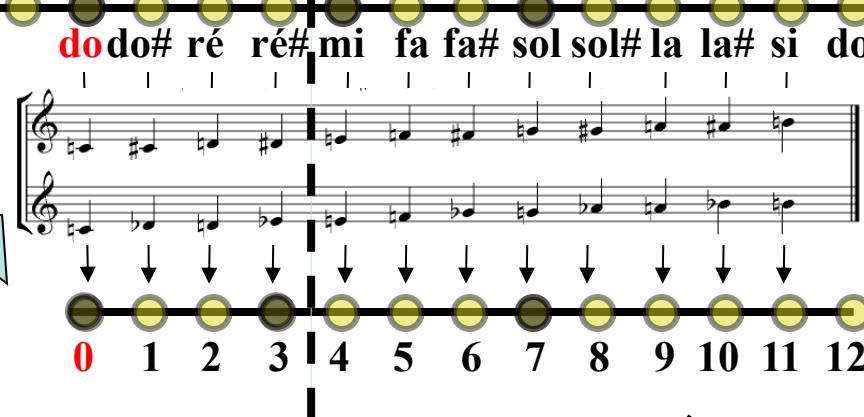
...  ...

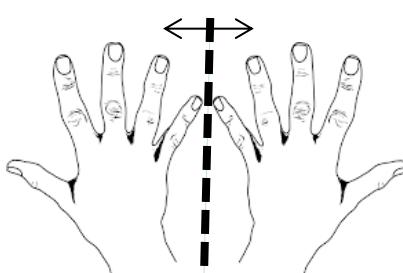
P comme parallèle

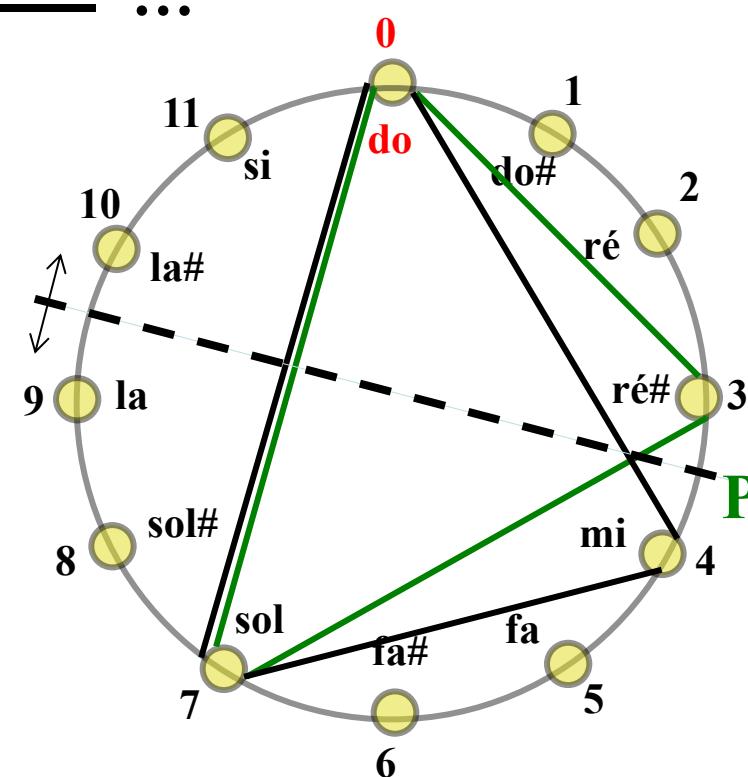
Do maj = {0,4,7}

Do min = {0,3,7}

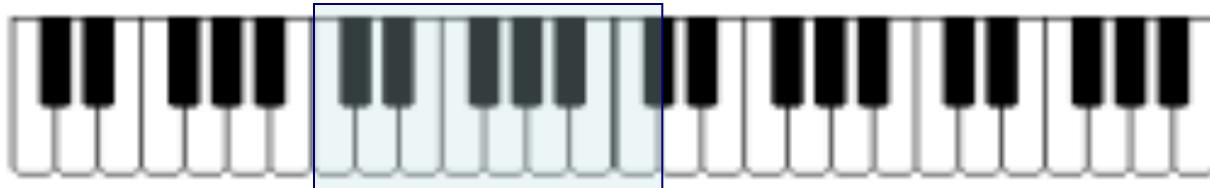
...  ...

...  ...

...  ...

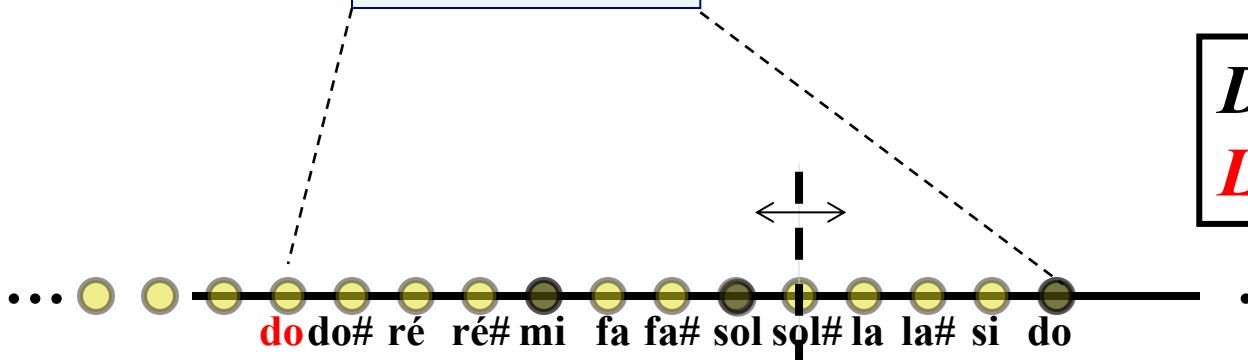
... 

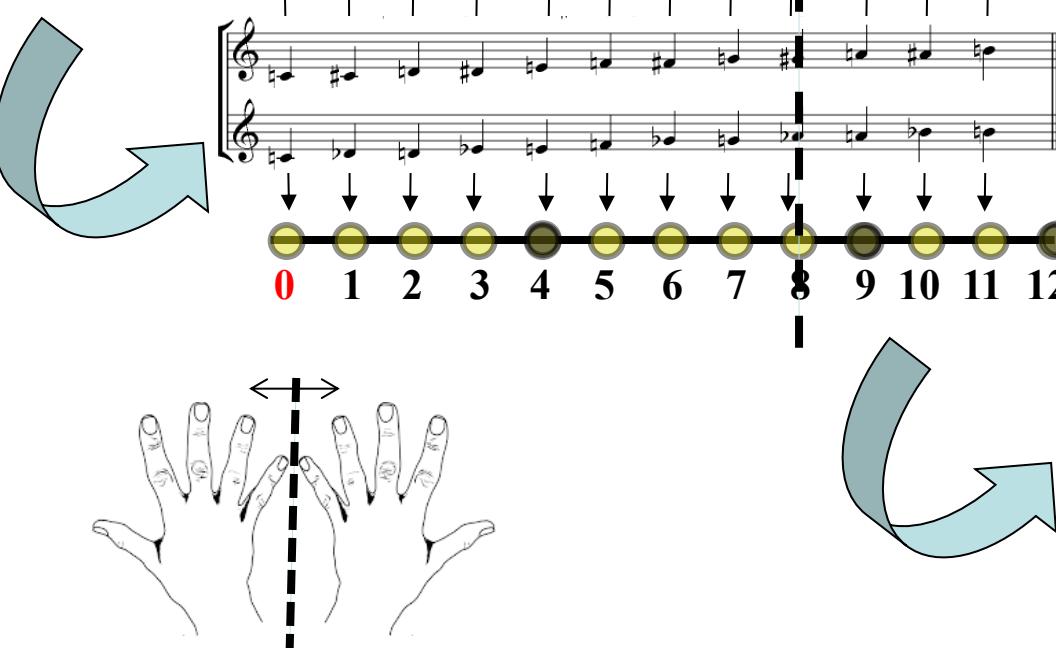
Les inversions sont des symétries axiales

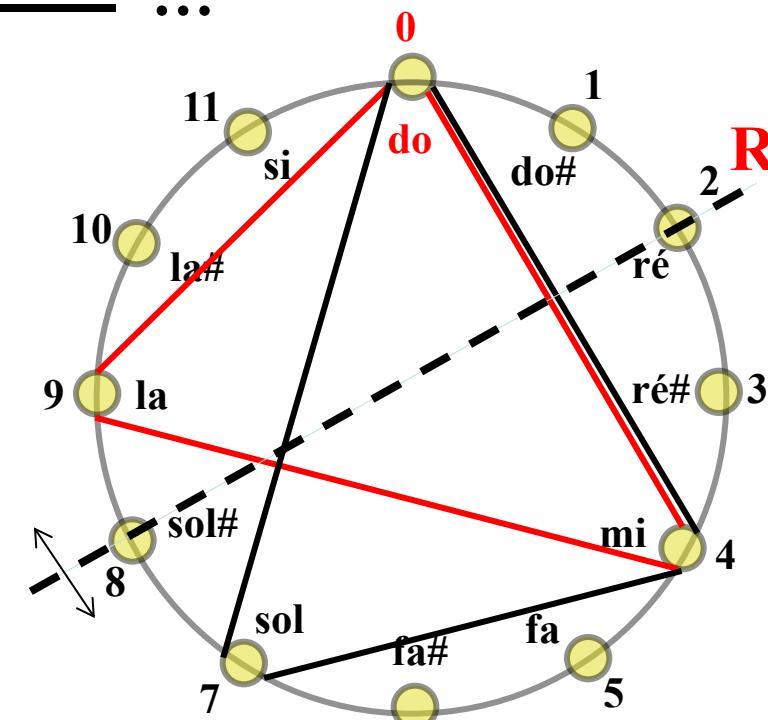
...  ...

R comme relatif

Do maj = {0,4,7}
La min = {0,4,9}

...  ...

...  ...

...  ...

Les inversions sont des symétries axiales

The diagram illustrates the concept of musical inversions as axial symmetries, specifically focusing on the Leading Tone (L).

Piano Keyboard: A horizontal piano keyboard is shown with a blue box highlighting a segment of keys. Dashed arrows point from this segment to a 12-tone circle below and to a hand position diagram.

12-Tone Circle: A circle divided into 12 equal segments, numbered 0 through 11 clockwise. The segments are color-coded: 0 (red), 1, 2, 3, 4, 5 (dark grey), 6, 7, 8, 9, 10, 11 (yellow). Below the circle, musical notes are labeled: do, do#, ré, ré#, mi, fa, fa#, sol, sol#, la, la#, si, do. Arrows point from the numbers 0-11 to the corresponding segments on the circle. A blue arrow points from the piano keyboard segment to the circle. A blue line labeled "L = Leading Tone" connects the 0 position to the 11 position. A vertical dashed line passes through the 6 position.

Hand Position: Two hands are shown in a playing position, with dashed arrows pointing from their positions to the 6 and 11 positions on the 12-tone circle.

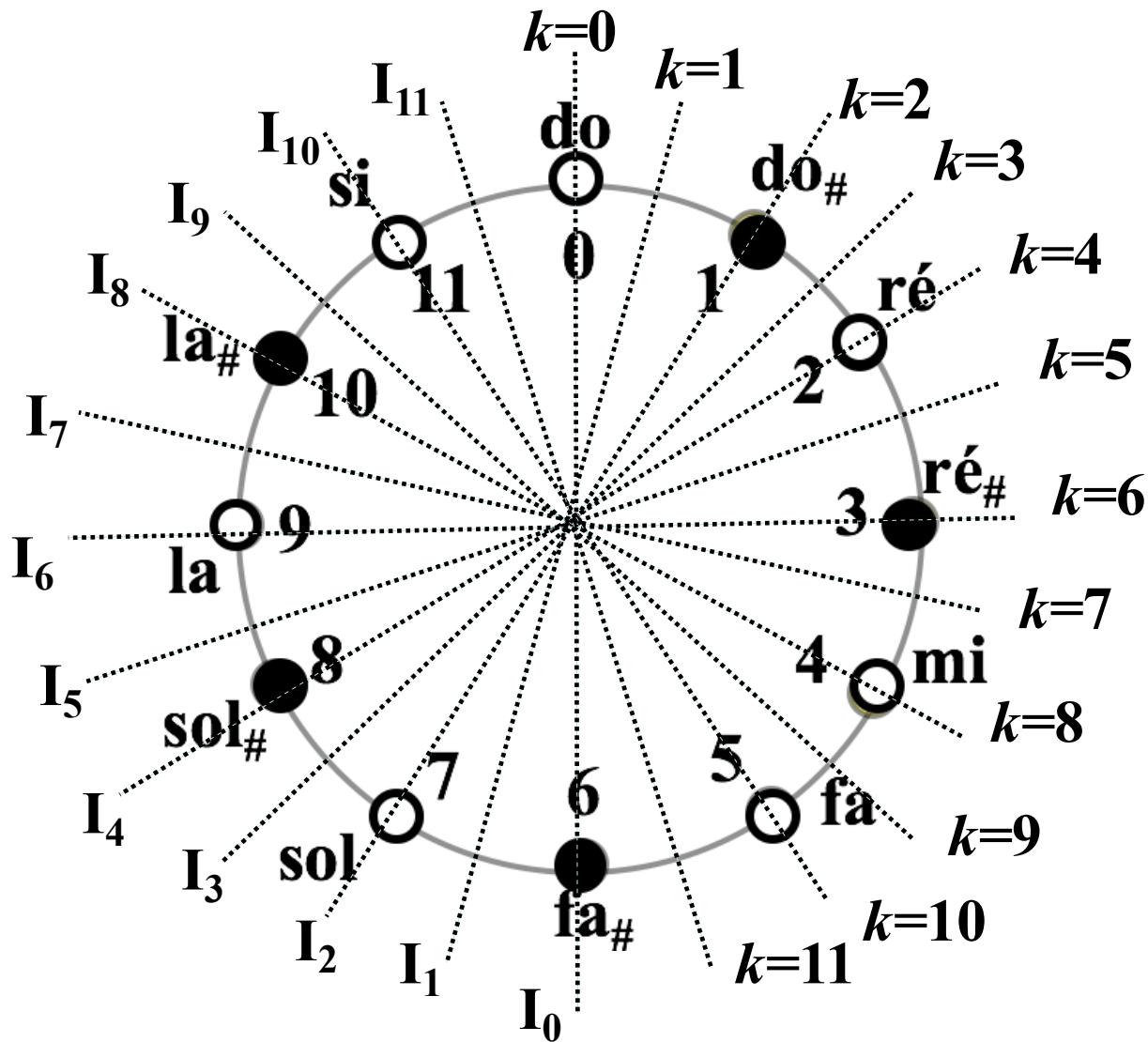
Text Boxes:

- Do maj** = {0,4,7}
- Mi min** = {4,7,11}

Circle Labels: The circle contains labels for musical notes: do, do#, ré, ré#, mi, fa, fa#, sol, sol#, la, la#, si, and do. The number 0 is also present.

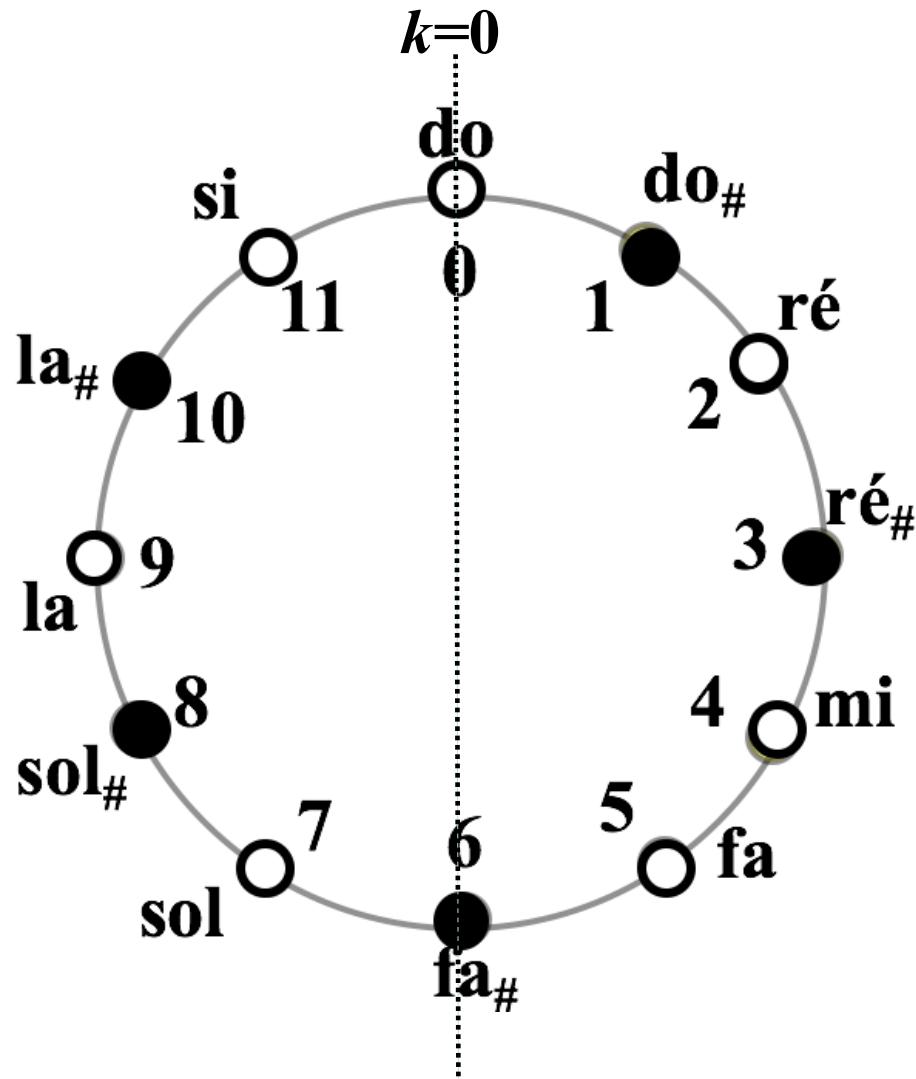
Les inversions sont des symétries axiales généralisées

$$x \xrightarrow{I_k} k \cdot x \text{ modulo } 12$$



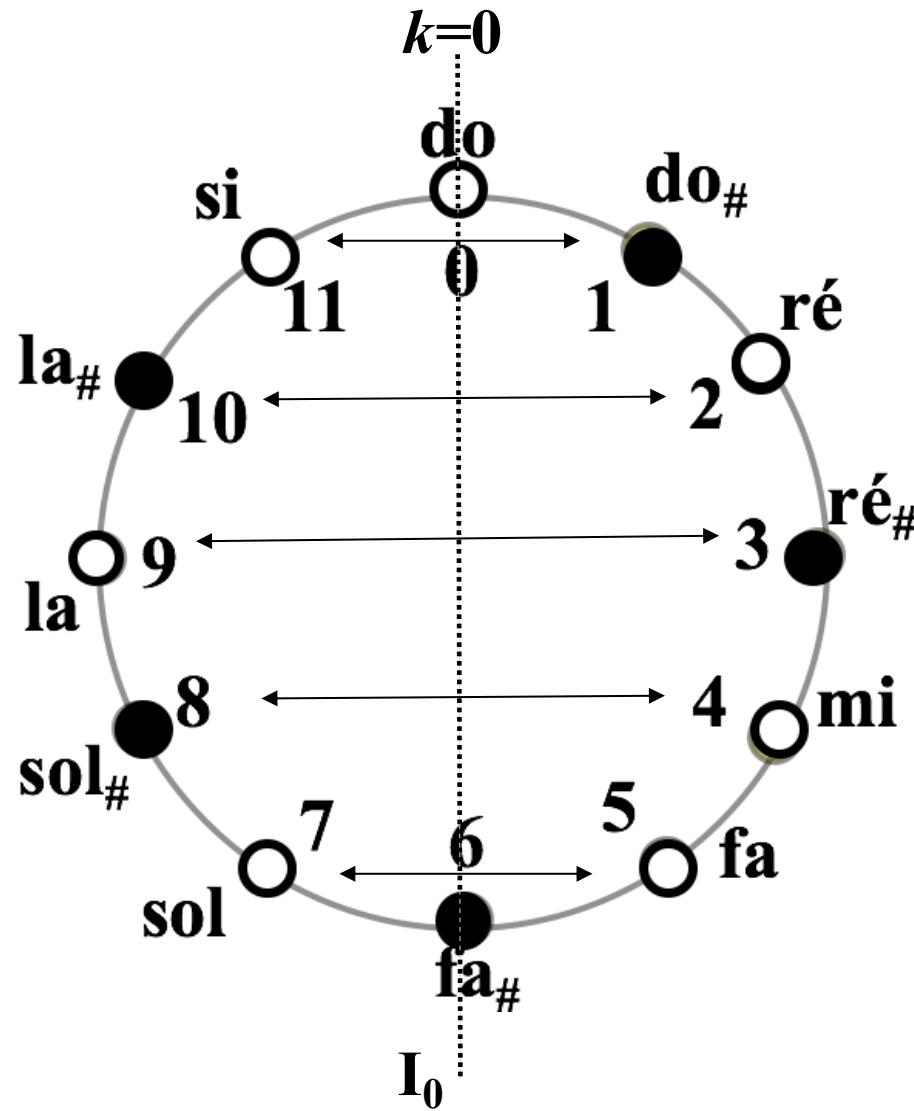
Quelques exemples

$$x \xrightarrow{I_0} -x \text{ modulo } 12$$



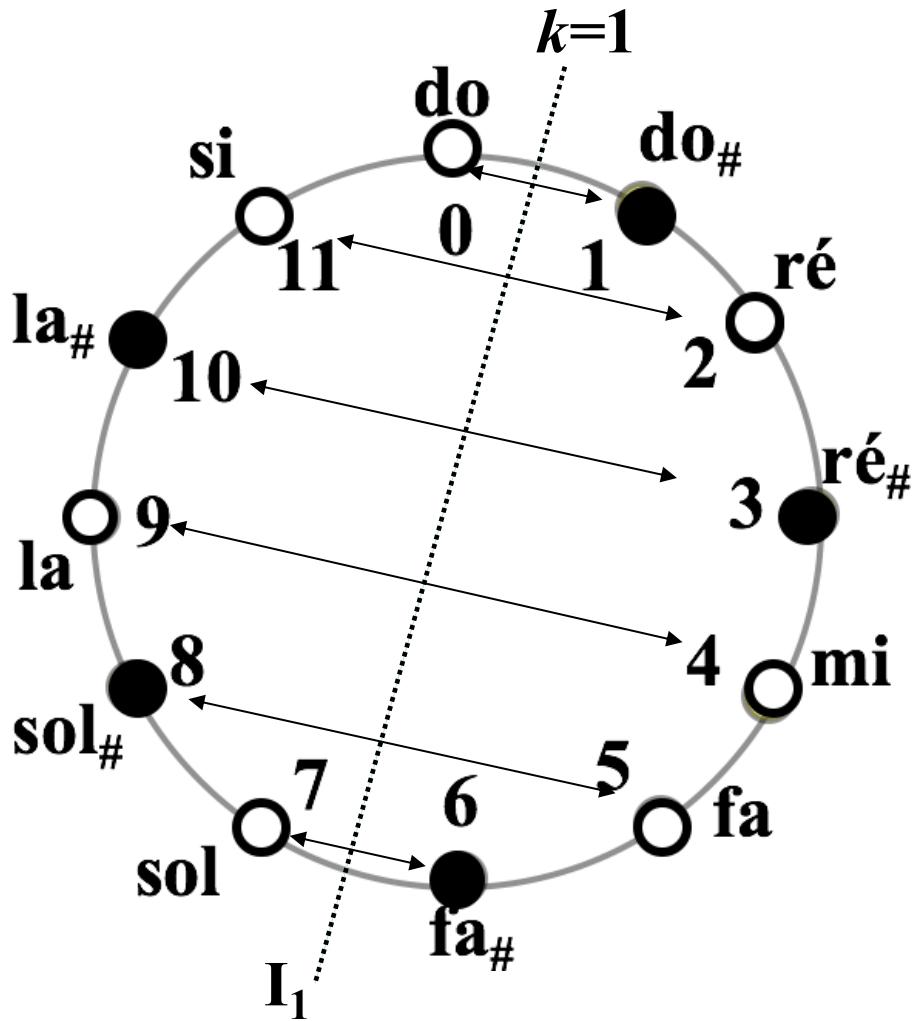
Quelques exemples

$$x \xrightarrow{I_0} -x \text{ modulo } 12$$

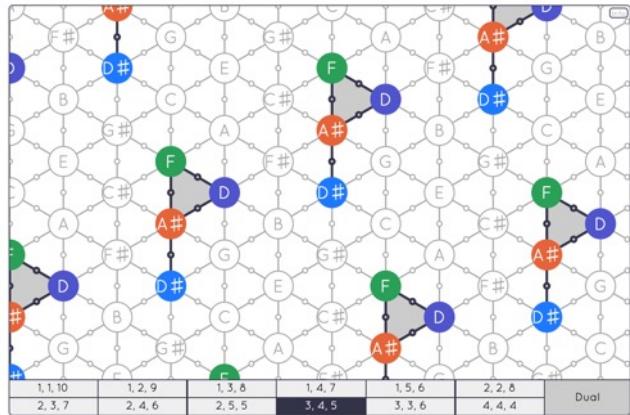


Les inversions sont des symétries axiales généralisées

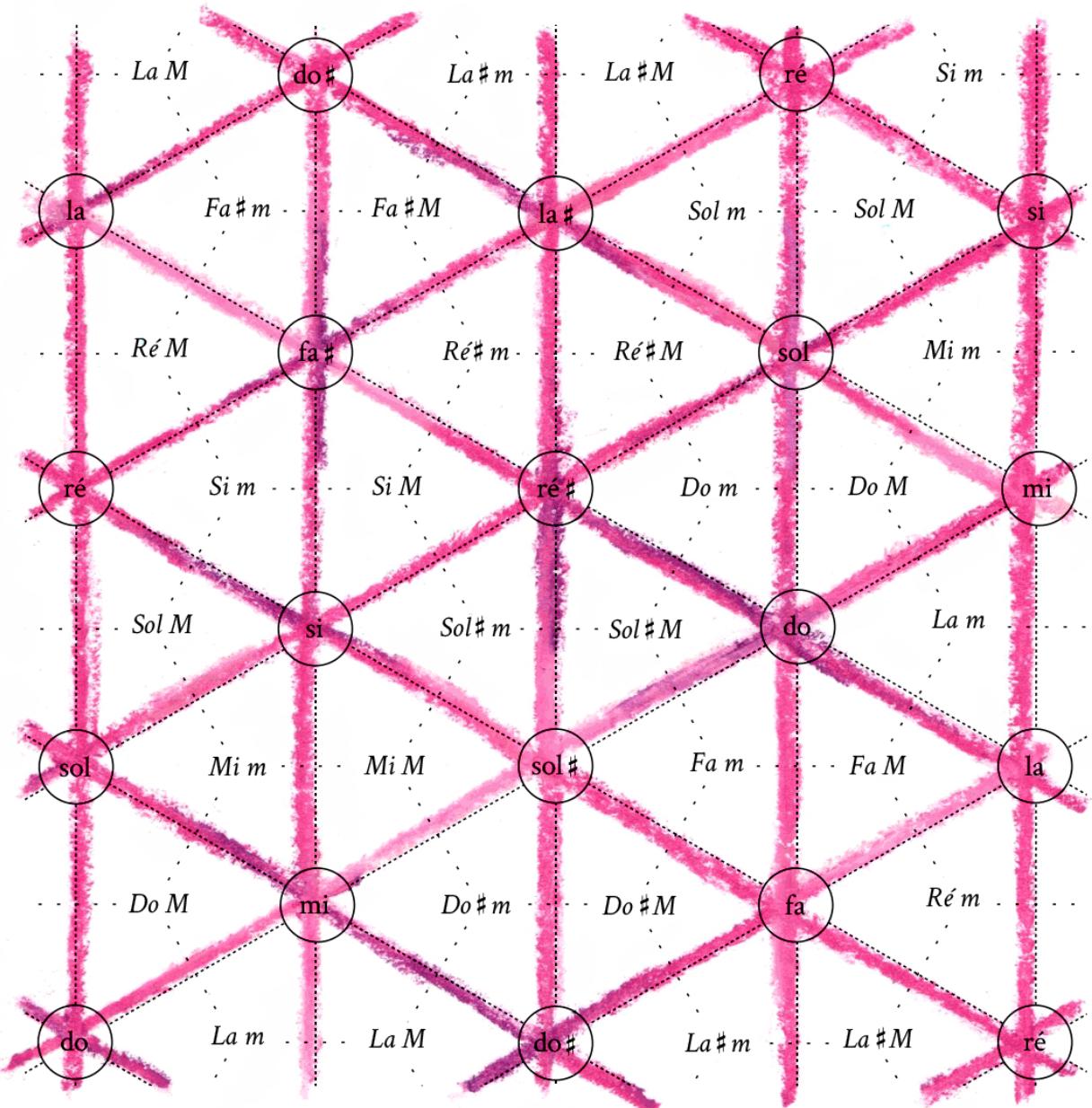
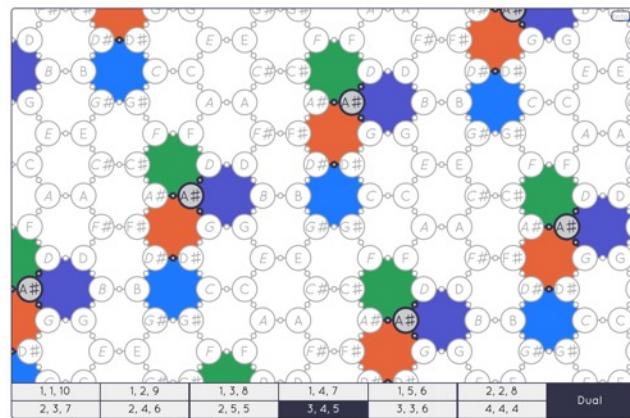
$$x \xrightarrow{I_1} 1-x \text{ modulo } 12$$



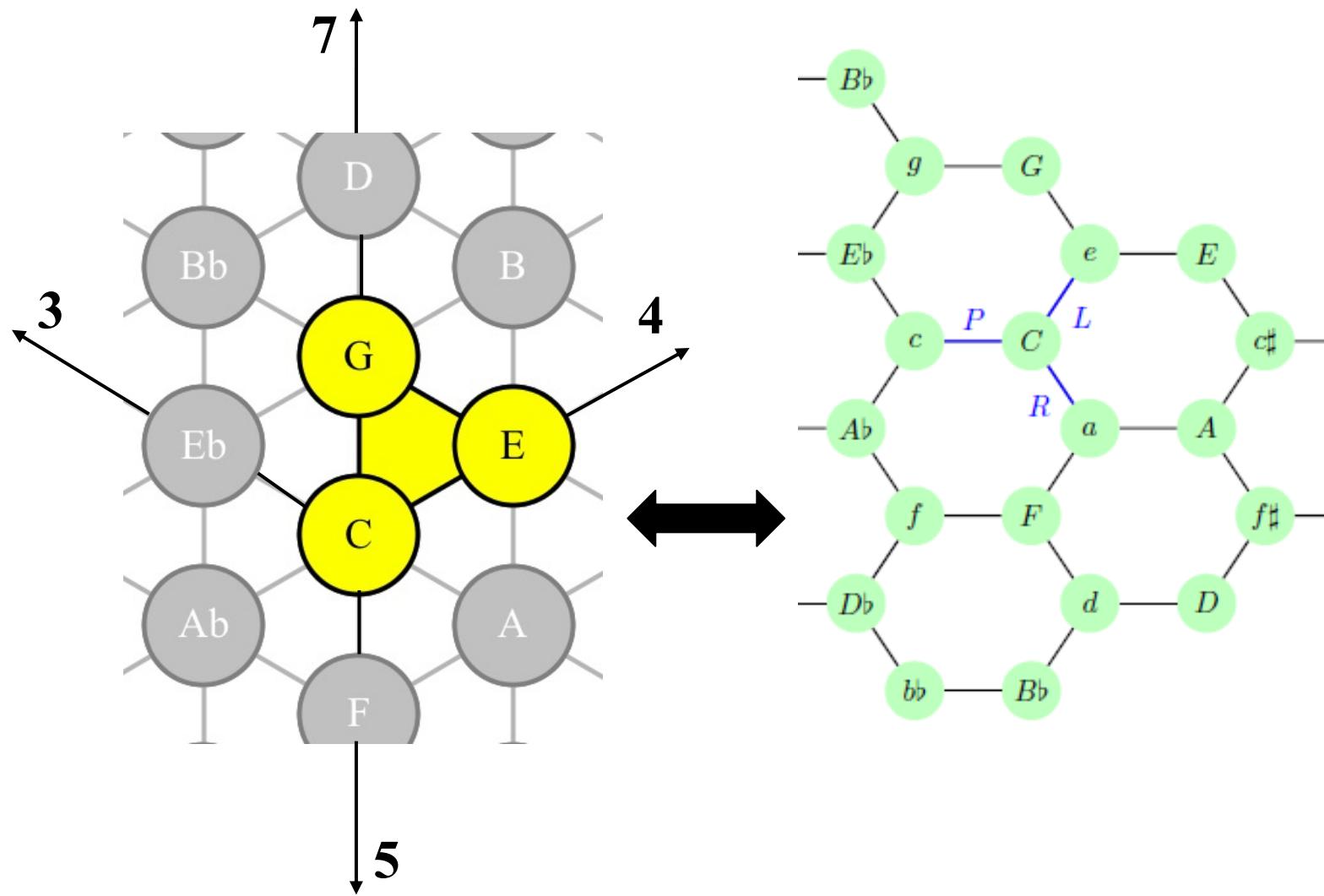
Du Tonnetz à l'espace dual



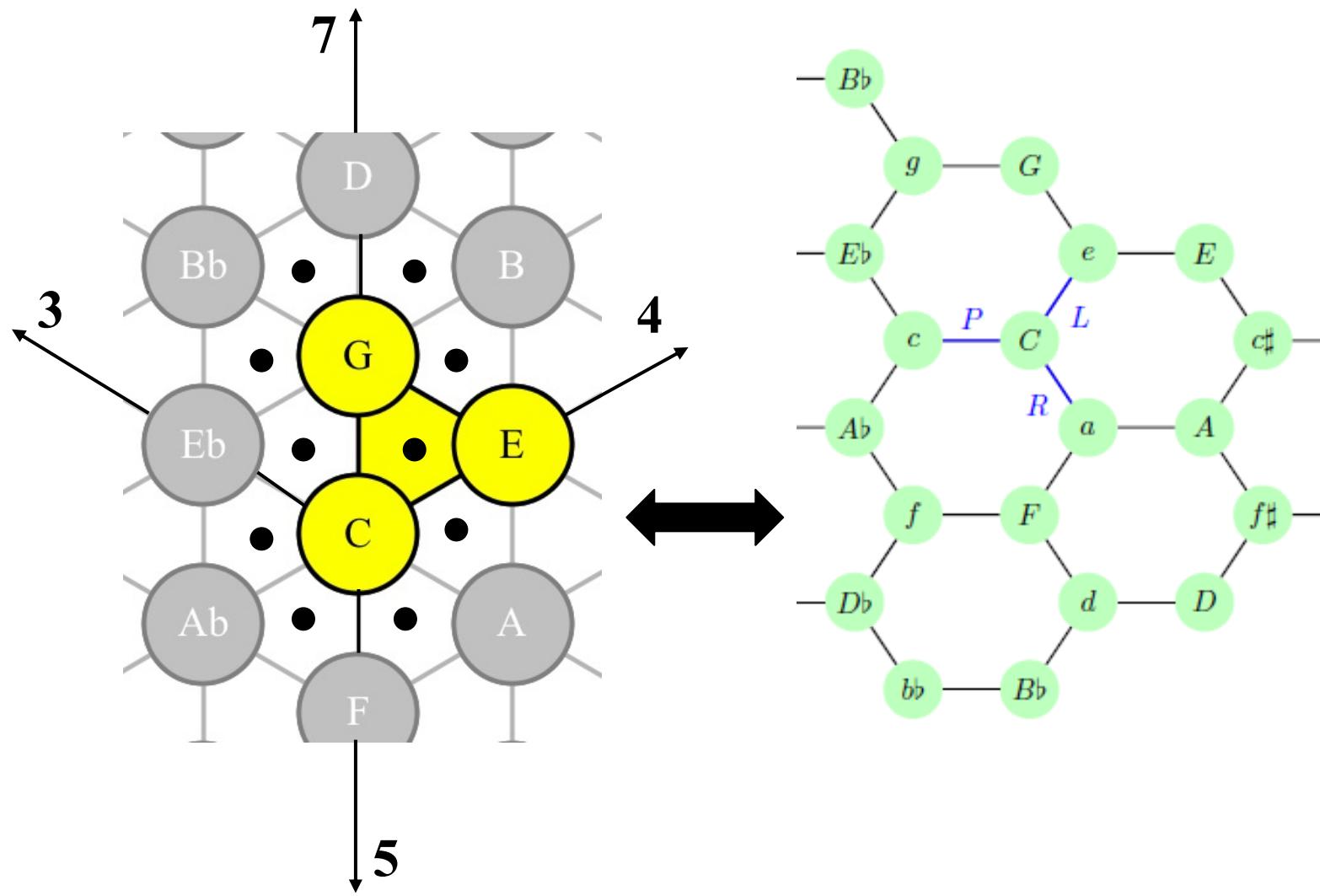
duality



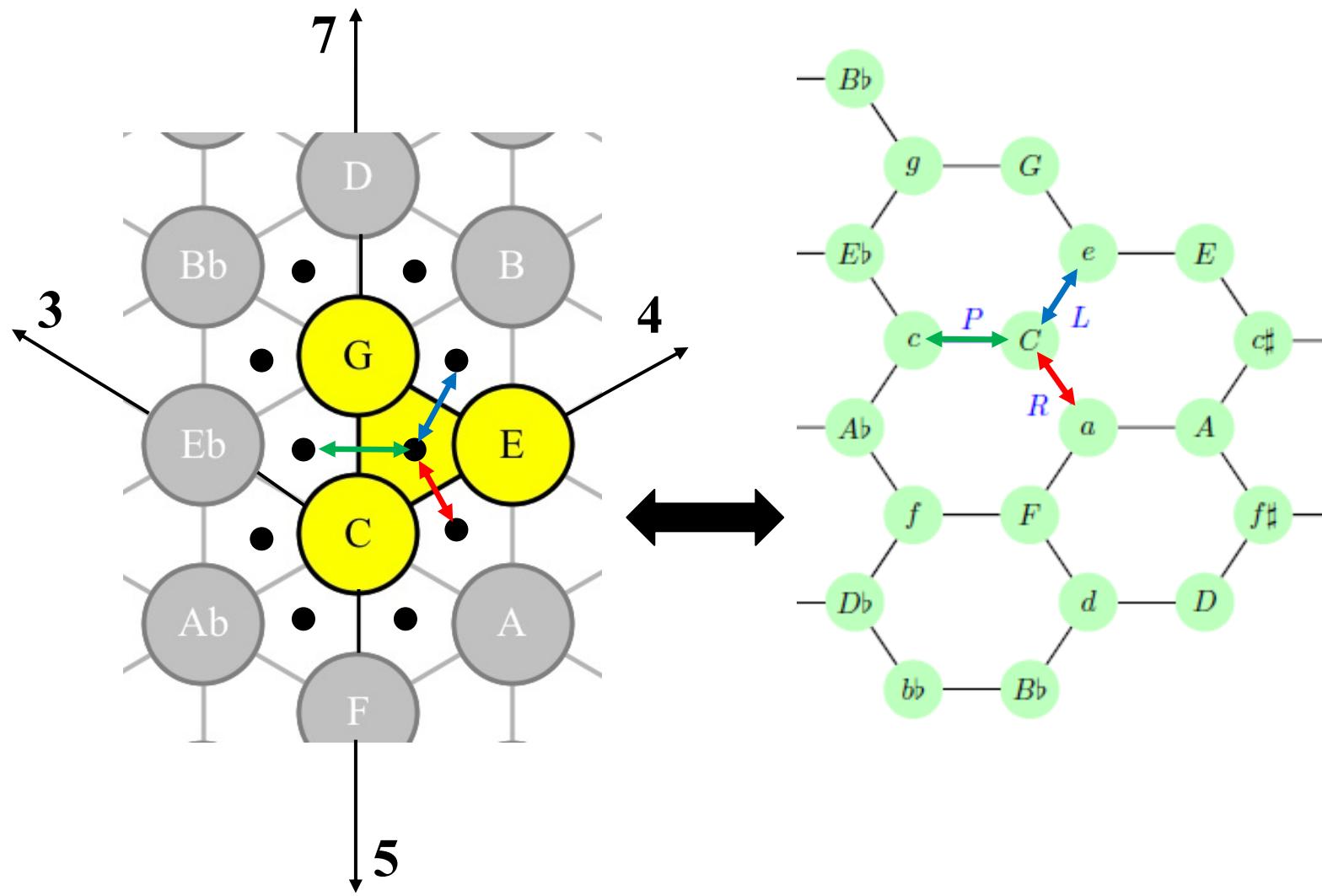
Construction du maillage hexagonal à partir du Tonnetz



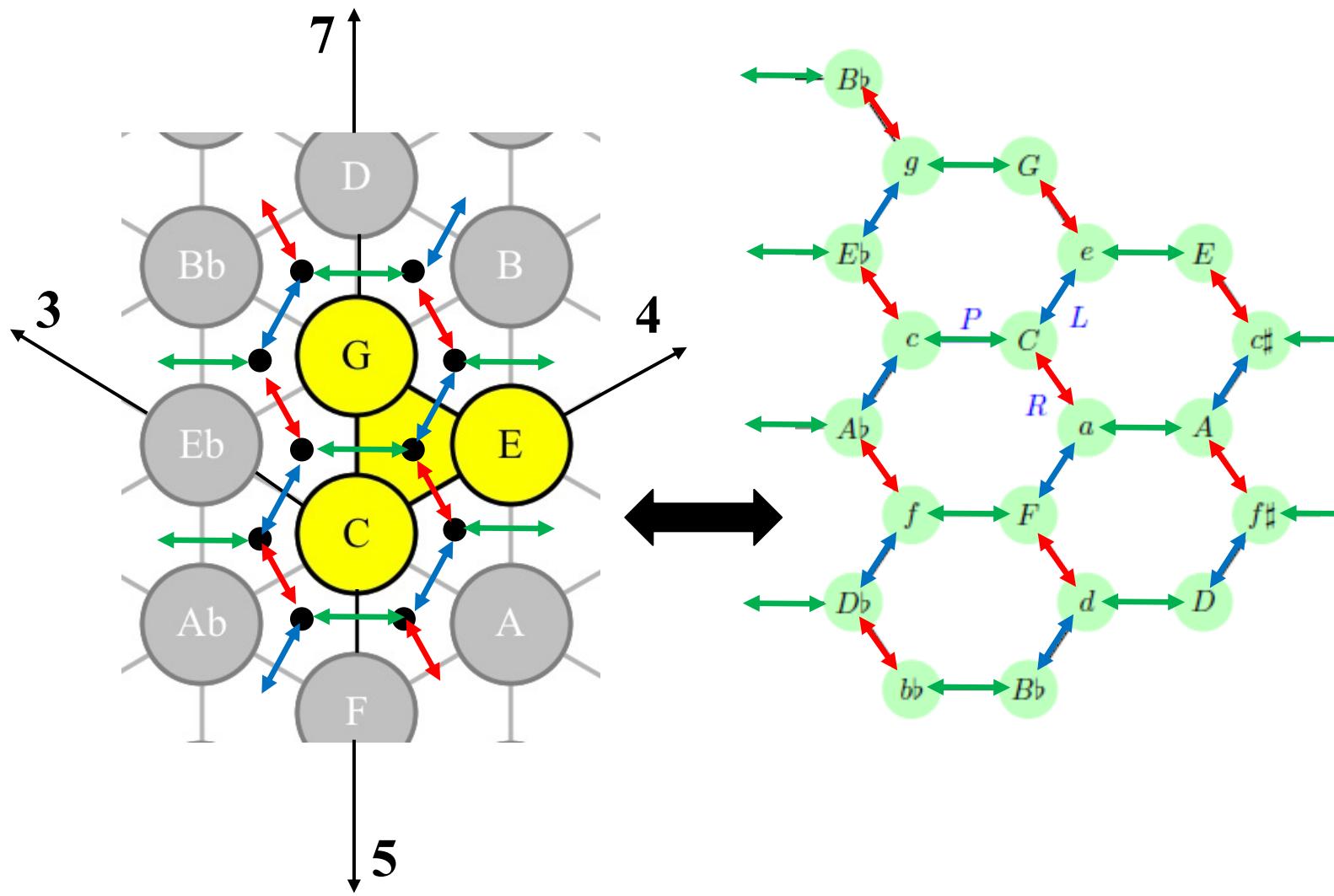
Construction du maillage hexagonal à partir du Tonnetz



Construction du maillage hexagonal à partir du Tonnetz



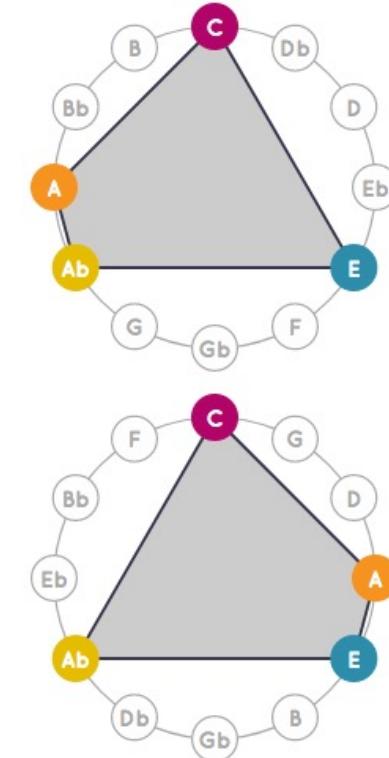
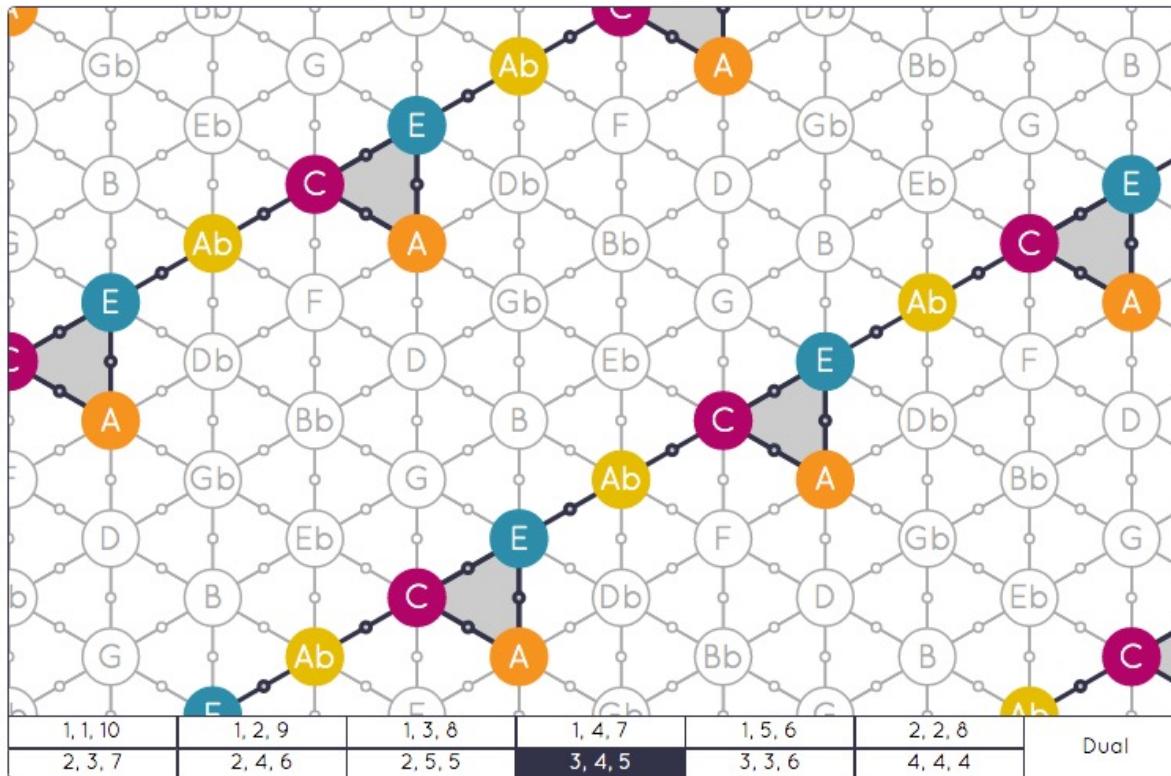
Construction du maillage hexagonal à partir du Tonnetz



Modèles computationnels : The Tonnetz

THE TONNETZ

ONE KEY – MANY REPRESENTATIONS



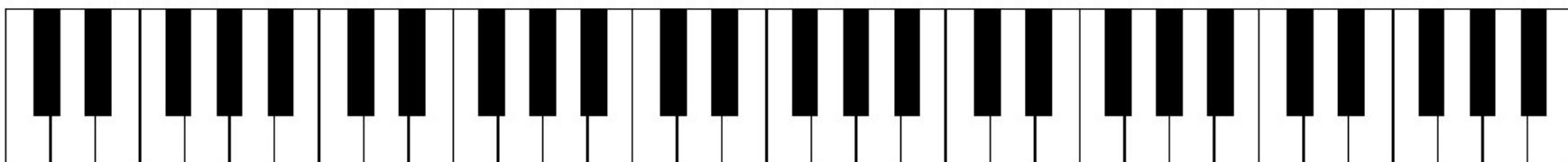
Load Midi File

Play

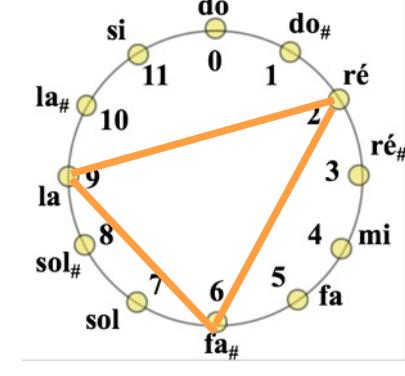
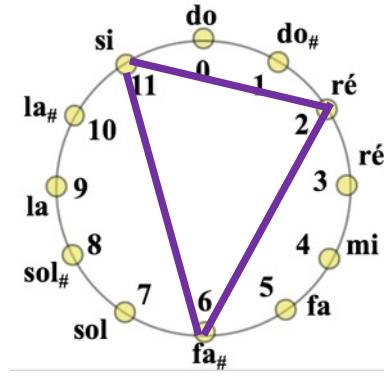
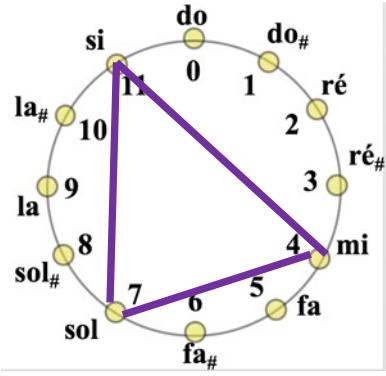
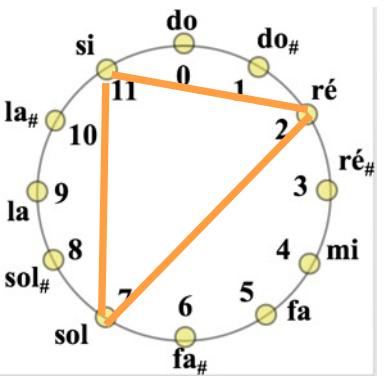
Start Recording

Rotate 180°

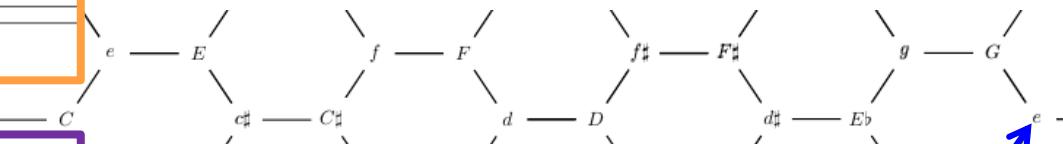
Translate



Quelques exemples analytiques : une Anatole...



G

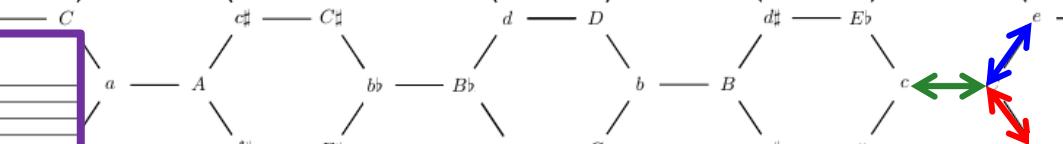


iii → V → I → vi

V → I → vi → iii

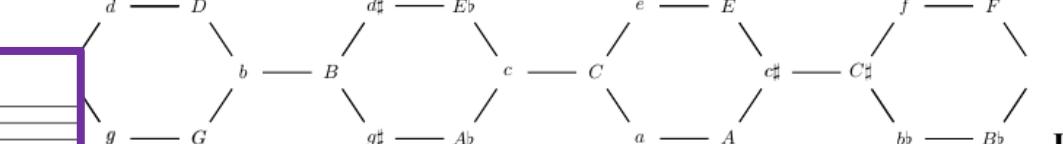
I → vi → iii → V

Em

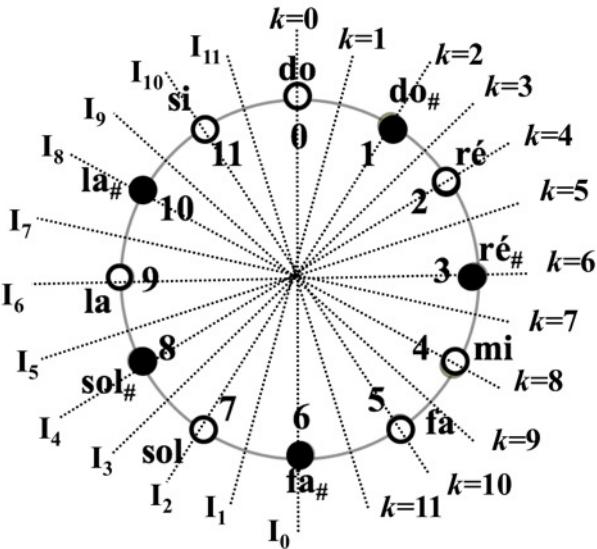
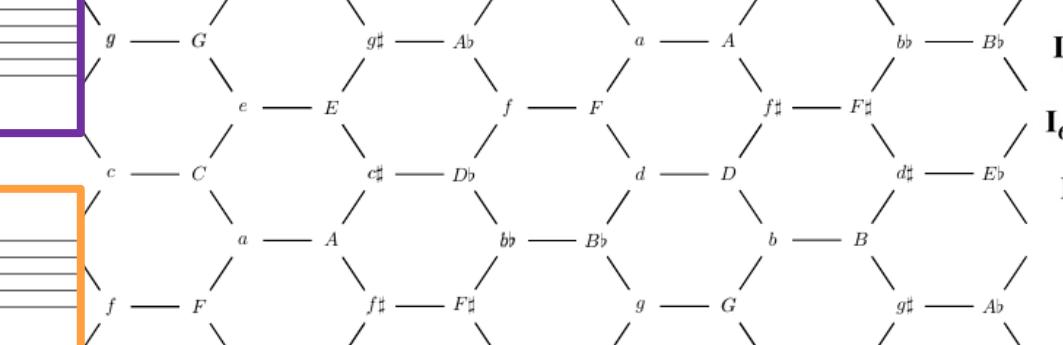


vi → iii → V → I

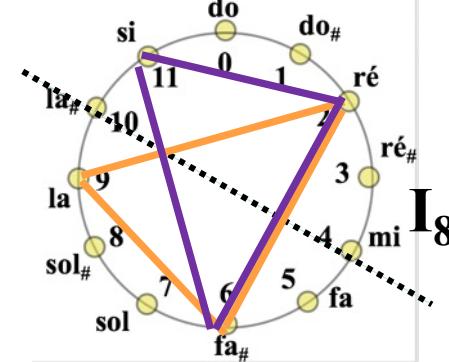
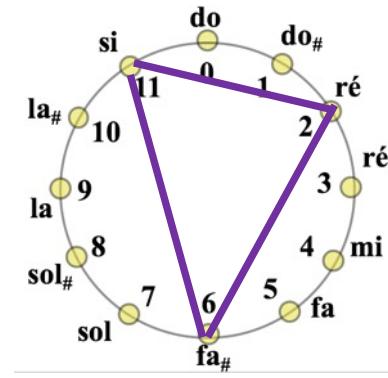
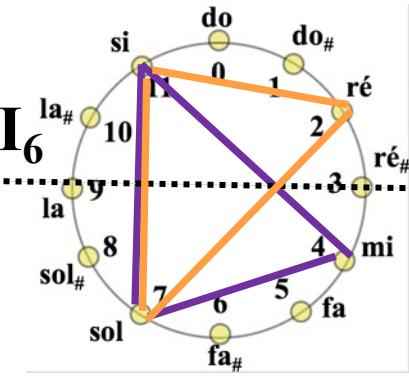
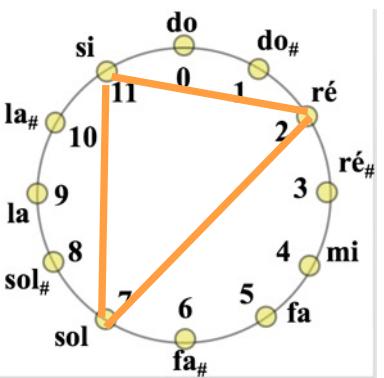
Bm



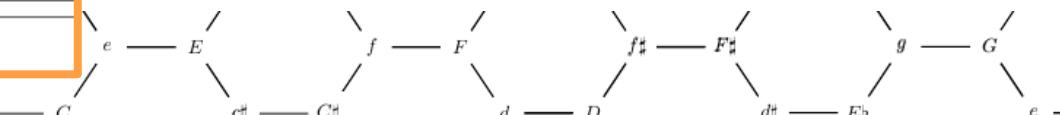
D



Quelques exemples analytiques : une Anatole...



G

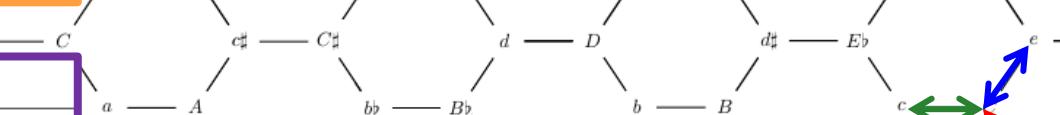


iii → V → I → vi

V → I → vi → iii

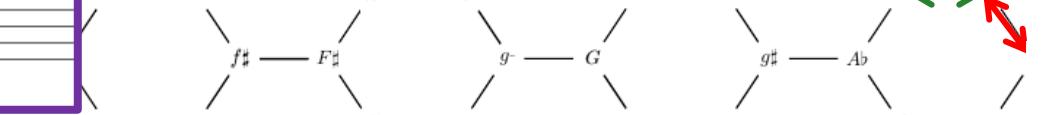
I → vi → iii → V

Em

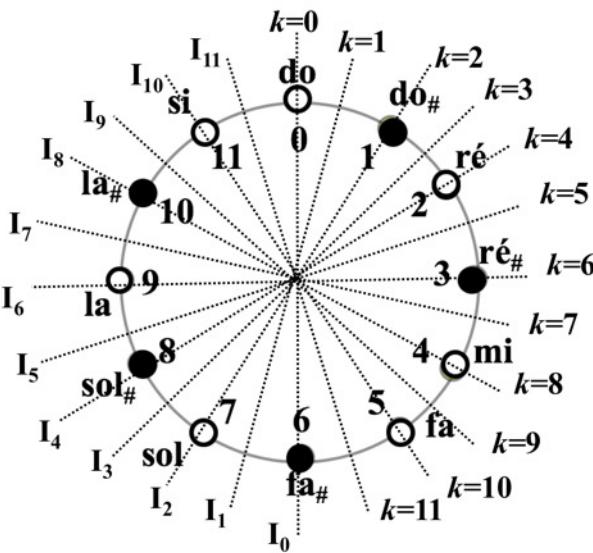
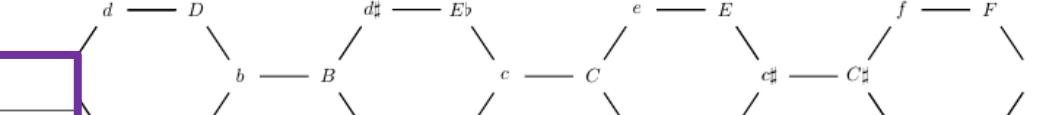


vi → iii → V → I

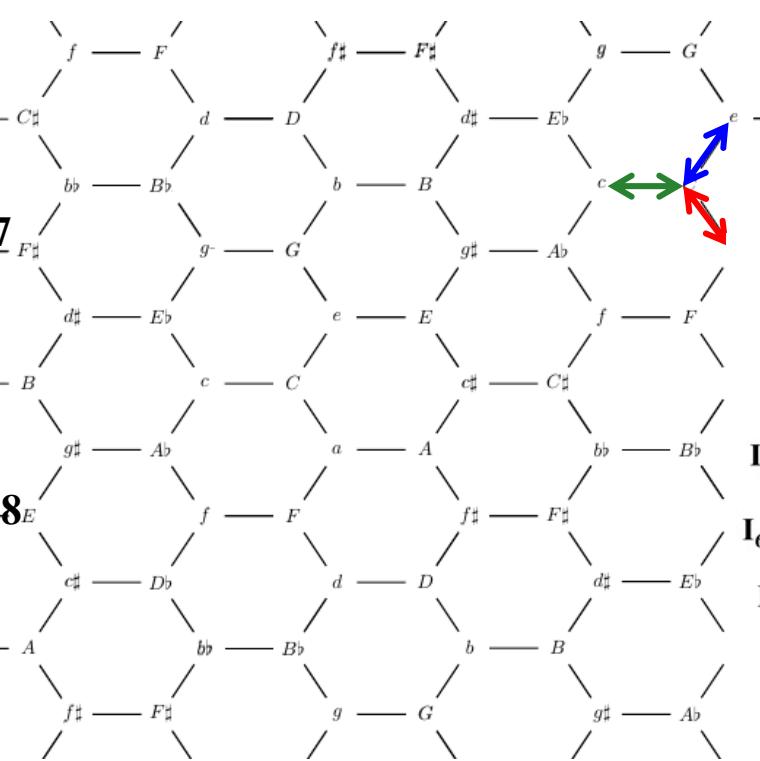
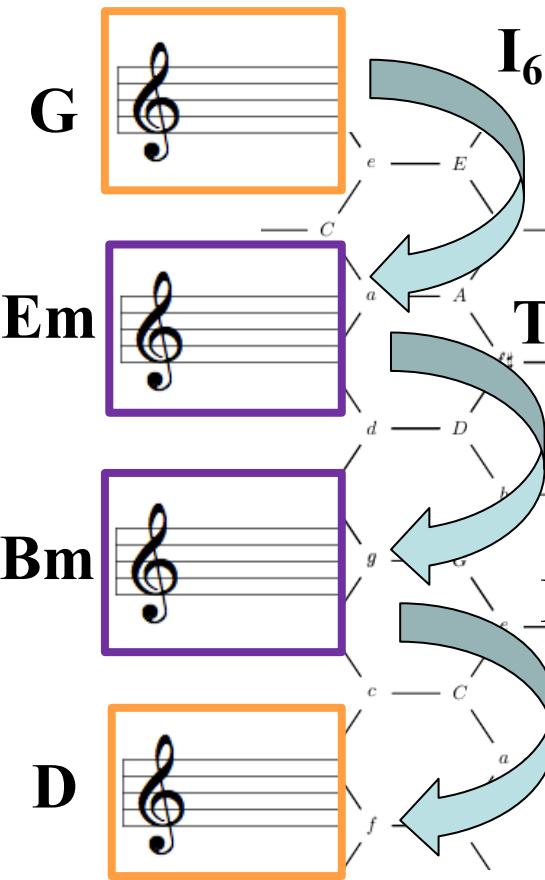
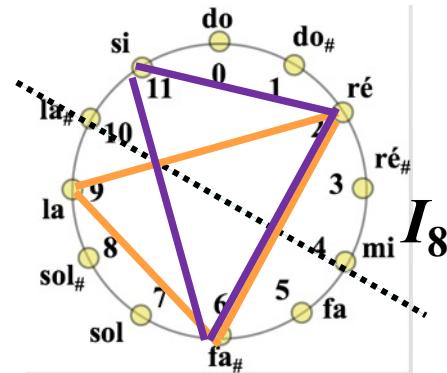
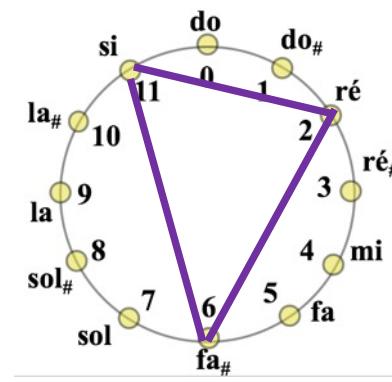
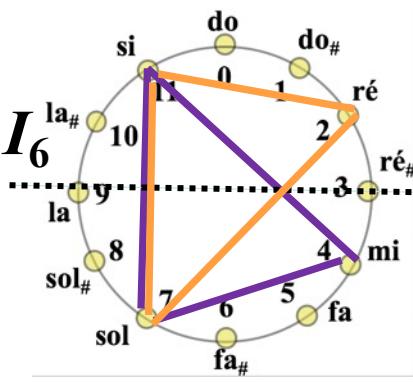
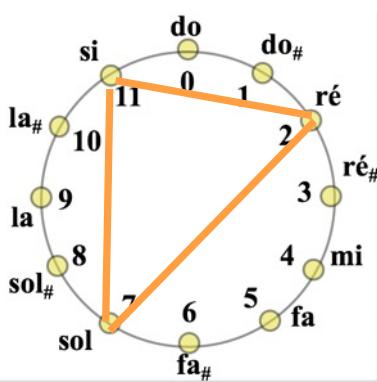
Bm



D



Quelques exemples analytiques : une Anatole...

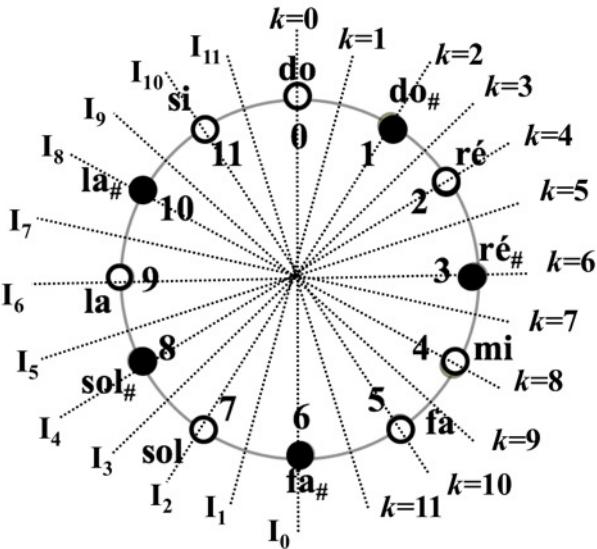


iii → V → I → vi

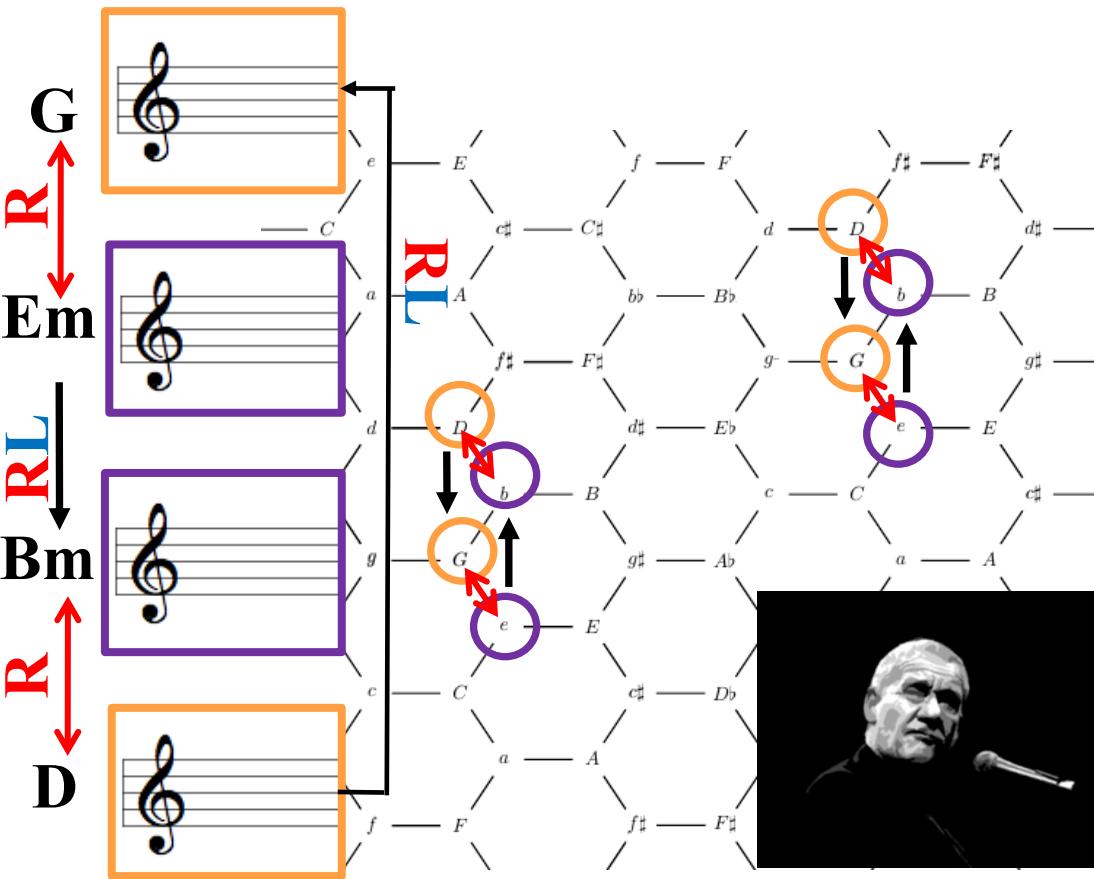
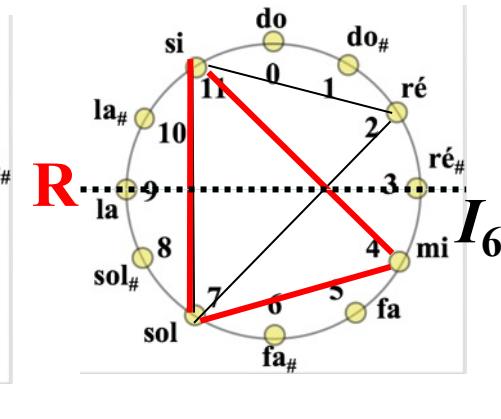
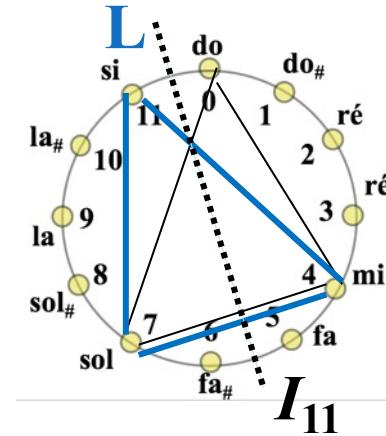
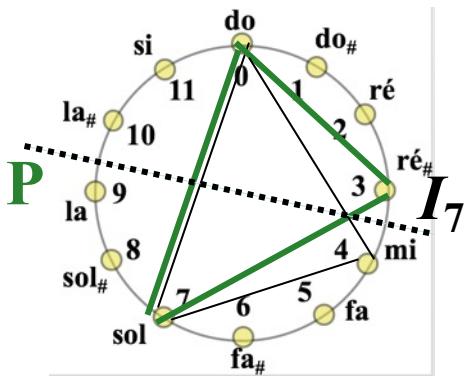
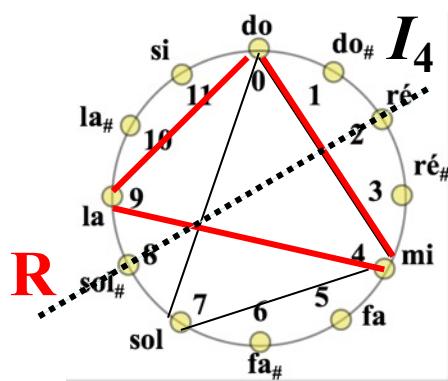
V → I → vi → iii

I → vi → iii → V

vi → iii → V → I

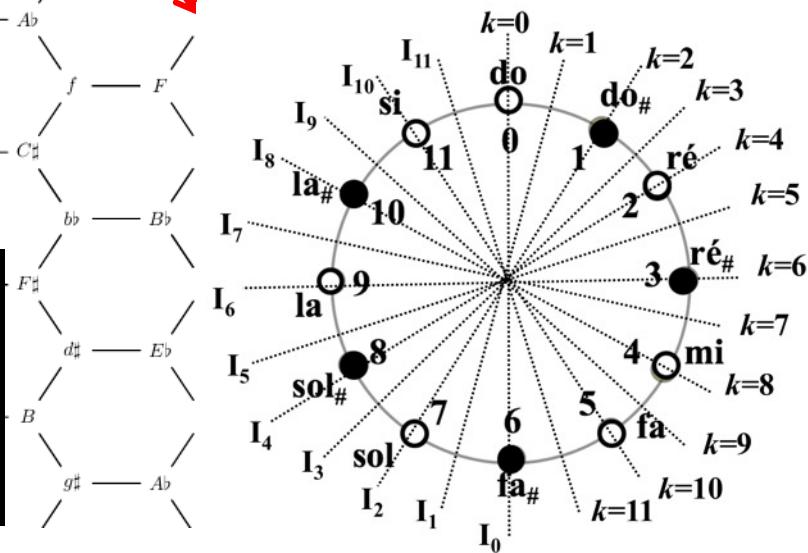


Quelques exemples analytiques : ...chez Paolo Conte



iii → V → I → vi
V → I → vi → iii
I → vi → iii → V

vi → iii → V → I



La trajectoire spatiale de l'Anatole

Harmonic Progressions

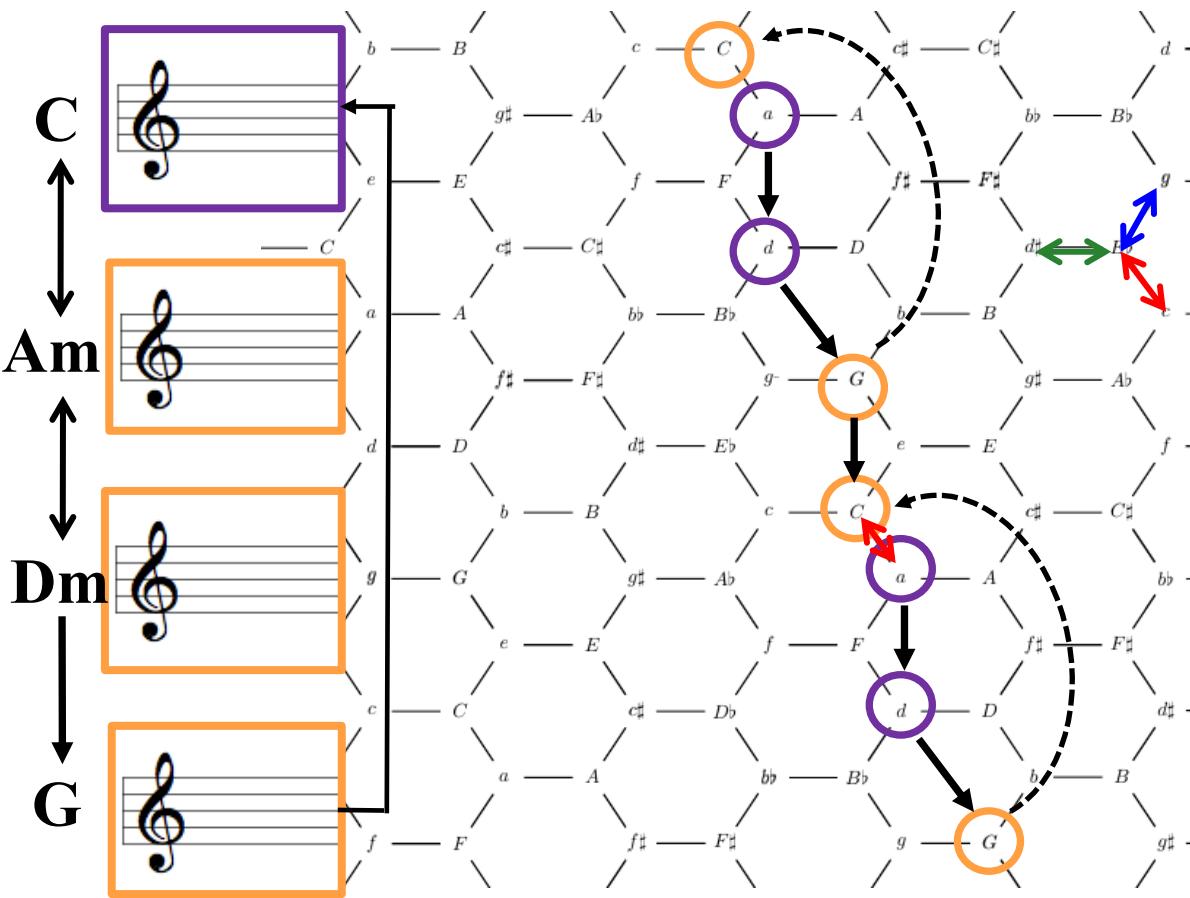
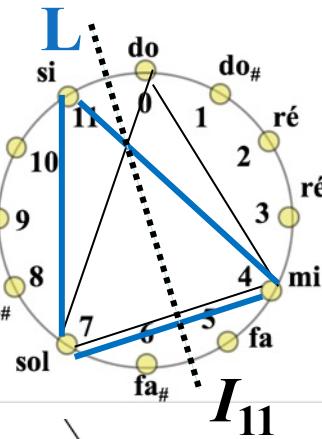
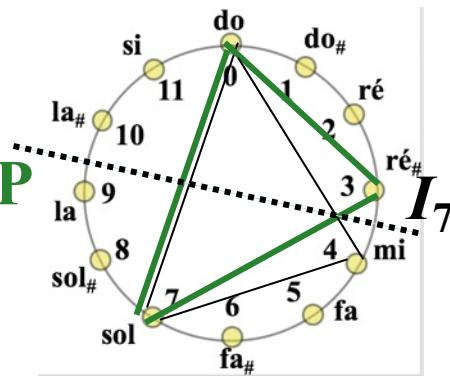
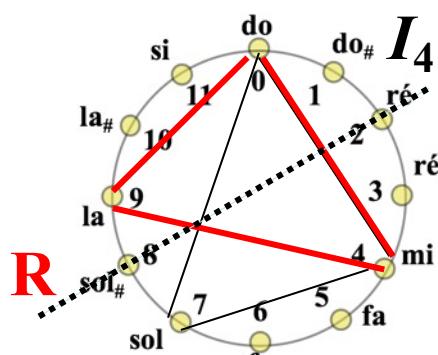
In Paolo Conte

Sotto le Stelle del Jazz



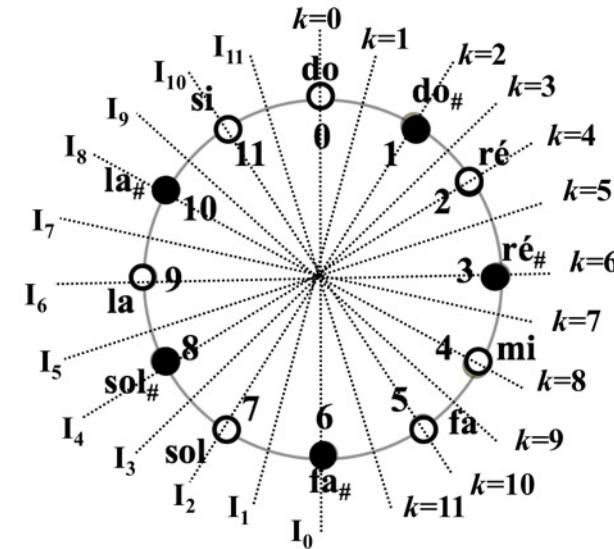
*Supervision Moreno Andreatta
Modélisation Gilles Baroin 2016*

Autres Anatoles et autres trajectoires

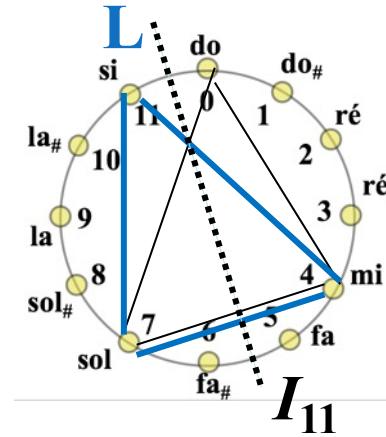
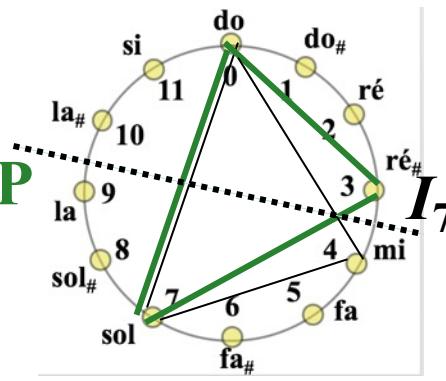
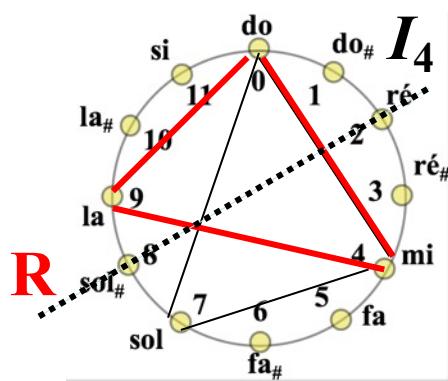


$\text{ii} \rightarrow \text{V} \rightarrow \text{I} \rightarrow \text{vi}$
 $\text{V} \rightarrow \text{I} \rightarrow \text{vi} \rightarrow \text{ii}$
I \rightarrow vi \rightarrow ii \rightarrow V

vi \rightarrow ii \rightarrow V \rightarrow I



Boucles harmoniques dans la pop

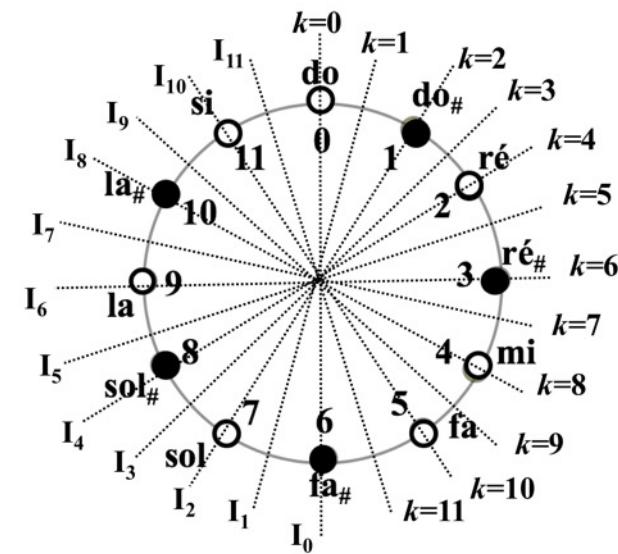
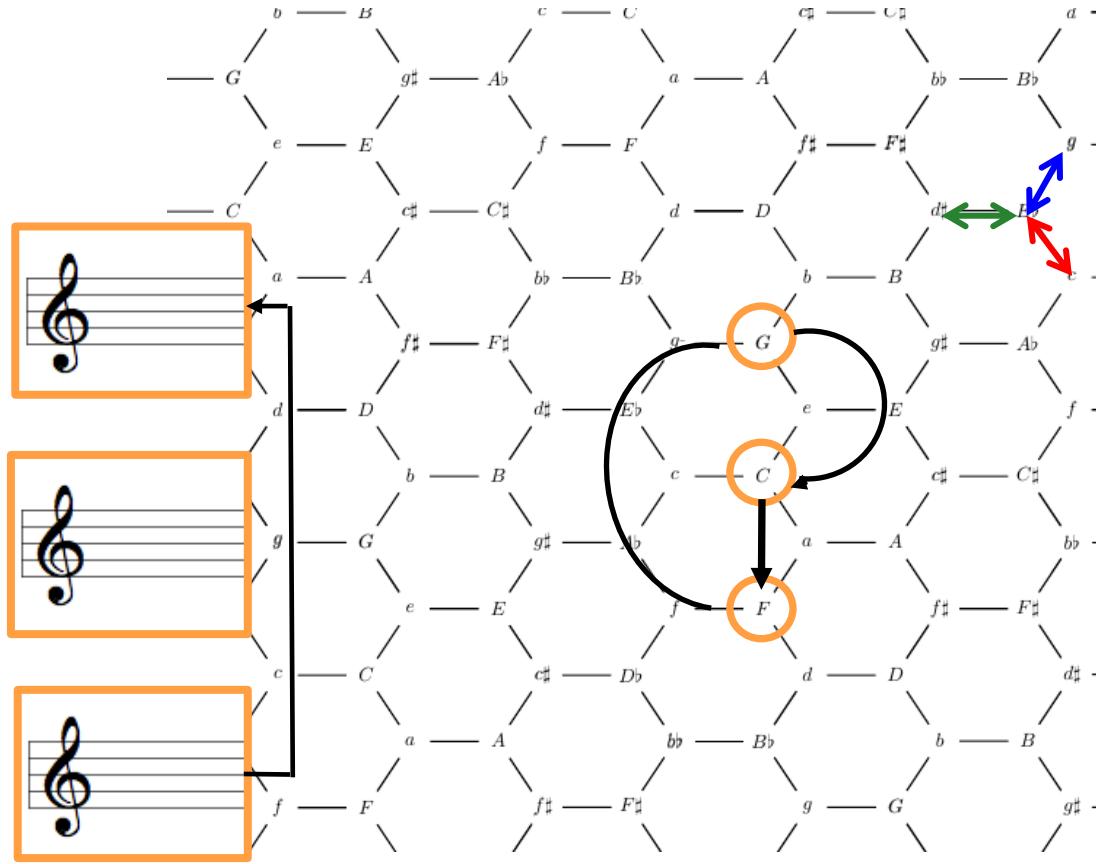


I → IV → V

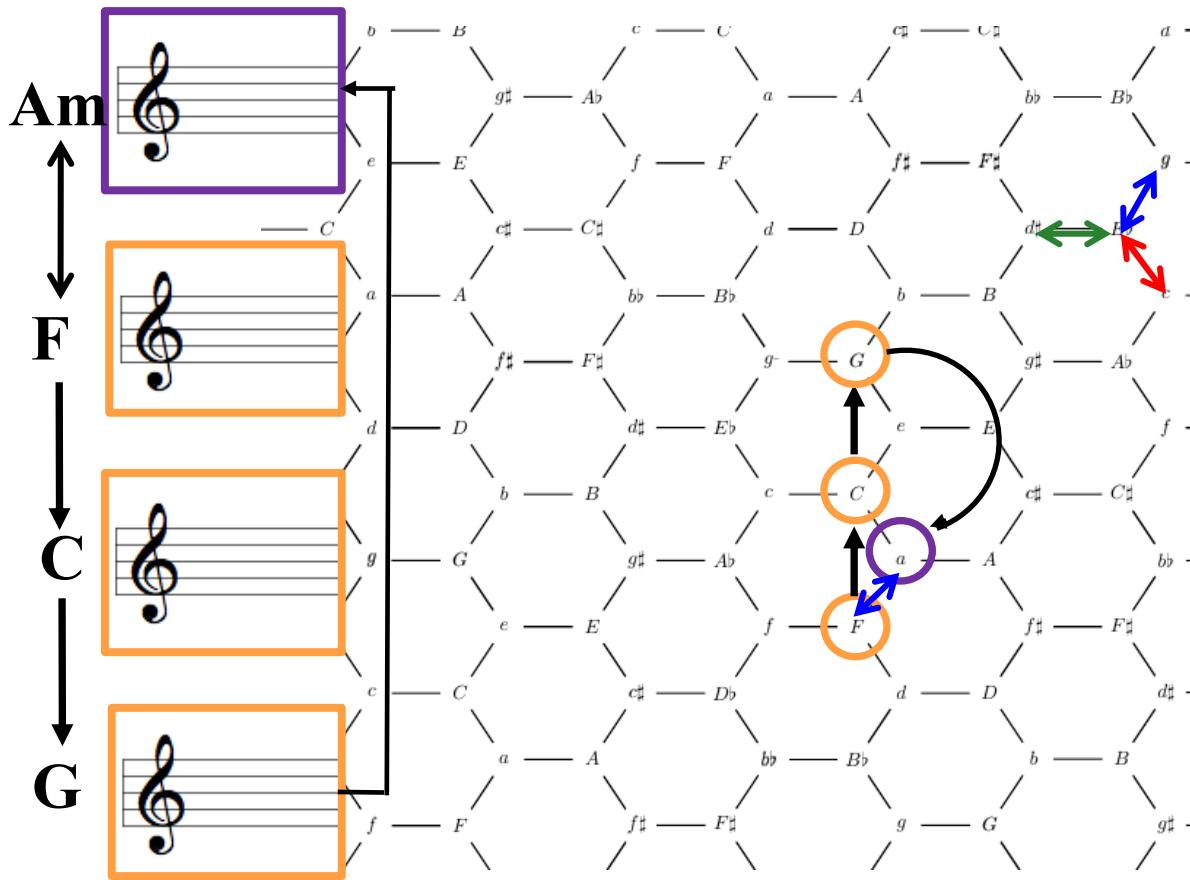
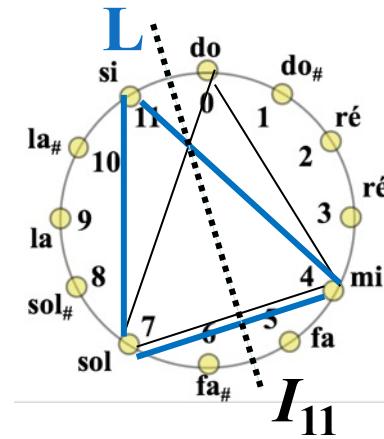
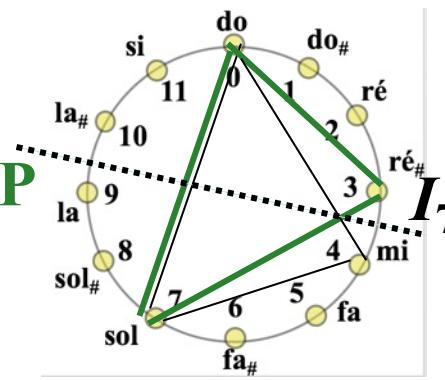
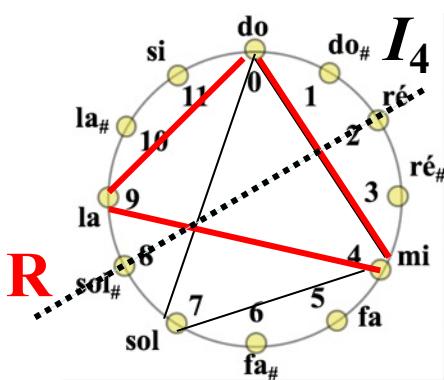
IV → V → I

V → I → IV

C
↓
F
↓
G



Boucles harmoniques dans la pop

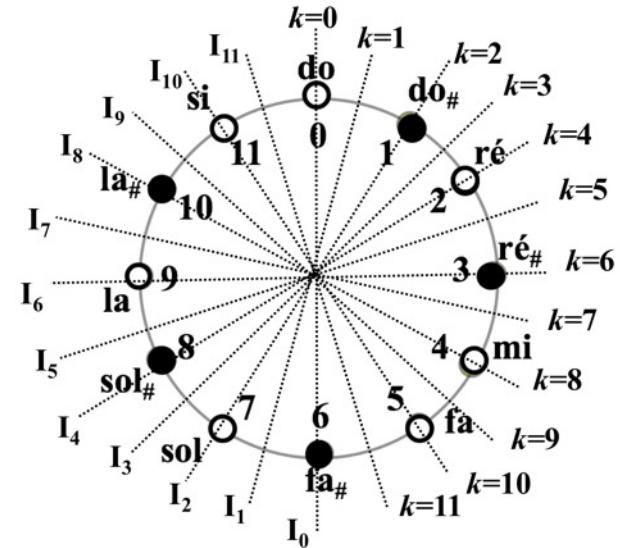


vi → IV → I → V

IV → I → V → vi

I → V → vi → IV

V → vi → IV → I



Mise en évidence des symétries dans la musica pop

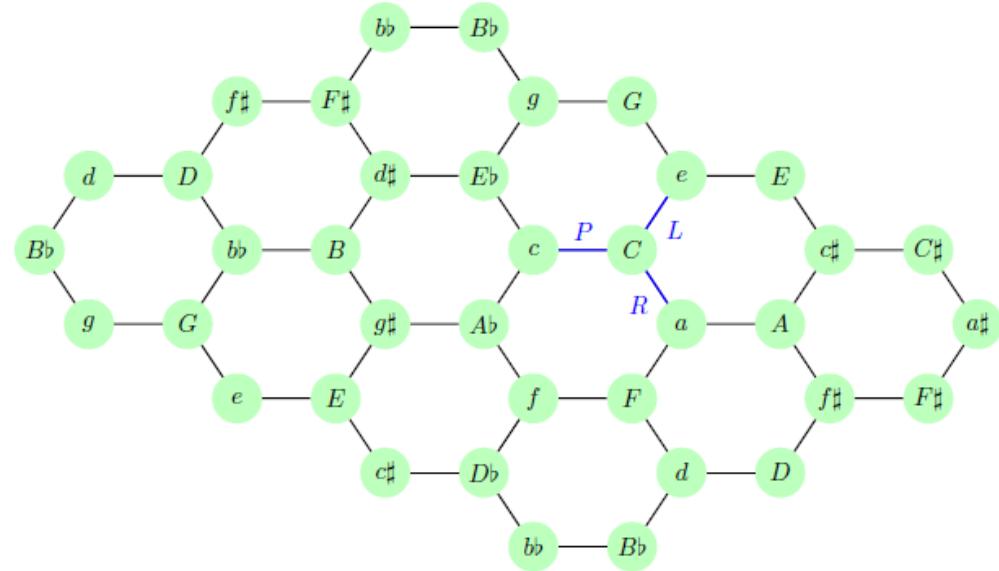
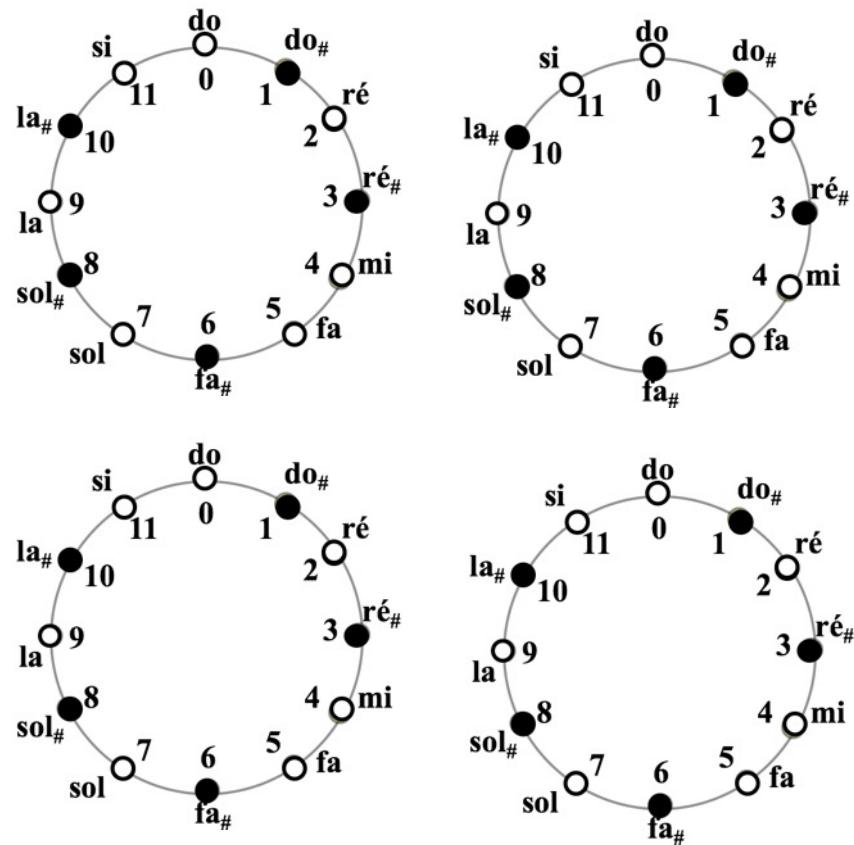
- Guy Capuzzo, "Neo-Riemannian Theory and the Analysis of Pop-Rock Music", *Music Theory Spectrum* 26(2), p. 177-199, 2004

Synthesizer

do do[#]

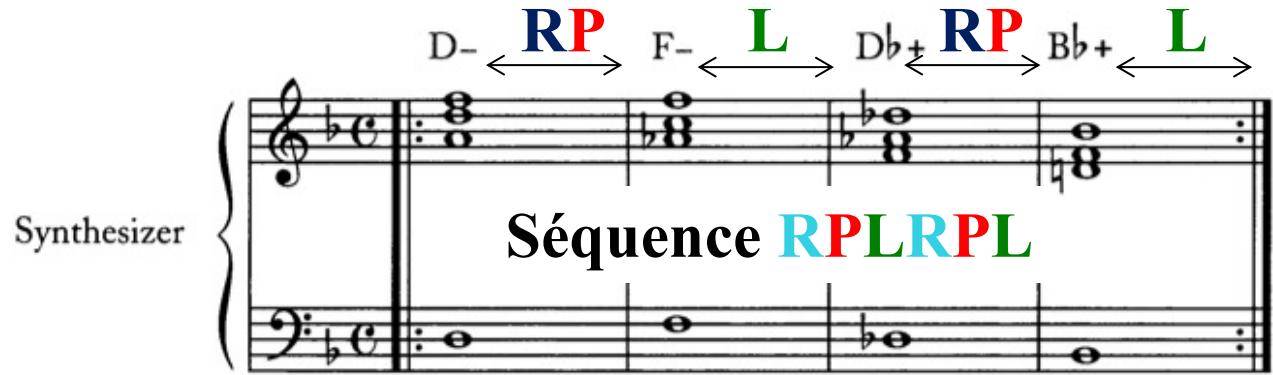
si si[#]

*Shake the disease - 1985
(Depeche Mode) – min. 2'17"*

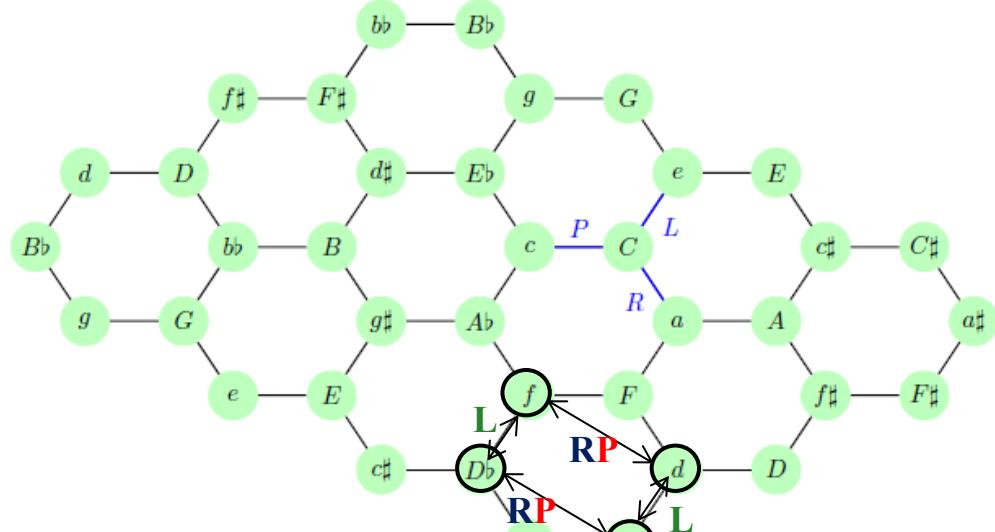
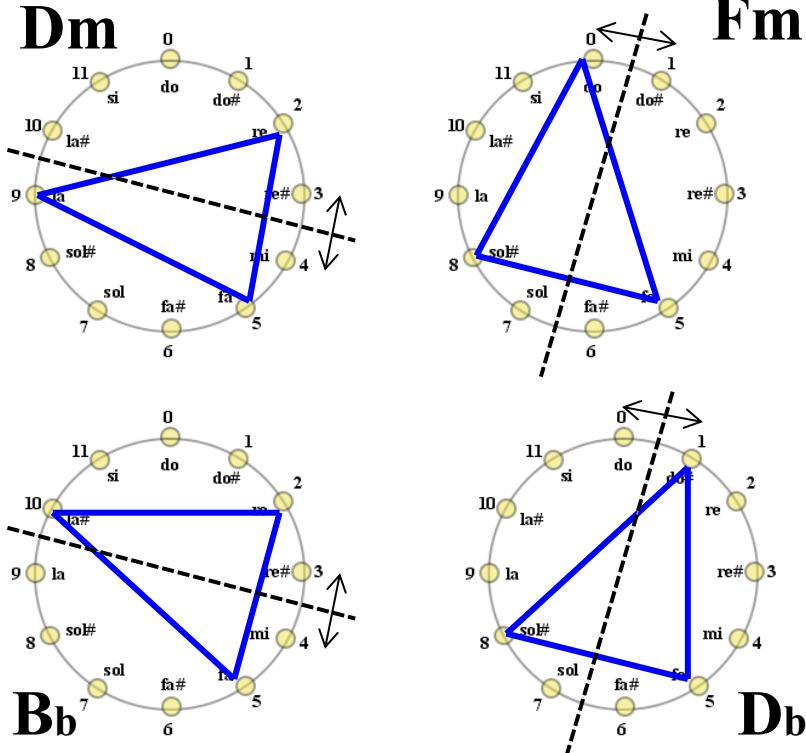


Mise en évidence des symétries dans la musica pop

- Guy Capuzzo, "Neo-Riemannian Theory and the Analysis of Pop-Rock Music", *Music Theory Spectrum* 26(2), p. 177-199, 2004

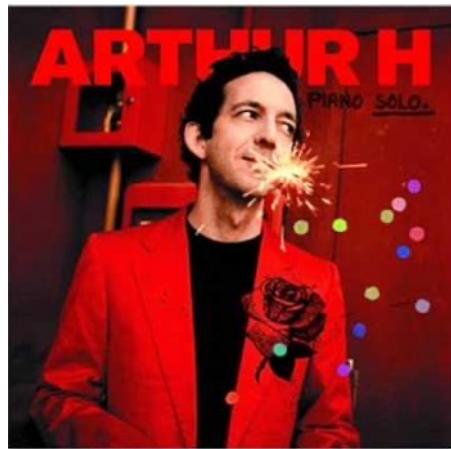


Shake the disease - 1985 Depeche Mode) – min. 2'17"

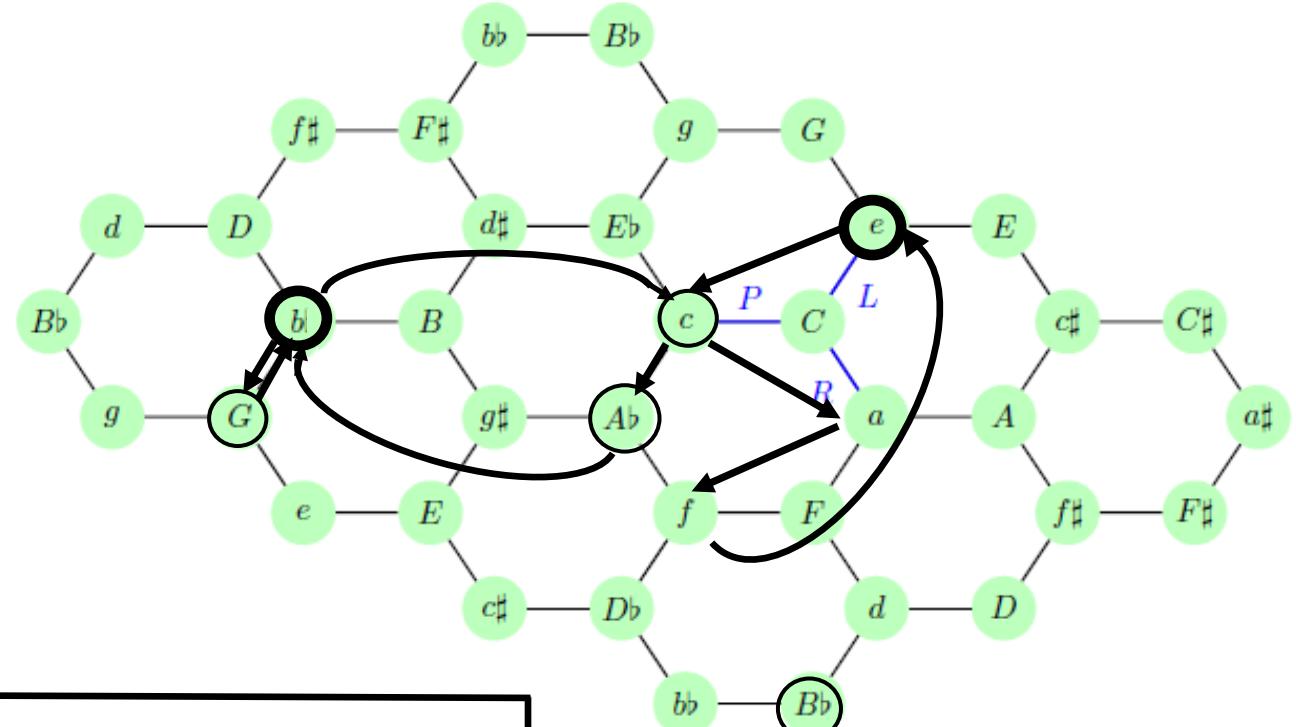


(Source <http://www.mathisintheair.org/>)

Parcours harmoniques chez Arthur H



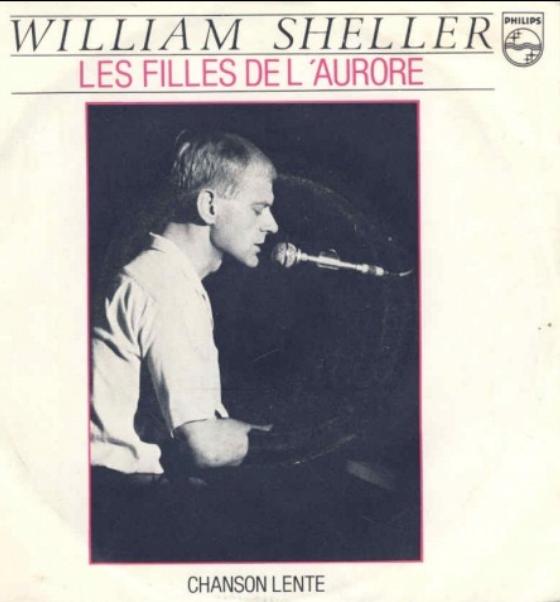
Le Baron noir (album *Piano solo*, 2002)



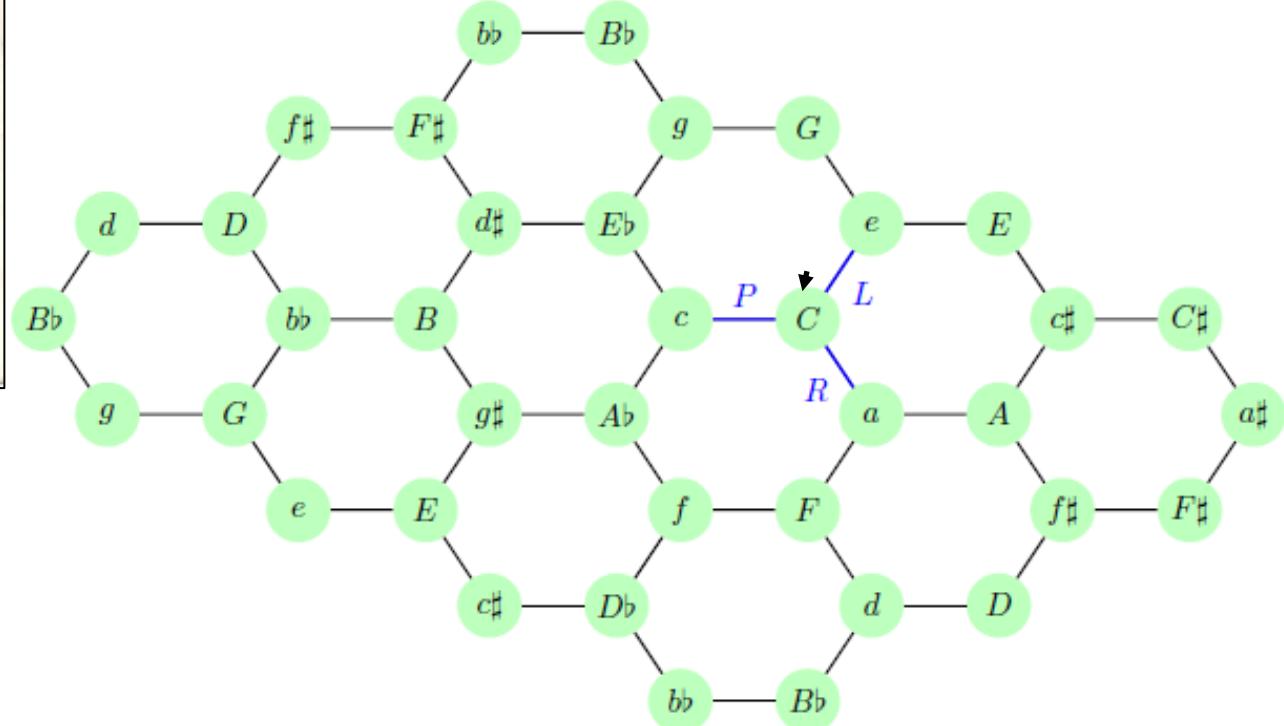
Cycle 1 : Bm $\xrightarrow{\text{PL}} \text{Cm} \xrightarrow{\text{L}} \text{Ab} \xrightarrow{\text{PR}} \text{Bm} \xrightarrow{\text{L}} \text{G} \xrightarrow{\text{L}} \text{Bm} \xrightarrow{\text{L}} \text{G} \xrightarrow{\text{L}} \text{Bm}$

Cycle 2 : Em $\xrightarrow{\text{LP}} \text{Cm} \xrightarrow{\text{PL}} \text{Em} \xrightarrow{\text{LP}} \text{Cm} \xrightarrow{\text{PR}} \text{Am} \xrightarrow{\text{LP}} \text{Fm}$
PLRL

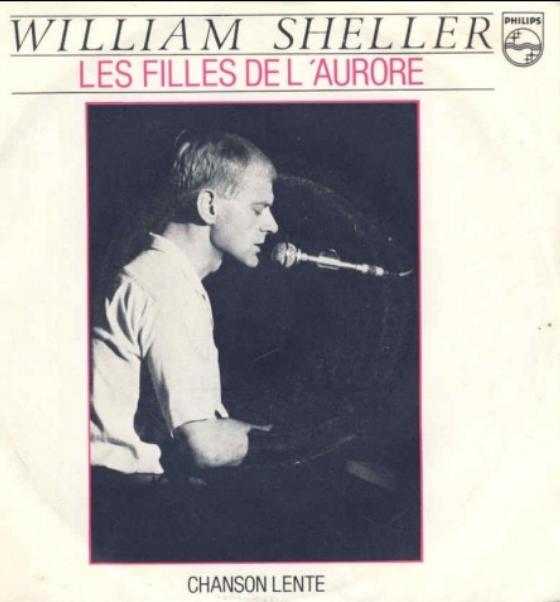
Parcours harmoniques chez William Sheller



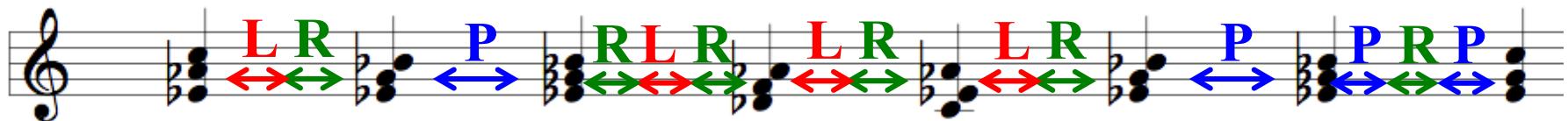
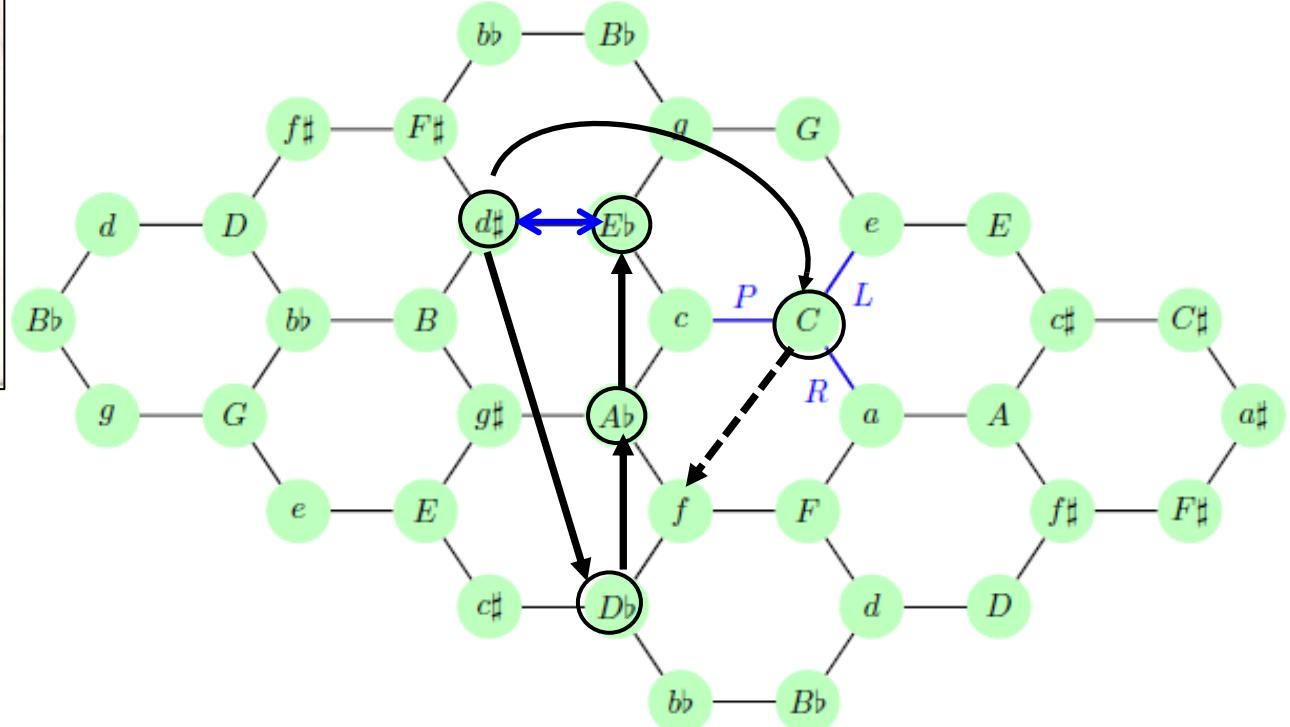
min. 0'33"

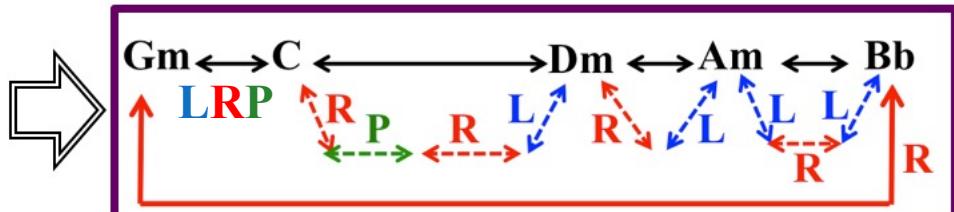
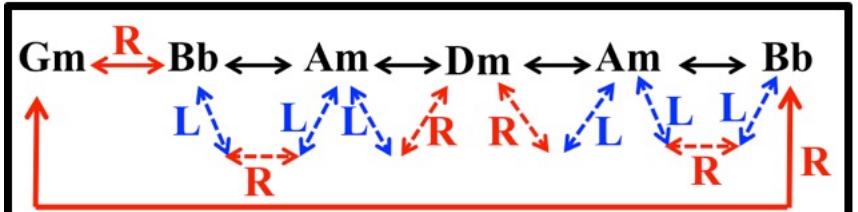


Parcours harmoniques chez William Sheller



min. 0'33"





MON APACHE

(Arman Melies)

Cette promesse, c'est de l'or que tu caches en attendant les apaches et leurs centaures

D'où vient la soie de ton ventre et d'où vient l'ardeur de ces beaux élans que tu défends

Où vont les flots noirs de cendre

les vaisseaux logés au creux de ta peau couleur d'encre

Une flèche en plein cœur un ciel à la dérive et je meurs de nous survivre

on allez sur la grève de nouveau enfin libre et je crève de nous survivre

on allez sur la grève de nouveau enfin libre et je crève de nous survivre

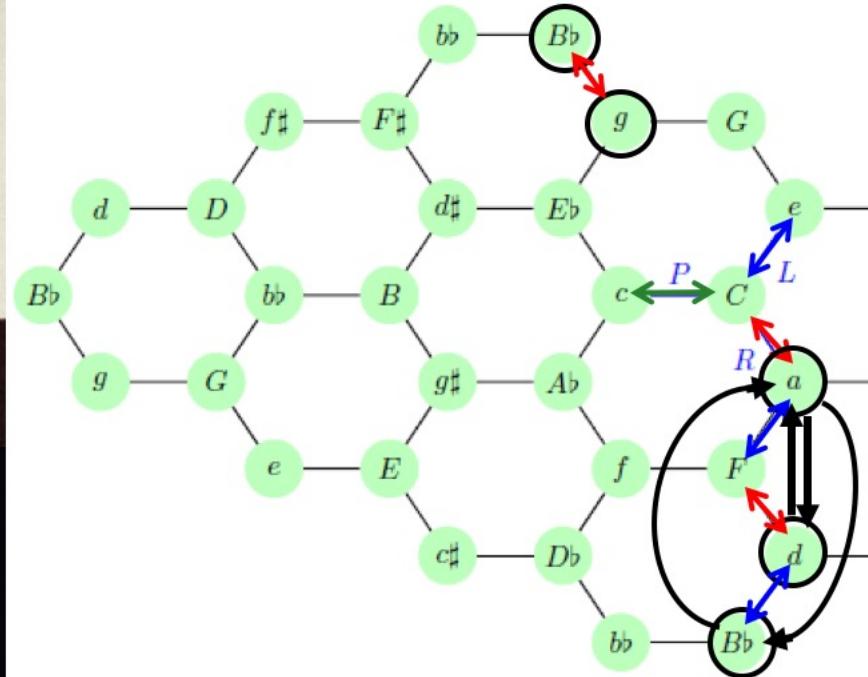
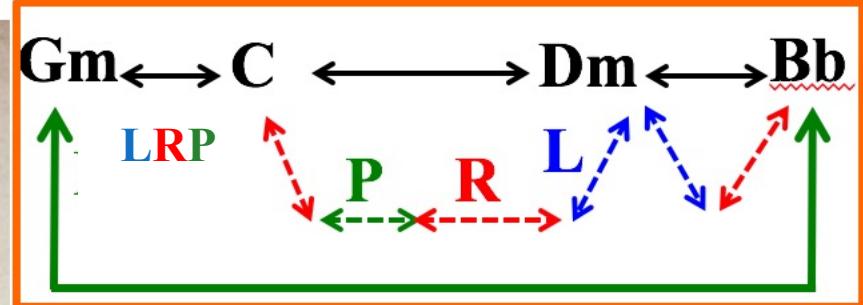
Cette lueur plus encore tu la caches en attendant les apaches et leurs trésors

Cette promesse c'est de l'or que tu caches en attendant les apaches

Cette promesse c'est de l'or que tu caches moi je t'attends

Mon apache

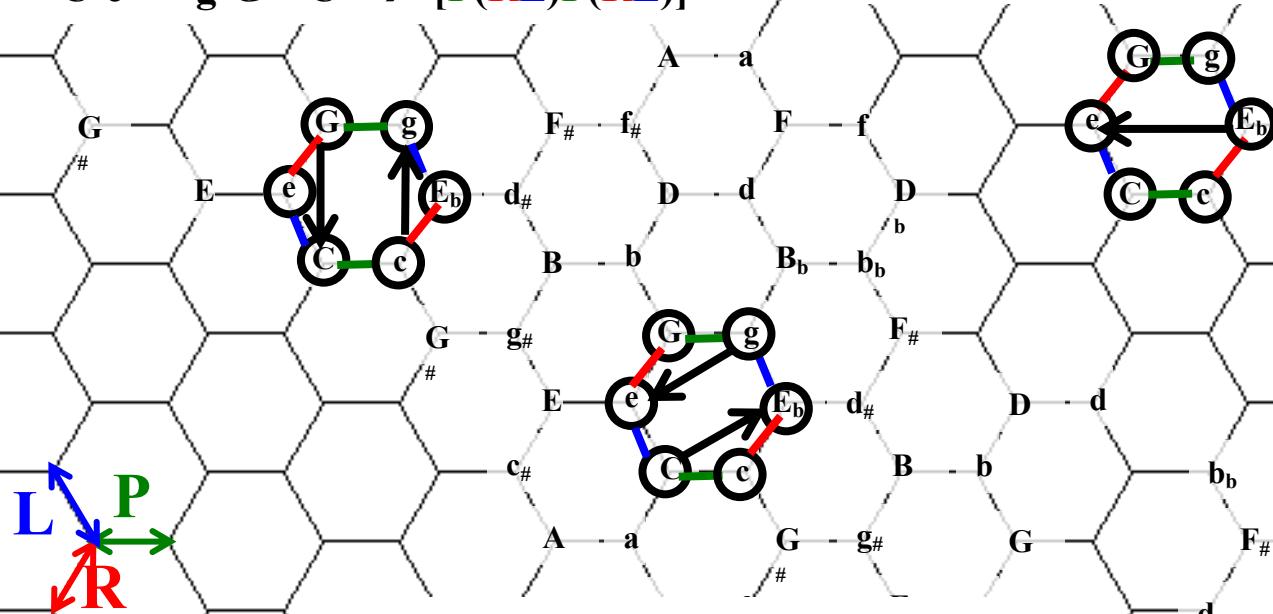
LOVE
Julien Doré



Un cycle et ses raccourcis...

$C-c-E_b-g-G-e-C \rightarrow [PRLPRL]$
 $C-c-----g-G---C \rightarrow [P(RL)P(RL)]$

$C-c-E_b-g-G-e-C \rightarrow [PRLPRL]$
 $C-c-E_b-----e-C \rightarrow [PR(LPR)L]$



$C-c-E_b-g-G-e-C \rightarrow [PRLPRL]$
 $C-----E_b-g---e-C \rightarrow [(PR)L(PR)L]$

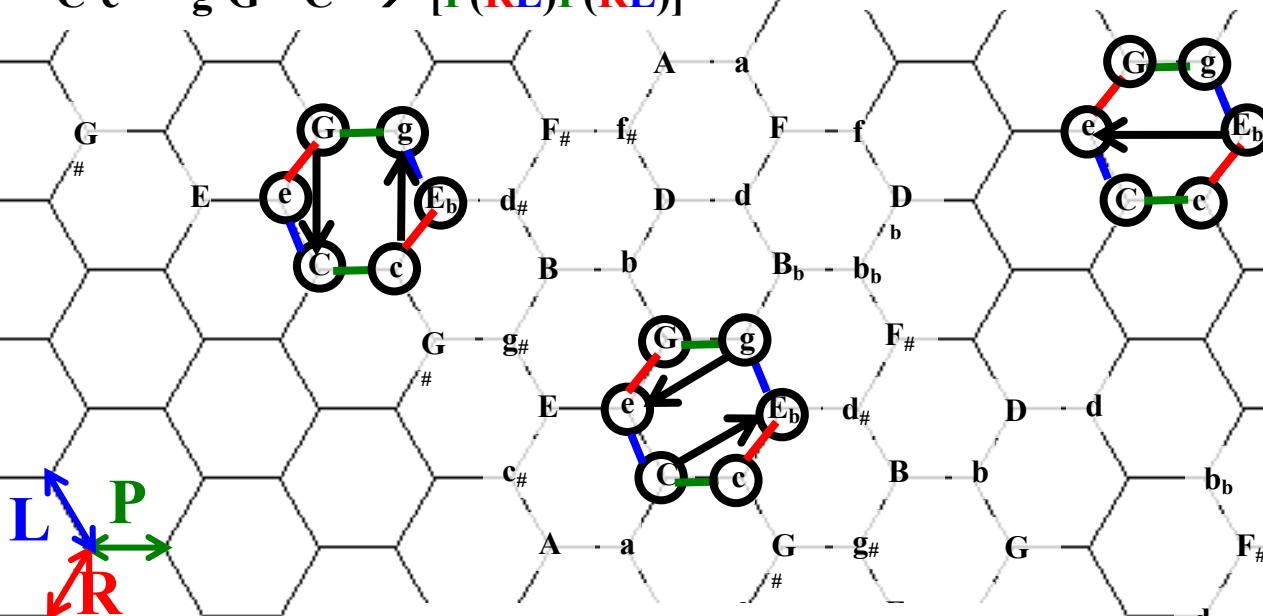
Un cycle et ses raccourcis...

C-c-E_b-g-G-e-C → [PRLPRL]

C-c-----g-G---C → [P(RL)P(RL)]

$$\text{C-c-E}_b\text{-g-G-e-C} \rightarrow [\text{PRLPRL}]$$

$$\text{C}-\text{c}-\text{E}_b-\cdots-\text{e}-\text{C} \rightarrow [\text{PR(LPR)L}]$$

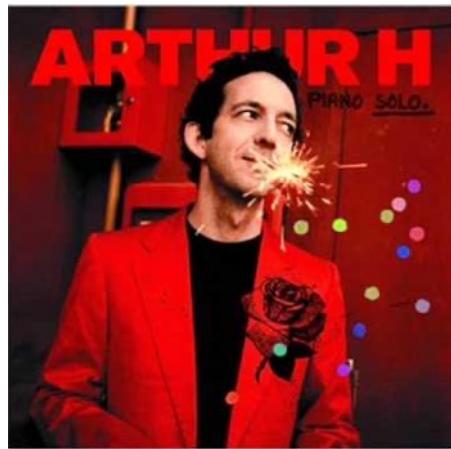


LPR = SLIDE

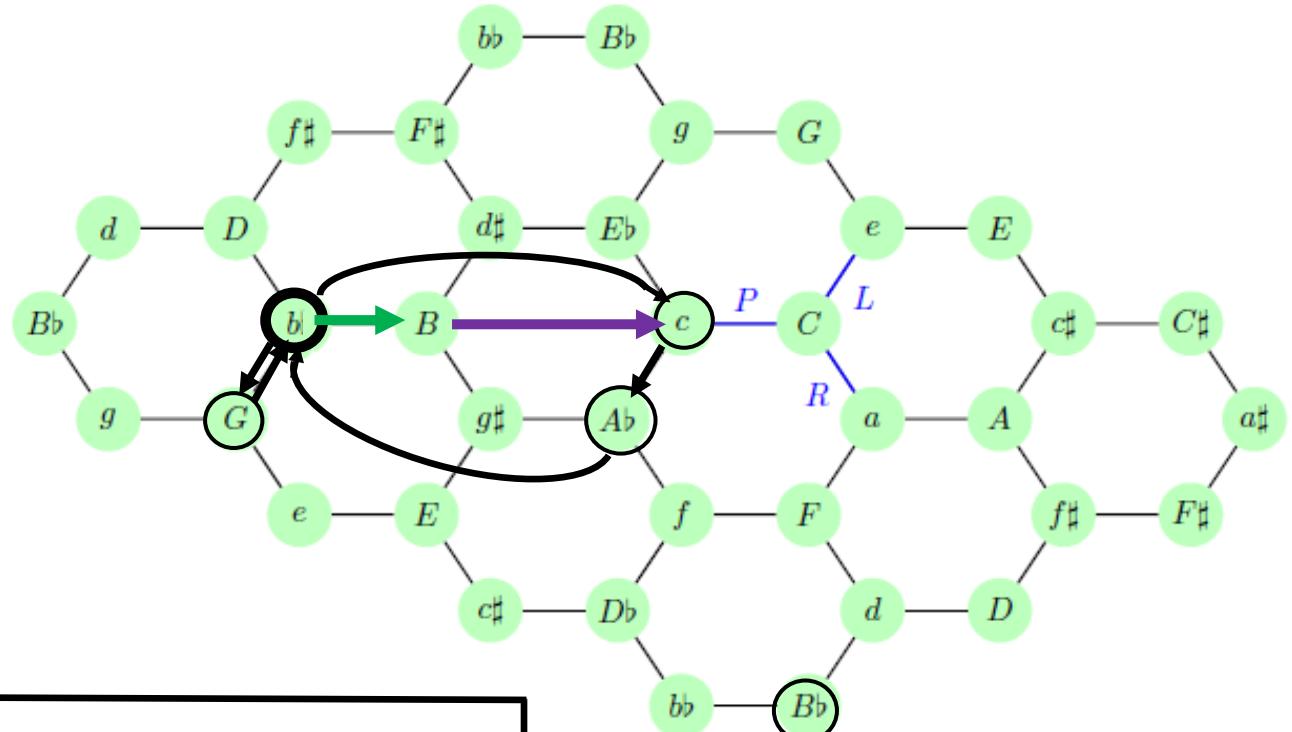
C-c-E_b-g-G-e-C → [PRLPRL]

$$\text{C---E}_b\text{-g---e-C} \rightarrow [(\text{PR})\text{L}(\text{PR})\text{L}]$$

Le SLIDE chez Arthur H



Le Baron noir (album *Piano solo*, 2002)

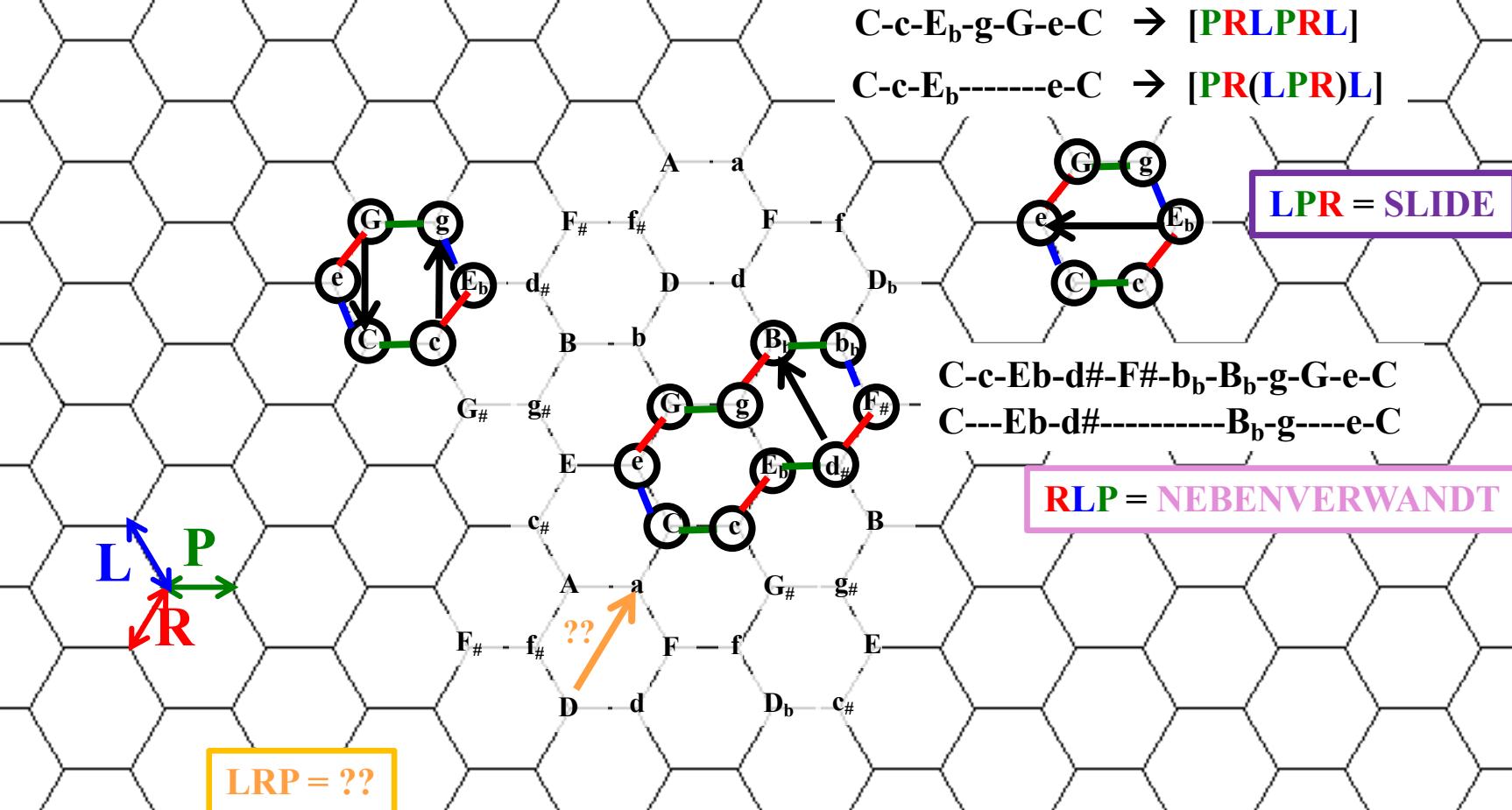


Cycle 1 : $\xrightarrow{\text{Bm}} \xrightarrow[\text{PS}]{\text{PLPR}} \text{Cm} \xrightarrow{\text{L}} \text{Ab} \xrightarrow{\text{PRP}} \text{Bm} \xrightarrow{\text{L}} \text{G} \xrightarrow{\text{L}} \text{Bm} \xrightarrow{\text{L}} \text{G} \xrightarrow{\text{L}} \text{Bm}$

Un cycle et ses raccourcis : SLIDE et NEBENVERWANDT

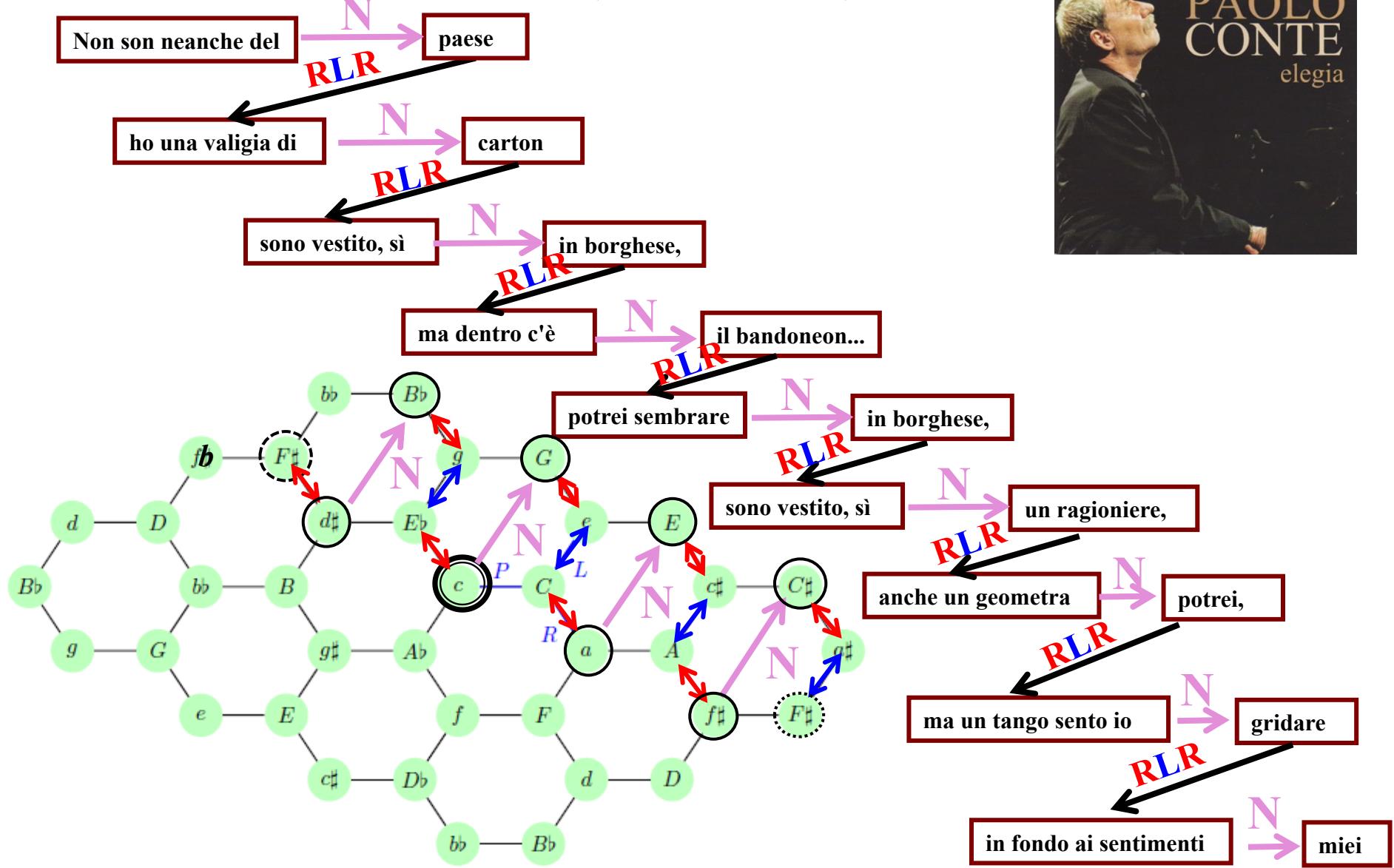
C-c-E_b-g-G-e-C → [PRLPRL]

C-c-----g-G---C → [P(RL)P(RL)]



Les zig-zag du *Nebenverwandt* chez Paolo Conte

IL REGNO DEL TANGO (Paolo Conte)



Harmonic Progressions

In Paolo Conte

Il Regno del Tango

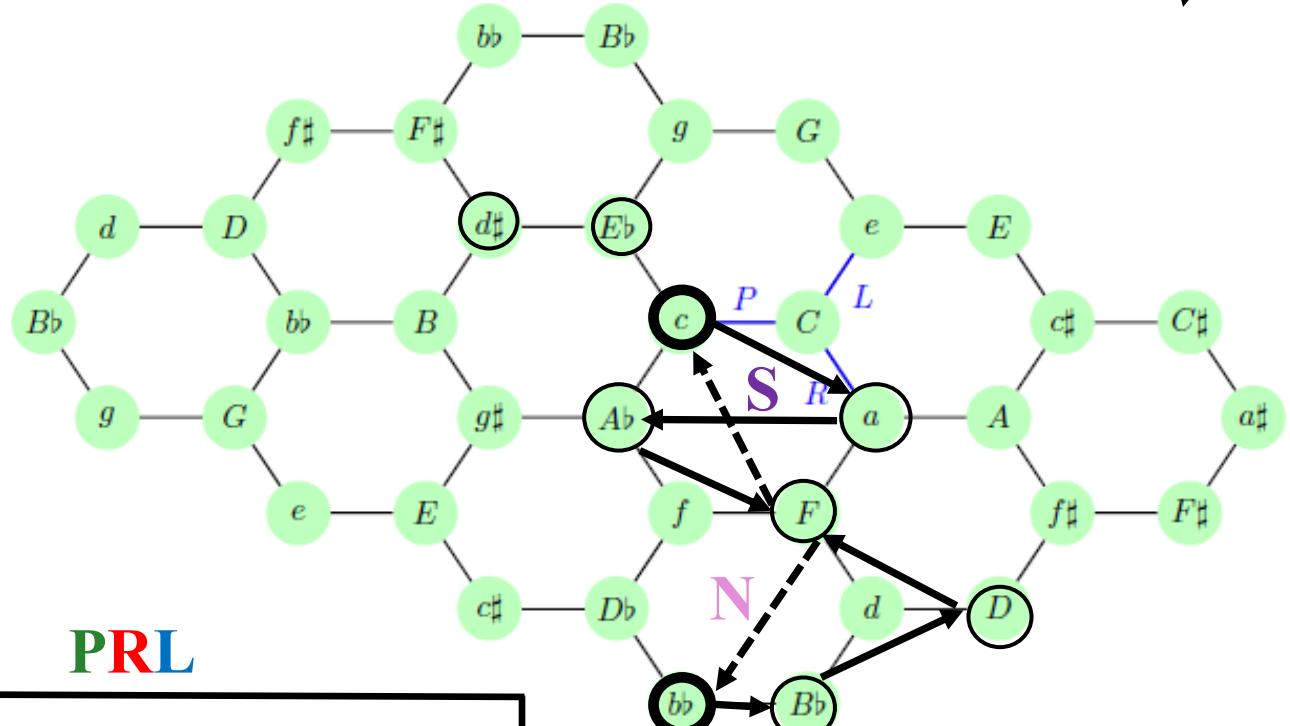


M.Andreatta G.Baroin
www.MatheMusic.net 2016

Parcours harmoniques chez Arthur H



Les Parures Secrètes (album *Pour Madame X*, 2000)



Cycle 1 : Cm $\xrightarrow{\text{PR}}$ Am $\xrightarrow{\text{LPR}=S}$ Ab $\xrightarrow{\text{RP}}$ F

Cycle 1 : Bbm $\xrightarrow{\text{P}}$ Bb $\xrightarrow{\text{LP}}$ D $\xrightarrow{\text{PR}}$ F

↑

PLR=N

Nebenverwandt comme principe modulant



Playlist Spotify
« Cours chanson »

GIURAMENTO
(L. Mello / M. Andreatta)

01:29

g
↓
e
↓
B
↓
d#
↓
*B*b
↓
d

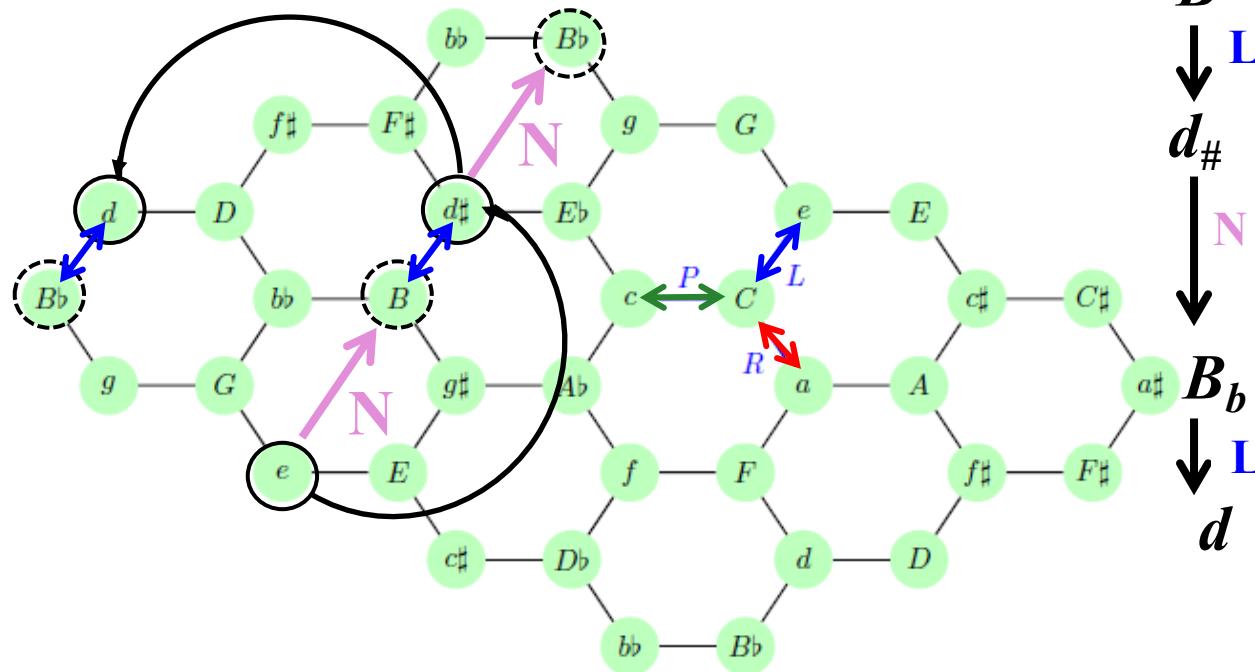
non ci saranno stelle già sfinite
a raccontare stanche i nostri inizi
non ci saranno immagini sfuocate
dell'alba fatta dolce degli abbracci

NL

non ci saranno frasi come lame
e baci di un raccolto più prezioso
non sagome di vetro a cancellare
la schiuma del tuo volto che compare

NL

nel mio respiro fragile d'argilla
non ci sarà la notte a distanziare
la brace dei tuoi angoli di labbra
la luce che nel tuo danzare brilla



Nebenverwandt comme principe modulant



Playlist Spotify
« Cours chanson »

01:29

FRANGIFLUTTI
(L. Mello / M. Andreatta)

Nel rifrangere i nostri cuori,
– gente nata che esige cura –
sono stato tra i meno bravi
nella tua favola insicura.

NL

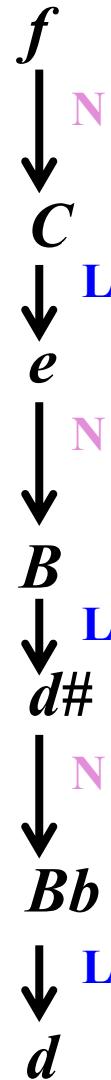
Ora è tardi lo so oramai
venti freddi come una fiaba
però tengo a cantare il canto
Eva sola che resta maga.

NL

Eva cenno di ribellione
Eva fascio pronto all'addio
Eva donna che sa parlare
Al silenzio fatto d'oblio.

NL

Sai parole da incatenare
sai sorridere per piacere
sai scappare senza tornare
sai ferire e sai far l'amore.



Le jeu des modulations dans *Madeleine* de Paolo Conte

Preludio *Moderato*

Lab → Réb/Fa → Sib⁷ → Mib⁷/Réb

Chorus

→ Lab → Réb/Fa → Sib⁷ → Mib⁷/Réb

→ Si/Ré# → Mi → Do# → Fa#

→ Ré/La → Sol → Mi⁷ → La⁷

→ Ré → Lab⁷ → Réb → Do⁷ → Mib⁷

Stefano La Via, *Poesia per musica e musica per poesia. Dai trovatori a Paolo Conte*, Carocci, 2006

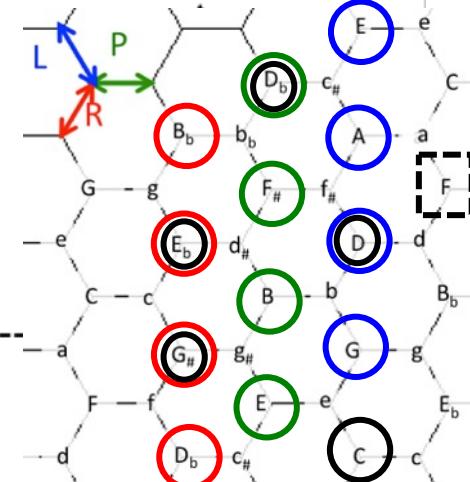
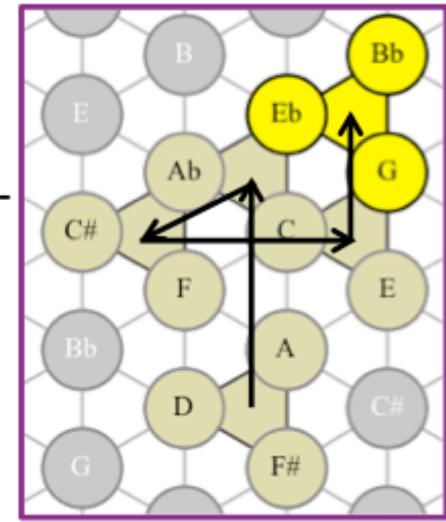
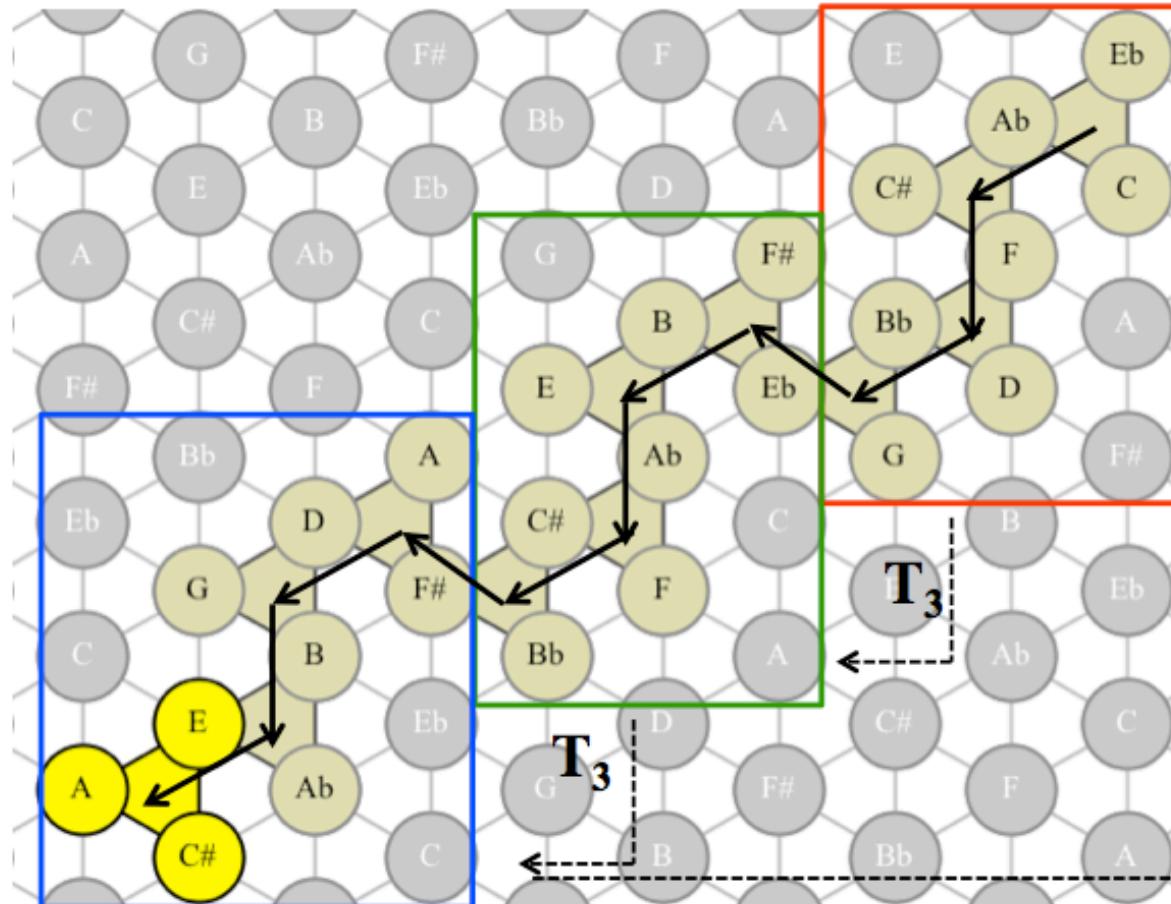
Stefano
La Via
**POESIA
PERMUSICA
EMUSICA
PERPOESIA**

Dai trovatori
a Paolo Conte
Contiene CD-ROM



Le jeu des modulations dans *Madeleine de Paolo Conte*

La_b Re_b Si_b Mi_b Si Mi Re_b Fa_# Re Sol Mi La Re La_b Re_b Do Mi_b

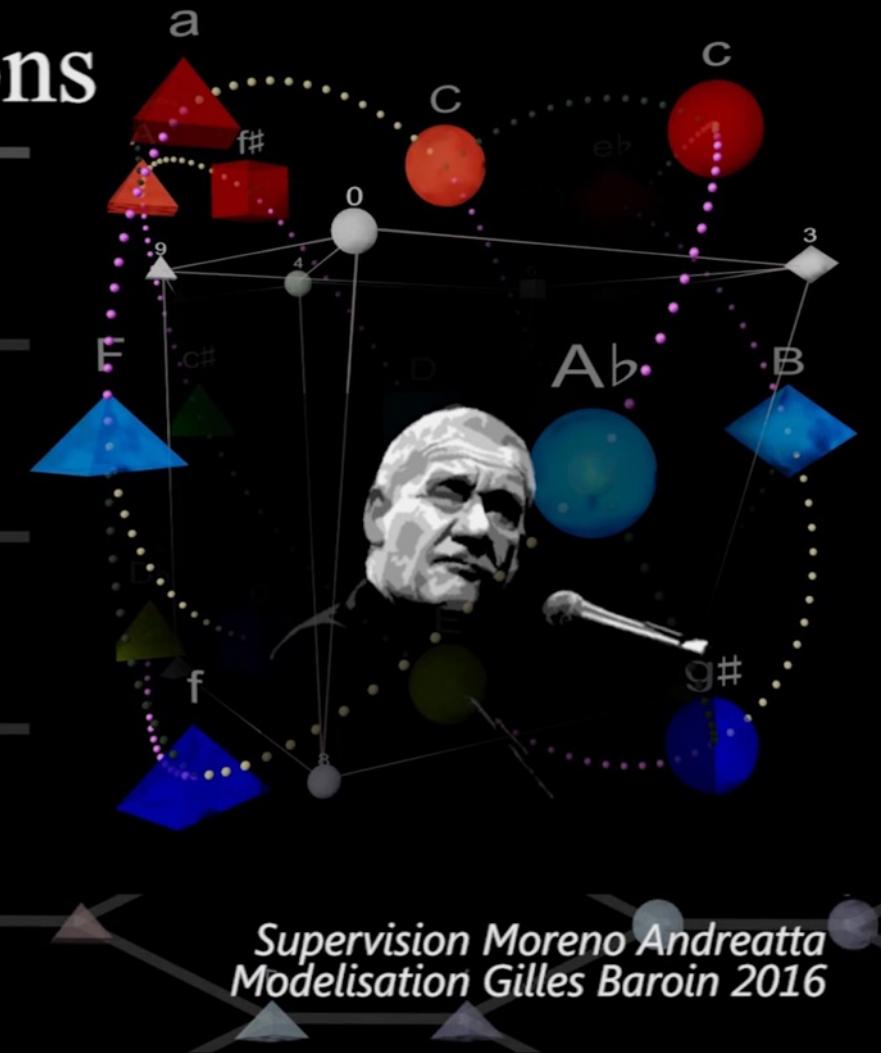
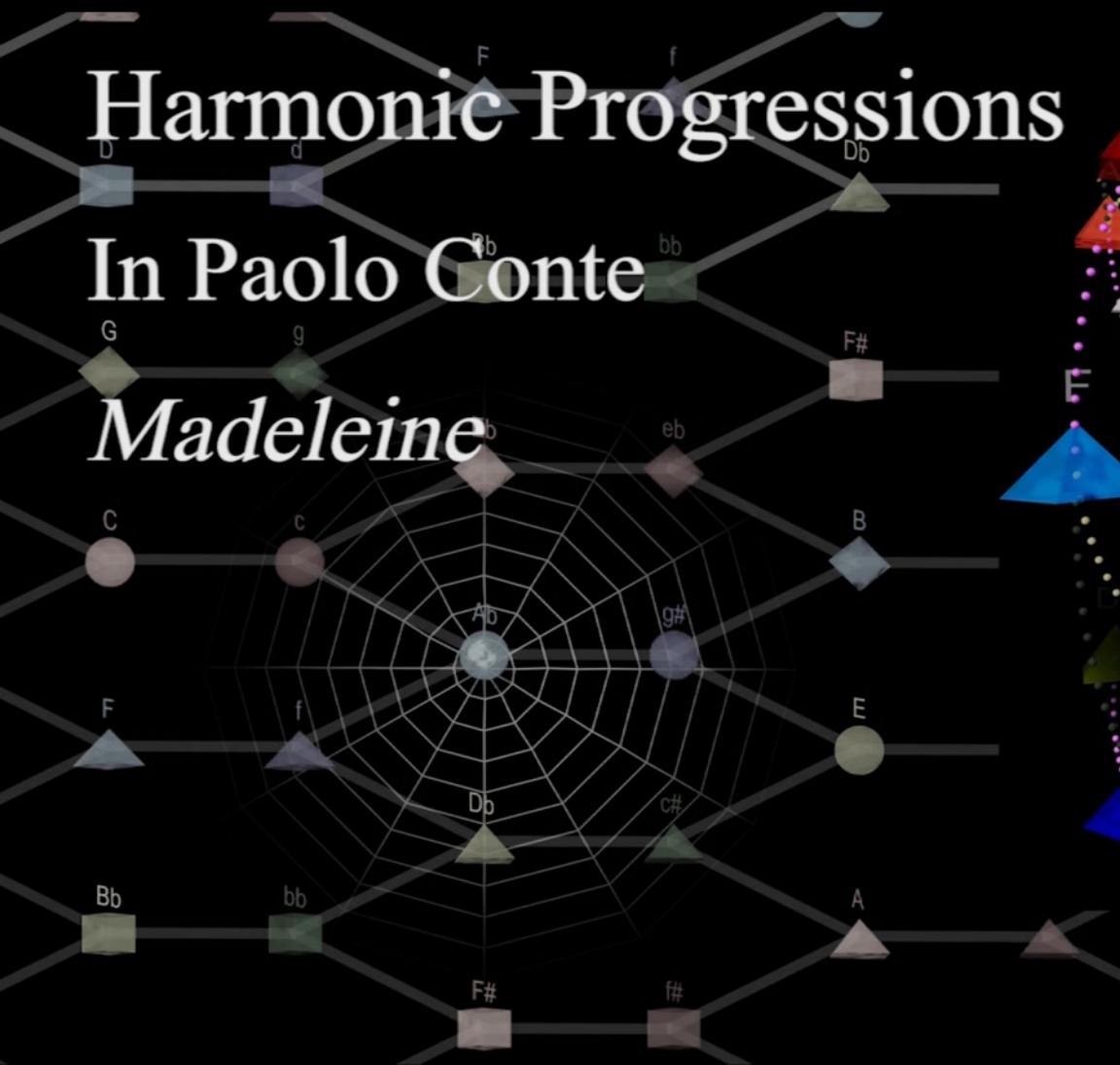


‘Recouvrement’ de l'espace des accords majeurs

Harmonic Progressions

In Paolo Conte

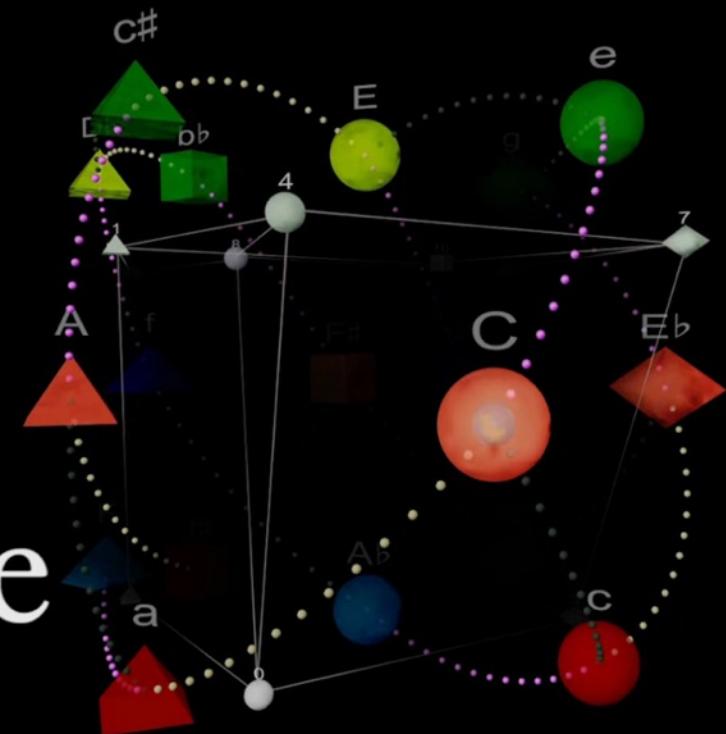
Madeleine



*Supervision Moreno Andreatta
Modélisation Gilles Baroin 2016*

Beethoven and the Hypersphere

(and the Tonnetz)



Gilles Baroin 2016
www.MatheMusic.net



Gilles Baroin

Hamiltonian Song

www.MatheMusic.net

Le Blé en Herbe

Lyrics, music and performance by Polo
Mathemusical supervision by Moreno Andreatta
Hyperspheres and animation by Gilles Baroin, 2016



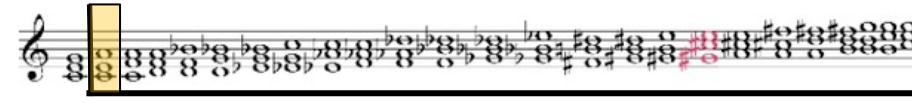
Polo Lamy



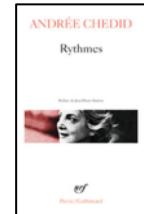
Gilles Baroin



Choix de la tonalité à partir du zig-zag



temps



A part (Andrée Chedid, poème tiré du recueil *Rythmes*, Gallimard, 2018)

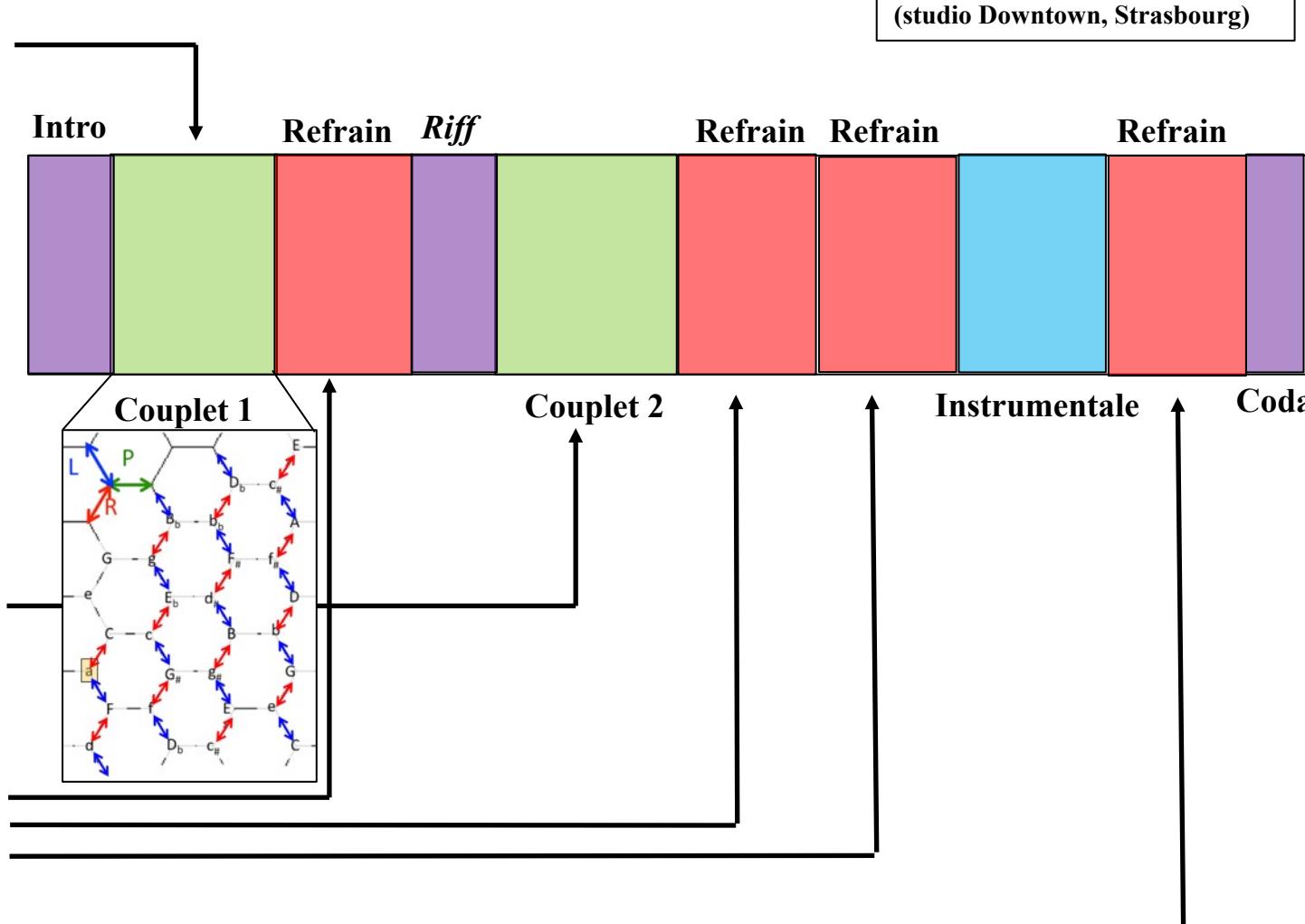
À part le temps
Et ses rouages
À part la terre
En éruptions
À part le ciel
Pétrisseur de nuages
À part l'ennemi
Qui génère l'ennemi

À part le désamour
Qui ronge l'illusion
À part la durée
Qui moisit nos visages

À part les fléaux
À part la tyrannie
À part l'ombre et le crime
Nos batailles nos outrages

Je te célèbre ô Vie
Entre cavités et songes
Intervalle convoité
Entre le vide et le rien

Composition : Moreno Andreatta
Arrangement : Benoît Messinger
Mixage : Didier Houbre
(studio Downtown, Strasbourg)



Arrang. : B. Messinger

Cycles hamiltoniens avec périodicité interne

8. C-Cm-Eb-Gm-Bb-Dm-F-Fm-Ab-Abm-B-Ebm-F#-Bbm-C#-C#m-E-Em-G-Bm-D-F#m-A-Am--PRLRLRPR
9. C-Em-E-Abm-Ab-Cm-Eb-Gm-G-Bm-B-Ebm-F#-Bbm-Bb-Dm-D-F#m-A-C#m-C#-Fm-F-Am--LPLPLR
10. C-Em-E-Abm-B-Ebm-Eb-Gm-G-Bm-D-F#m-F#-Bbm-Bb-Dm-F-Am-A-C#m-C#-Fm-Ab-Cm--LPLRLP
11. C-Em-G-Gm-Bb-Bbm-C#-C#m-E-Abm-B-Bm-D-Dm-F-Fm-Ab-Cm-Eb-Ebm-F#-F#m-A-Am--LRPRPRPR
12. C-Em-G-Gm-Bb-Bbm-C#-Fm-Ab-Cm-Eb-Ebm-F#-F#m-A-C#m-E-Abm-B-Bm-D-Dm-F-Am--LRPRPRLR



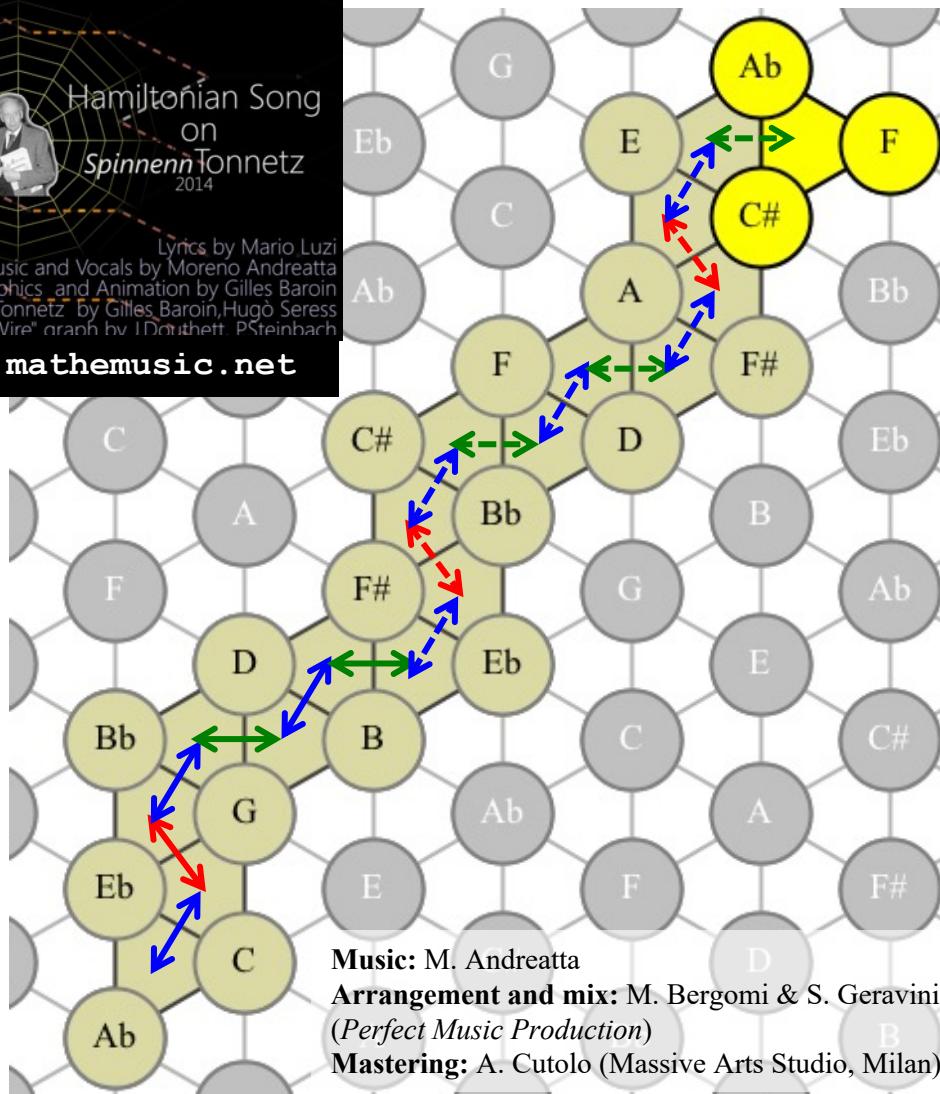
L P L P L R ...
 P L P L R L ...
 L P L R L P ...
 PL R L P L ...
L R L P L P ...
 R L P L P L ...

Luzi



<http://www.mathemusic.net>

min. 1'02"



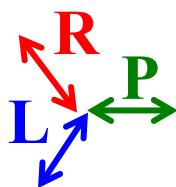
La sera non è più la tua canzone
 (Mario Luzi, 1945, in *Poesie sparse*)

La sera non è più la tua canzone,
 è questa roccia d'ombra traforata
 dai lumi e dalle voci senza fine,
 la quiete d'una cosa già pensata.

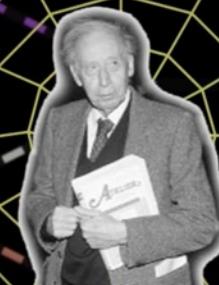
Ah questa luce viva e chiara viene
 solo da te, sei tu così vicina
 al vero d'una cosa conosciuta,
 per nome hai una parola ch'è passata
 nell'intimo del cuore e s'è perduta.

Caduto è più che un segno della vita,
 riposi, dal viaggio sei tornata
 dentro di te, sei scesa in questa pura
 sostanza così tua, così romita
 nel silenzio dell'essere, (compiuta).

L'aria tace ed il tempo dietro a te
 si leva come un'arida montagna
 dove vaga il tuo spirito e si perde,
 un vento raro scivola e ristagna.



Luzi



Hamiltonian Song on *SpinnenTonnetz* 2014

Lyrics by Mario Luzi

Music and Vocals by Moreno Andreatta

Graphics and Animation by Gilles Baroin

SpinnenTonnetz by Gilles Baroin, Hugò Seress

Original "Chicken Wire" graph by J.Douthett, P.Steinbach

La collection des 28 cycles hamiltoniens « redondants »

1. C-Cm-Ab-Abm-E-C#m-A-Am-F-Fm-C#-Bbm-F#-F#m-D-Dm-Bb-Gm-Eb-Ebm-B-Bm-G-Em--PLPLRL
2. C-Cm-Ab-Fm-C#-C#m-A-Am-F-Dm-Bb-Bbm-F#-F#m-D-Bm-G-Gm-Eb-Ebm-B-Abm-E-Em--PLRLPL
3. C-Cm-Eb-Ebm-F#-F#m-A-C#m-E-Em-G-Gm-Bb-Bbm-C#-Fm-Ab-Abm-B-Bm-D-Dm-F-Am--PRPRPRLR
4. C-Cm-Eb-Ebm-F#-Bbm-C#-C#m-E-Em-G-Gm-Bb-Dm-F-Fm-Ab-Abm-B-Bm-D-F#m-A-Am--PRPRLRPR
5. C-Cm-Eb-Ebm-F#-Bbm-C#-Fm-Ab-Abm-B-Bm-D-F#m-A-C#m-E-Em-G-Gm-Bb-Dm-F-Am--PRPRLRLR
6. C-Cm-Eb-Gm-Bb-Bbm-C#-C#m-E-Em-G-Bm-D-Dm-F-Fm-Ab-Abm-B-Ebm-F#-F#m-A-Am--PRLRPRPR
7. C-Cm-Eb-Gm-Bb-Bbm-C#-Fm-Ab-Abm-B-Ebm-F#-F#m-A-C#m-E-Em-G-Bm-D-Dm-F-Am--PRLRPRPR
8. C-Cm-Eb-Gm-Bb-Dm-F-Fm-Ab-Abm-B-Ebm-F#-Bbm-C#-C#m-E-Em-G-Bm-D-F#m-A-Am--PRLRRLRPR
9. **C-Em-E-Abm-Ab-Cm-Eb-Gm-G-Bm-B-Ebm-F#-Bbm-Bb-Dm-D-F#m-A-C#m-C#-Fm-F-Am--LPLPLR**
10. C-Em-E-Abm-B-Ebm-Eb-Gm-G-Bm-D-F#m-F#-Bbm-Bb-Dm-F-Am-A-C#m-C#-Fm-Ab-Cm--LPLRLP
11. C-Em-G-Gm-Bb-Bbm-C#-C#m-E-Abm-B-Bm-D-Dm-F-Fm-Ab-Cm-Eb-Ebm-F#-F#m-A-Am--LRPRPRPR
12. C-Em-G-Gm-Bb-Bbm-C#-Fm-Ab-Cm-Eb-Ebm-F#-F#m-A-C#m-E-Abm-B-Bm-D-Dm-F-Am--LRPRPRLR
13. C-Em-G-Gm-Bb-Dm-F-Fm-Ab-Cm-Eb-Ebm-F#-Bbm-C#-C#m-E-Abm-B-Bm-D-F#m-A-Am--LRPR
14. C-Em-G-Bm-B-Ebm-Eb-Gm-Bb-Dm-D-F#m-F#-Bbm-C#-Fm-F-Am-A-C#m-E-Abm-Ab-Cm--LRLPLP
15. C-Em-G-Bm-D-Dm-F-Fm-Ab-Cm-Eb-Gm-Bb-Bbm-C#-C#m-E-Abm-B-Ebm-F#-F#m-A-Am--LRLRPRPR
16. C-Em-G-Bm-D-F#m-A-C#m-E-Abm-B-Ebm-F#-Bbm-C#-Fm-Ab-Cm-Eb-Gm-Bb-Dm-F-Am--LR
17. C-Am-A-F#m-F#-Ebm-Eb-Cm-Ab-Fm-F-Dm-D-Bm-B-Abm-E-C#m-C#-Bbm-Bb-Gm-G-Em--RPRPRPRL
18. C-Am-A-F#m-F#-Ebm-B-Abm-Ab-Fm-F-Dm-D-Bm-G-Em-E-C#m-C#-Bbm-Bb-Gm-Eb-Cm--RPRPRLRP
19. C-Am-A-F#m-F#-Ebm-B-Abm-E-C#m-C#-Bbm-Bb-Gm-Eb-Cm-Ab-Fm-F-Dm-D-Bm-G-Em--RPRPRLRL
20. C-Am-A-F#m-D-Bm-B-Abm-Ab-Fm-F-Dm-Bb-Gm-G-Em-E-C#m-C#-Bbm-F#-Ebm-Eb-Cm--RPRLRPRP
21. C-Am-A-F#m-D-Bm-B-Abm-E-C#m-C#-Bbm-F#-Ebm-Eb-Cm-Ab-Fm-F-Dm-Bb-Gm-G-Em--RPRL
22. C-Am-A-F#m-D-Bm-G-Em-E-C#m-C#-Bbm-F#-Ebm-B-Abm-Ab-Fm-F-Dm-Bb-Gm-Eb-Cm--RPRLRLRP
23. C-Am-F-Fm-C#-C#m-A-F#m-D-Dm-Bb-Bbm-F#-Ebm-B-Bm-G-Gm-Eb-Cm-Ab-Abm-E-Em--RLPLPL
24. C-Am-F-Dm-D-Bm-B-Abm-Ab-Fm-C#-Bbm-Bb-Gm-G-Em-E-C#m-A-F#m-F#-Ebm-Eb-Cm--RLRPRPRP
25. C-Am-F-Dm-D-Bm-B-Abm-E-C#m-A-F#m-F#-Ebm-Eb-Cm-Ab-Fm-C#-Bbm-Bb-Gm-G-Em--RLRPRPRL
26. C-Am-F-Dm-D-Bm-G-Em-E-C#m-A-F#m-F#-Ebm-B-Abm-Ab-Fm-C#-Bbm-Bb-Gm-Eb-Cm--RLRP
27. C-Am-F-Dm-Bb-Gm-G-Em-E-C#m-A-F#m-D-Bm-B-Abm-Ab-Fm-C#-Bbm-F#-Ebm-Eb-Cm--RLRLRPRP
28. C-Am-F-Dm-Bb-Gm-Eb-Cm-Ab-Fm-C#-Bbm-F#-Ebm-B-Abm-E-C#m-A-F#m-D-Bm-G-Em--RL



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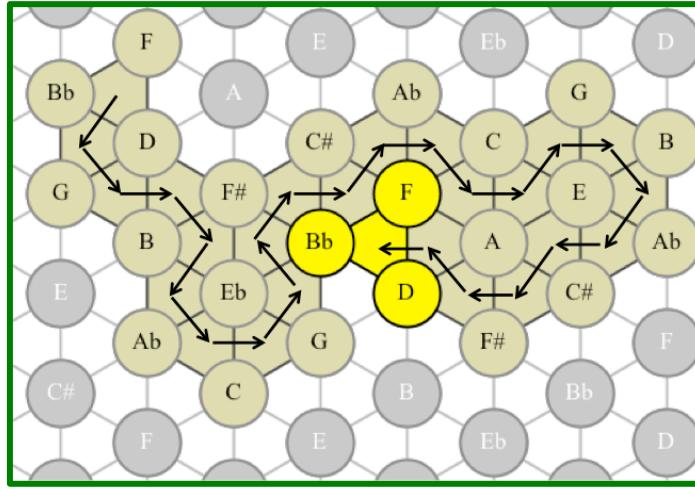
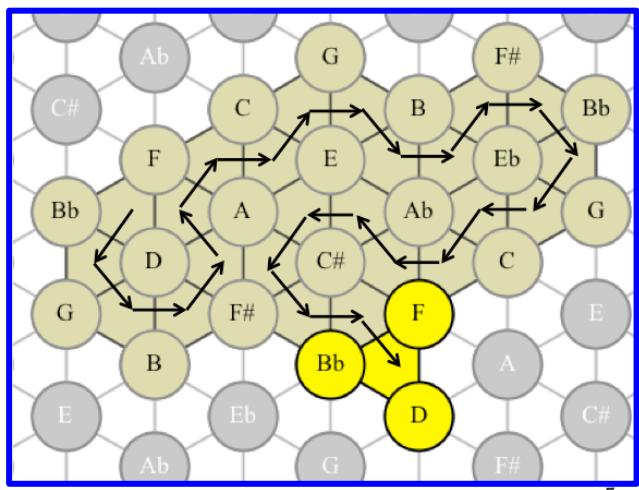
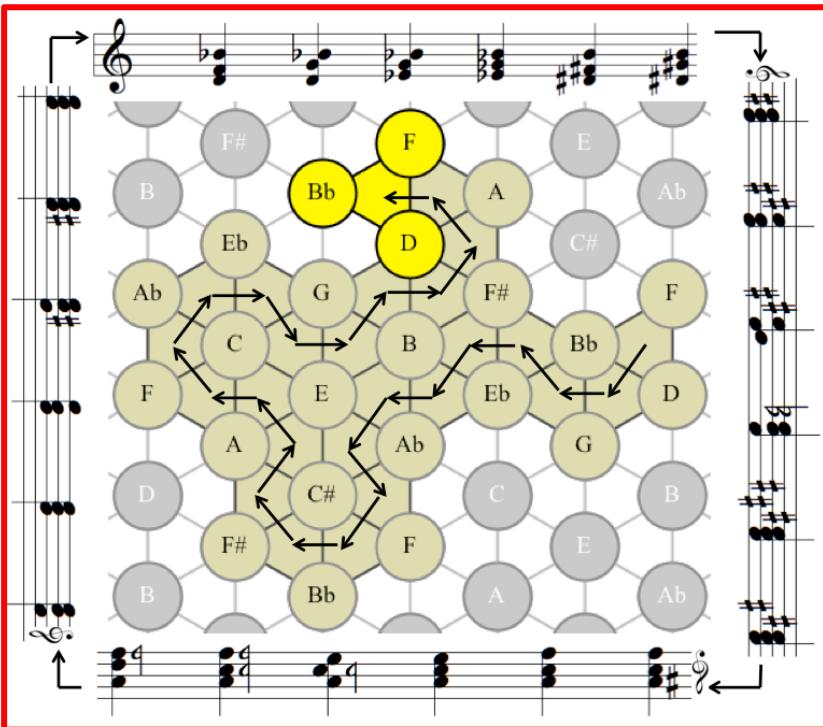
List of 124 Hamiltonian Cycles (Bigo/Andreatta, February 2016)

1. C-Cm-Ab-Abm-E-Em-G-Gm-Eb-Ebm-B-Bm-D-Dm-Bb-Bbm-F#-F#m-A-C#m-C#-Fm-F-Am--PLPLPRLPLPRLPRLPRLPRLPLR
2. C-Cm-Ab-Abm-E-Em-G-Gm-Eb-Ebm-B-Bm-D-F#m-F#-Bbm-Bb-Dm-F-Fm-C#-C#m-A-Am--PLPLPRLPLPRLPRLPRLPRLPLR
3. C-Cm-Ab-Abm-E-G-Bm-B-Ebm-Eb-Gm-Bb-Bbm-F#-F#m-D-Dm-F-Fm-C#-C#m-A-Am--PLPLPRLPLPRLPRLPRLPRL
4. C-Cm-Ab-Abm-E-C#m-C#-Fm-F-Am-A-F#m-F#-Bbm-Bb-Dm-D-Bm-B-Ebm-Eb-Gm-G-Em--PLPLPRLPLPRLPRLPRLPRL
5. C-Cm-Ab-Abm-E-C#m-A-Am-F-Fm-C#-Bbm-F#-F#m-D-Dm-Bb-Gm-Eb-Ebm-B-Bm-G-Em--PLPLRL
6. C-Cm-Ab-Abm-B-Bm-G-Gm-Eb-Ebm-F#-F#m-D-Dm-Bb-Bbm-C#-Fm-F-Am-A-C#m-E-Em--PLPRPLPLPRLPRLPRLPRLPRL
7. C-Cm-Ab-Abm-B-Bm-G-Gm-Eb-Ebm-F#-Bbm-Bb-Dm-D-F#m-A-Am-F-Fm-C#-C#m-E-Em--PLPRPLPLPRLPRLPRLPRLPRL
8. C-Cm-Ab-Abm-B-Bm-G-Em-E-C#m-A-F#m-D-Dm-Bb-Gm-Eb-Ebm-F#-Bbm-C#-Fm-F-Am--PLPRPLRPLRPLRPLRPLR
9. C-Cm-Ab-Abm-B-Ebm-Eb-Gm-G-Bm-D-Dm-Bb-Bbm-F#-F#m-A-Am-F-Fm-C#-C#m-E-Em--PLPLPRLPLPRLPRLPRLPRL
10. C-Cm-Ab-Abm-B-Ebm-Eb-Gm-Bb-Dm-D-Bm-G-Em-E-C#m-A-F#m-F#-Bbm-C#-Fm-F-Am--PLPRPLPRLPRLPRLPRLPRL
11. C-Cm-Ab-Abm-B-Ebm-Eb-Gm-Bb-Dm-F-Fm-C#-Bbm-F#-F#m-D-Bm-G-Em-E-C#m-A-Am--PLPLPRLPRLPRLPRLPRLPRL
12. C-Cm-Ab-Fm-F-Am-A-C#m-C#-Bbm-Bb-Dm-D-F#m-F#-Ebm-Eb-Gm-G-Bm-B-Abm-E-Em--PLRPLPRLPRLPRLPRLPRL
13. C-Cm-Ab-Fm-F-Am-A-F#-F#-Bbm-C#-C#m-E-Abm-B-Ebm-Eb-Gm-Bb-Dm-D-Bm-G-Em--PLRPLPRLPRLPRLPRLPRL
14. C-Cm-Ab-Fm-F-Am-A-F#m-D-Dm-Bb-Gm-Eb-Ebm-F#-Bbm-C#-C#m-E-Abm-B-Bm-G-Em--PLRPLPRLPRLPRLPRLPRL
15. C-Cm-Ab-Fm-F-Dm-Bb-Gm-Eb-Ebm-B-Abm-E-Em-G-Bm-D-F#m-F#-Bbm-C#-C#m-A-Am--PLRPLPRLPRLPRLPRLPRLPRL
16. C-Cm-Ab-Fm-C#-C#m-A-Am-F-Dm-Bb-Bbm-F#-F#m-D-Bm-G-Gm-Eb-Ebm-B-Abm-E-Em--PLRLPRL
17. C-Cm-Ab-Fm-C#-C#m-A-F#-Bbm-Bb-Gm-Eb-Ebm-B-Abm-E-Em-G-Bm-D-Dm-F-Am--PLRLPRLPRLPRLPRLPRLPRL
18. C-Cm-Ab-Fm-C#-C#m-A-F#m-D-Bm-B-Abm-E-Em-G-Gm-Eb-Ebm-F#-Bbm-Bb-Dm-F-Am--PLRLPRLPRLPRLPRLPRL
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20. C-Cm-Ab-Fm-C#-C#m-E-Abm-B-Bm-Eb-Gm-Bb-Bbm-F#-F#m-A-Am-F-Dm-D-Bm-G-Em--PLRLPRLPRLPRLPRLPRL
21. C-Cm-Ab-Fm-C#-Bbm-Bb-Dm-F-Am-A-C#m-E-Abm-B-Bm-D-F#m-F#-Ebm-Eb-Gm-G-Em--PLRLPRLPRLPRLPRLPRLPRL
22. C-Cm-Ab-Fm-C#-Bbm-Bb-Gm-Eb-Ebm-F#-F#m-D-Dm-F-Am-A-C#m-E-Abm-B-Bm-G-Em--PLRLPRLPRLPRLPRLPRLPRL
23. C-Cm-Eb-Ebm-B-Bm-G-Gm-Bb-Bbm-F#-F#m-D-Dm-F-Am-A-C#m-C#-Fm-Ab-Abm-E-Em--PRPLPRLPRLPRLPRLPRLPRL
24. C-Cm-Eb-Ebm-B-Bm-G-Gm-Bb-Dm-D-F#m-F#-Bbm-C#-C#m-A-Am-F-Fm-Ab-Abm-E-Em--PRPLPRLPRLPRLPRLPRL
25. C-Cm-Eb-Ebm-B-Bm-D-F#m-F#-Bbm-C#-Fm-Ab-Abm-E-C#m-A-Am-F-Dm-Bb-Gm-G-Em--PRPLPRLPRLPRLPRLPRL
26. C-Cm-Eb-Ebm-B-Abm-Ab-Fm-C#-Bbm-F#-F#m-D-Bm-G-Gm-Bb-Dm-F-Am-A-C#m-E-Em--PRPLPRLPRLPRLPRLPRLPRL
27. C-Cm-Eb-Ebm-F#-F#m-A-C#m-E-Em-G-Gm-Bb-Bbm-C#-Fm-Ab-Abm-B-Bm-D-Dm-F-Am--PRPRPLR
28. C-Cm-Eb-Ebm-F#-Bbm-C#-C#m-E-Em-G-Gm-Bb-Dm-F-Fm-Ab-Abm-B-Bm-D-F#m-A-Am--PRPRLR
29. C-Cm-Eb-Ebm-F#-Bbm-C#-Fm-Ab-Abm-B-Bm-D-F#m-A-C#m-E-Em-G-Gm-Bb-Dm-F-Am--PRPRRLR
30. C-Cm-Eb-Gm-G-Bm-B-Ebm-F#-F#m-D-Dm-Bb-Bbm-C#-C#m-A-Am-F-Fm-Ab-Abm-E-Em--PRPLPRLPRLPRLPRLPRLPRL
31. C-Cm-Eb-Gm-G-Bm-D-F#m-F#-Ebm-B-Abm-Ab-Fm-C#-Bbm-Bb-Dm-F-Am-A-C#m-E-Em--PRPLPRLPRLPRLPRLPRLPRL
32. C-Cm-Eb-Gm-G-Bm-D-F#m-A-Am-F-Dm-Bb-Bbm-F#-Ebm-B-Abm-Ab-Fm-C#-C#m-E-Em--PRPLRPLRPLRPLRPLRPLRPL
33. C-Cm-Eb-Gm-G-Em-A-Bm-Ab-Fm-C#-C#m-A-F#m-D-Bm-B-Ebm-F#-Bbm-Bb-Dm-F-Am--PRPLPRLPRLPRLPRLPRL
34. C-Cm-Eb-Gm-Bb-Bbm-F#-Ebm-B-Bm-G-Em-E-Abm-Ab-Fm-C#-C#m-A-F#m-D-Dm-F-Am--PRLRPLRPLRPLRPLRPLRPL
35. C-Cm-Eb-Gm-Bb-Bbm-C#-C#m-E-Em-G-Bm-D-Dm-F-Fm-Ab-Abm-B-Ebm-F#-F#m-A-Am--PRLRPR
36. C-Cm-Eb-Gm-Bb-Bbm-C#-Fm-Ab-Abm-E-C#m-A-Am-F-Dm-D-F#m-F#-Ebm-B-Bm-G-Em--PRLRPLRPLRPLRPLRPL
37. C-Cm-Eb-Gm-Bb-Bbm-C#-Fm-Ab-Abm-B-Ebm-F#-F#m-A-C#m-E-Em-G-Bm-D-Dm-F-Am--PLR
38. C-Cm-Eb-Gm-Bb-Dm-D-F#m-A-Am-F-Fm-Ab-Abm-E-C#m-C#-Bbm-F#-Ebm-B-Bm-G-Em--PRLRPLRPLRPLRPLRPL
39. C-Cm-Eb-Gm-Bb-Dm-D-F#m-A-C#m-C#-Bbm-F#-Ebm-B-Bm-G-Em-E-Abm-Ab-Fm-F-Am--PRLRPLRPLRPLRPLRPLRPL
40. C-Cm-Eb-Gm-Bb-Dm-F-Fm-Ab-Abm-B-Ebm-F#-Bbm-C#-C#m-E-Em-G-Bm-D-F#m-A-Am--PLRPLR
41. C-Em-E-Abm-Ab-Cm-Eb-Ebm-B-Bm-G-Gm-Bb-Bbm-F#-F#m-D-Dm-F-Fm-C#-C#m-A-Am--LPLPRLPRLPRLPRLPRLPRLPRL
42. C-Em-E-Abm-Ab-Cm-Eb-Gm-G-Bm-B-Ebm-F#-Bbm-Bb-Dm-D-F#m-A-C#m-C#-Fm-F-Am--LPLPLR
43. C-Em-E-Abm-Ab-Fm-F-Am-A-C#m-C#-Bbm-Bb-Dm-D-F#m-F#-Ebm-B-Bm-G-Em-Cm--LPLPRLPRLPRLPRLPRLPRLPRL
44. C-Em-E-Abm-Ab-Fm-F-Am-A-C#m-C#-Bbm-F#-F#m-D-Dm-Bb-Gm-G-Bm-B-Ebm-Eb-Cm--LPLPRLPRLPRLPRLPRLPRLPRL
45. C-Em-E-Abm-Ab-Fm-C#-C#m-A-Am-F-Dm-D-F#m-F#-Bbm-Bb-Gm-G-Bm-B-Ebm-Eb-Cm--LPLPRLPRLPRLPRLPRLPRLPRL
46. C-Em-E-Abm-B-Bm-G-Gm-Eb-Ebm-F#-F#m-D-Dm-Bb-Bbm-C#-C#m-A-Am-F-Fm-Ab-Cm--LPLPRLPRLPRLPRLPRLPRL
47. C-Em-E-Abm-B-Bm-G-Gm-Bb-F#-Ebm-Eb-Cm-Ab-Fm-C#-C#m-A-F#m-D-Dm-F-Am--LPLPRLPRLPRLPRLPRLPRL
48. C-Em-E-Abm-B-Bm-G-Gm-Bb-Dm-D-F#m-A-C#m-C#-Bbm-F#-Ebm-Eb-Cm-Ab-Fm-F-Am--LPLPRLPRLPRLPRLPRLPRL
49. C-Em-E-Abm-B-Ebm-Eb-Gm-G-Bm-D-F#m-F#-Bbm-Bb-Dm-F-Am-A-C#m-C#-Fm-Ab-Cm--LPLRPL
50. C-Em-E-Abm-B-Ebm-Eb-Cm-Ab-Fm-F-Dm-Bb-Gm-G-Bm-D-F#m-F#-Bbm-C#-C#m-A-Am--LPLPRLPRLPRLPRLPRLPRL
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52. C-Em-E-Abm-B-Ebm-F#-F#m-D-Bm-G-Gm-Eb-Cm-Ab-Fm-F-Dm-Bb-Bbm-C#-C#m-A-Am--LPLPRLPRLPRLPRLPRLPRL
53. C-Em-E-Abm-B-Ebm-F#-F#m-A-C#m-C#-Bbm-Bb-Dm-D-Bm-G-Gm-Eb-Cm-Ab-Fm-F-Am--LPLPRLPRLPRLPRLPRLPRL

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54. C-Em-E-C#m-C#-Fm-F-Am-A-F#m-F-Bbm-Bb-Dm-D-Bm-G-Gm-Eb-Ebm-B-Abm-Ab-Cm--LPRPLPRLPRLPRLPRLPRLPRLP
55. C-Em-E-C#m-C#-Fm-F-Am-A-F#m-D-Dm-Bb-Bbm-F#-Ebm-Eb-Gm-G-Bm-B-Abm-Ab-Cm--LPRPLPRLPRLPRLPRLPRLP
56. C-Em-E-C#m-C#-Fm-F-Dm-Bb-Bbm-F#-Ebm-B-Abm-Ab-Cm-Eb-Gm-G-Bm-D-F#m-A-Am--LPRPLPRLPRLPRLPRLPRLP
57. C-Em-E-C#m-C#-Fm-Ab-Abm-B-Ebm-F#-Bbm-Bb-Dm-F-Am-A-F#m-D-Bm-G-Gm-Eb-Cm--LPRPLPRLPRLPRLPRLP
58. C-Em-E-C#m-A-Am-F-Fm-C#-Fm-Bb-Dm-D-F#m-F#-Ebm-Eb-Gm-G-Bm-B-Abm-Ab-Cm--LPRPLPRLPRLPRLPRLP
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67. C-Em-G-Gm-Eb-Cm-Ab-Abm-E-C#m-A-F#-Ebm-B-Bm-D-Dm-Bb-Bbm-C#-Fm-F-Am--LRPLPRLPRLPRLPRLP
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69. C-Em-G-Gm-Bb-Bbm-C#-Fm-Ab-Cm-Eb-Ebm-F#-F#m-A-C#m-E-Abm-B-Bm-D-Dm-F-Am--LRPRPR
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82. C-Em-G-Bm-D-Dm-F-Fm-Ab-Cm-Eb-Gm-Bb-Bbm-C#-C#m-E-Abm-B-Ebm-F#-F#m-A-Am--LRLP
83. C-Em-G-Bm-D-Dm-F-Am-A-F#m-F#-Bbm-Bb-Gm-Eb-Ebm-B-Abm-E-C#m-C#-Fm-Ab-Cm--LRLP
84. C-Em-G-Bm-D-F#m-A-C#m-E-Abm-B-Ebm-F#-Bbm-C#-Fm-Ab-Cm-Eb-Gm-Bb-Dm-F-Am--LR
85. C-Am-A-C#m-C#-Fm-F-Dm-D-F#m-F#-Bbm-Bb-Gm-G-Bm-B-Ebm-Eb-Cm-Ab-Abm-E-Em--RPLP
86. C-Am-A-C#m-C#-Fm-F-Dm-D-F#m-F#-Bbm-Bb-Gm-Eb-Ebm-B-Bm-G-Em-E-Abm-Ab-Cm--RPLP
87. C-Am-A-C#m-C#-Fm-F-Dm-Bb-Bbm-F#-F#m-D-Bm-B-Ebm-Eb-Gm-G-Em-E-Abm-Ab-Cm--RPLP
88. C-Am-A-C#m-C#-Bbm-Bb-Dm-F-Fm-Ab-Cm-Eb-Gm-G-Bm-D-F#m-F#-Ebm-B-Abm-E-Em--RPLP
89. C-Am-A-C#m-C#-Bbm-F#-F#m-D-Bm-G-Gm-Bb-Dm-F-Fm-Ab-Cm-Eb-Ebm-B-Abm-E-Em--RPLP
90. C-Am-A-C#m-C#-Bbm-F#-F#m-D-Bm-G-Em-E-Abm-B-Ebm-Eb-Gm-Bb-Dm-F-Fm-Ab-Cm--RPLP
91. C-Am-A-C#m-E-Em-G-Bm-D-F#m-F#-Bbm-C#-Fm-F-Dm-Bb-Gm-Eb-Ebm-B-Abm-Ab-Cm--RPLP
92. C-Am-A-C#m-E-Ab-Cm-Eb-Ebm-B-Bm-D-F#m-F#-Bbm-C#-Fm-F-Dm-Bb-Gm-G-Em--RPLP
93. C-Am-A-C#m-E-Abm-Ab-Cm-Eb-Gm-Bb-Bbm-C#-Fm-F-Dm-D-F#m-F#-Ebm-B-Bm-G-Em--RPLP
94. C-Am-A-F#m-F#-Ebm-Eb-Cm-Ab-Fm-F-Dm-D-Bm-B-Abm-E-C#m-C#-Bbm-Bb-Gm-G-Em--RPRP
95. C-Am-A-F#m-F#-Ebm-B-Abm-Ab-Fm-F-Dm-D-Bm-G-Em-E-C#m-C#-Bbm-Bb-Gm-Eb-Cm--RPRP
96. C-Am-A-F#m-F#-Ebm-B-Abm-E-C#m-C#-Bbm-Bb-Gm-Eb-Cm-Ab-Fm-F-Dm-D-Bm-G-Em--RPRP
97. C-Am-A-F#m-D-Dm-F-Fm-C#-C#m-E-Abm-Ab-Cm-Eb-Gm-Bb-Bbm-F#-Ebm-B-Bm-G-Em--RPLP
98. C-Am-A-F#m-D-Bm-B-Ebm-F#-Bbm-Bb-Dm-F-Fm-C#-C#m-E-Abm-Ab-Cm-Eb-Gm-G-Em--RPLP
99. C-Am-A-F#m-D-Bm-B-Abm-Ab-Fm-F-Dm-Bb-Gm-G-Em-E-C#m-C#-Bbm-F#-Ebm-Eb-Cm--RPLP
100. C-Am-A-F#m-D-Bm-B-Abm-E-C#m-C#-Bbm-F#-Ebm-Eb-Cm-Ab-Fm-F-Dm-Bb-Gm-G-Em--RPR
101. C-Am-A-F#m-D-Bm-G-Gm-Eb-Cm-Ab-Abm-B-Ebm-F#-Bbm-Bb-Dm-F-Fm-C#-C#m-E-Em--RPLP
102. C-Am-A-F#m-D-Bm-G-Em-E-C#m-C#-Bbm-F#-Ebm-B-Abm-Ab-Fm-F-Dm-Bb-Gm-Eb-Cm--RPLR
103. C-Am-F-Fm-C#-C#m-A-F#-F#-Bbm-Bb-Dm-D-Bm-B-Abm-Eb-Gm-G-Em-E-Abm-Ab-Cm--RPLP
104. C-Am-F-Fm-C#-C#m-A-F#m-D-Dm-Bb-Bbm-F#-Ebm-B-Bm-G-Gm-Eb-Cm-Ab-Abm-E-Em--RPLP
105. C-Am-F-Fm-C#-Bbm-Bb-Dm-D-Bm-B-Abm-F#-F#m-A-C#m-E-Abm-Ab-Cm-Eb-Gm-G-Em--RPLP
106. C-Am-F-Fm-C#-Bbm-Bb-Dm-D-Bm-G-Gm-Eb-Cm-Ab-Abm-B-Ebm-F#-F#m-A-C#m-E-Em--RPLP
107. C-Am-F-Fm-C#-Bbm-F#-F#m-A-C#m-E-Em-G-Bm-D-Dm-Bb-Gm-Eb-Ebm-B-Abm-Ab-Cm--RPLP

Le catalogue complet des 124 cycles hamiltoniens



Aprile (d'après Gabriele D'Annunzio)



La fenêtre est entr'ouverte, sur le jardin.
Une heure passe, lente, somnolente.
Et elle, d'abord attentive, finit par s'endormir.
À cette voix qui là-bas se lamente,
Qui se lamente au fond de ce jardin.

Cycle hamiltonien #1

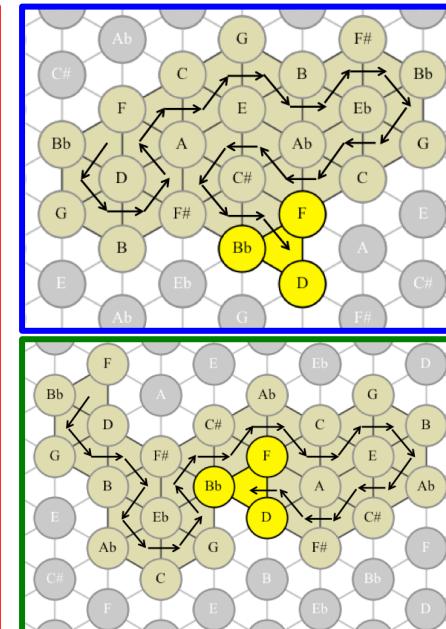
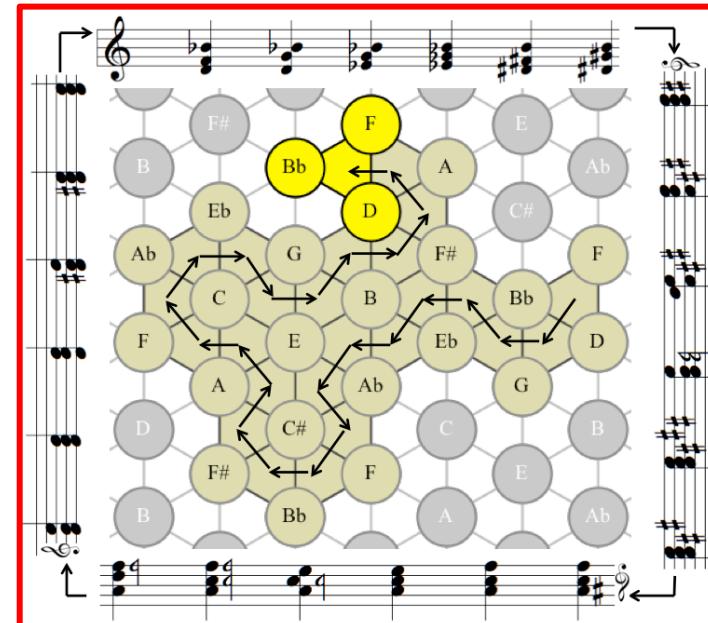
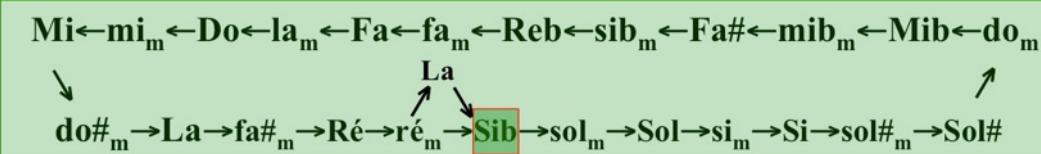
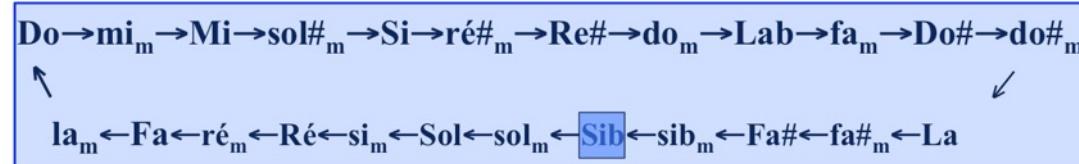
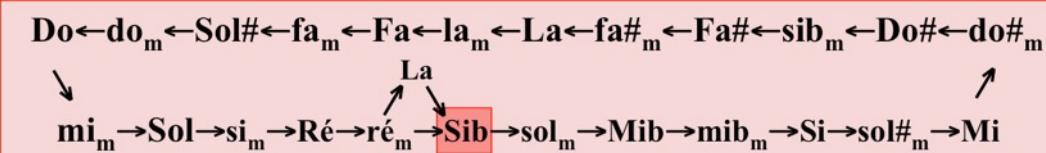
Ce n'est qu'une voix d'eau sur la pierre,
Et combien de fois, combien de fois entendue !
Cet amour et cette heure s'abîment dans cette vie
Comme s'abîment dans l'onde sans fin
Le cadavre et la pierre liés ensemble.

Cycle hamiltonien #2

Elle détend son angoisse dans le sommeil.
Mais l'angoisse est forte, et le sommeil est si léger !
(La lumière d'avril ressemble presque à une neige
qui serait tiède.)

Et certes elle doit souffrir,
Vaguement souffrir, aussi dans le sommeil.

Cycle hamiltonien #3





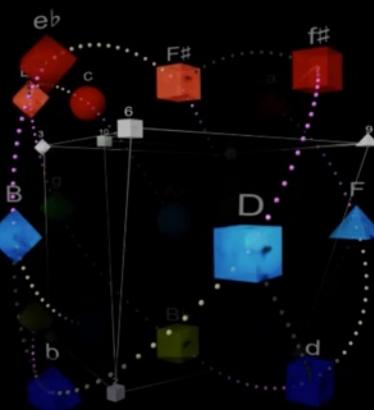
G. D'Annuzio
(1863-1938)

Aprile

Hamiltonian Song



Mathemusical
2D & 4D Visualizations



Composition, Performance: Moreno Andreatta
Hyperspheres & Animations: Gilles Baroin

Spinnen-Tonnetz: Hugo Seress & G.B

Lyrics by Gabriele D'Annuzio

www.MatheMusic.net

→ https://www.youtube.com/watch?v=AB8By7ghTkU&ab_channel=MatheMusic4D

« Ah ! » : une ballade semi-hamiltonienne en compagnie de Jacques Roubaud

List of 124 Hamiltonian Cycles (Bigo/Andreatta, February 2016)

1. C-Cm-Ab-Ab-E-Em-G-Gm-Ed-Bb-Bbm-F#-Fm-A-C#-Cm-B-Fm-Am-
PLPLPRLPRLPRLPRLPRLPRLPRL

2. C-Cm-Ab-Ab-E-Em-G-Gm-Ed-Bb-Bbm-D-F#-Bbm-Bb-Dm-F-Fm-C#-Cm-A-Am-
PLPLPRLPRLPRLPRLPRLPRLPRL

3. C-Cm-Ab-Ab-E-Em-G-Bm-Bb-Eb-Gm-Bb-Bbm-F#-Fm-D-Dm-F-Fm-C#-Cm-A-Am-
PLPLPRLPRLPRLPRLPRLPRLPRL

4. C-Cm-Ab-Ab-E-C#-C#-Fm-F-Am-A-Fm-B#-Bbm-Bb-Dm-D-Bm-B-Eb-Bm-G-Gm-
PLPLPRLPRLPRLPRLPRLPRLPRL

5. C-Cm-Ab-Ab
PLPLR
27. C-Cm-Ab-Eb-Fm-F#-Fm-A-C#-M-E-Em-G-Gm-Bb-Bbm-C#-Fm-Ab-Abm-B-Bm-D-Dm-F-Am-
PRPRPRLPRL

6. C-Cm-Ab-Ab
PLPLR
28. C-Cm-Ab-Eb-F#-Bbm-C#-C#-M-E-Em-G-Gm-Bb-Dm-F-Fm-Ab-Abm-B-Bm-D-F#-A-Am-
PRPRPRLPRL

7. C-Cm-Ab-Ab
PLPLRPLP
29. C-Cm-Ab-Eb-F#-Bbm-C#-Fm-Ab-Abm-B-Bm-D-F#-A-C#-M-E-Em-G-Gm-Bb-Dm-F-Am-
PRPRPRLR

8. C-Cm-Ab-Ab
PLPLRPLP
30. C-Cm-Ab-Gm-G-Bm-B-Eb-Fbm-F#-Fm-D-Dm-Bb-Bbm-C#-C#-Fm-A-Em-F-Fm-Ab-Abm-E-Em-
PLPLRPLPRLPRLPRLPRLPRL

9. C-Cm-Ab-Ab
PLPLRPL
31. C-Cm-Ab-Gm-G-Bm-D-F#-Fm-B-Em-Bbm-Ab-Fm-C#-Bbm-Bb-Dm-F-Am-A-C#-M-E-Em-
PLPLRPLPRLPRLPRLPRLPRL

10. C-Cm-Ab-Ab
PLPLRPL
32. C-Cm-Ab-Gm-G-Bm-D-F#-Fm-A-Em-Dm-Bb-Bbm-F#-Ebm-B-Abm-Ab-Fm-C#-M-E-Em-
PLPLRPLPRLPRLPRLPRL

11. C-Cm-Ab-Ab
PLPLRPLP
33. C-Cm-Ab-Gm-G-B-
PLPLRPLP
54. C-Em-E-C#-Cm-C#-Fm-A-F-#-Fm-B#-Bbm-Bb-Dm-D-Bm-G-Gm-Eb-Ebm-B-Abm-Ab-Cm-
PLPLRPLPRLPRLPRLPRLPRL

12. C-Cm-Ab-Fn
PLPLRPLP
34. C-Cm-Ab-Gm-B-
PLPLRPLP
55. C-Em-E-Cm-C#-Fm-A-F-#-Fm-B#-Bbm-Bb-Dm-F-Am-A-F-Fm-D-Bm-G-Gm-Eb-Abm-Ab-Cm-
PLPLRPLPRLPRLPRL

13. C-Cm-Ab-Fn
PLPLRPLP
35. C-Cm-Ab-Gm-B-
PLPLRPLP
56. C-Em-E-C#-Cm-C#-Fm-F-Dm-Bb-Bbm-F#-Ebm-B-Abm-Ab-Cm-Eb-Gm-G-Bm-D-F#-A-Am-
PLPLRPLPRLPRLPRL

14. C-Cm-Ab-Fn
PLPLRPLP
36. C-Cm-Ab-Gm-B-
PLPLRPLP
57. C-Em-E-Cm-C#-Fm-A-F-#-Fm-B#-Bbm-Bb-Dm-F-Am-A-F-Fm-D-Bm-G-Gm-Eb-Cm-
PLPLRPLPRLPRLPRLPRL

15. C-Cm-Ab-Fn
PLPLRPLP
38. C-Cm-Ab-Gm-B-
PLPLRPLP
58. C-Em-E-Cm-A-Em-F-Fm-C#-B#-Bbm-C#-Fm-Ab-Abm-B-Ebm-F#-Fm-D-Bm-G-Gm-Eb-Cm-
PLPLRPLPRLPRLPRLPRL

16. C-Cm-Ab-Fn
PLPLRPLP
39. C-Cm-Ab-Gm-B-
PLPLRPLP
59. C-Em-E-Cm-A-Em-F-Fm-D-Bb-Bbm-C#-Fm-Ab-Abm-B-Ebm-F#-Fm-D-Bm-G-Gm-Eb-Cm-
PLPLRPLPRLPRLPRLPRL

17. C-Cm-Ab-Fn
PLPLRPLP
60. C-Em-E-Cm-A-
PLPLRPLP
61. C-Em-E-Cm-A-
PLPLRPLP
81. C-Em-G-Gm-B-Dm-Bb-Gm-Eb-Ebm-B-Abm-E-C#-Bbm-F#-Fm-A-Em-F-Fm-Ab-Cm-
PLPLRPLPRLPRLPRLPRLPRL

18. C-Cm-Ab-Fn
PLPLRPLP
62. C-Em-E-Cm-A-
PLPLRPLP
82. C-Em-G-Bm-Dm-F-Fm-Ab-Cm-Eb-Gm-Bb-Bbm-C#-C#-E-Abm-B-Ebm-F#-Fm-A-Am-
PLPLRPLPRLPRLPRL

19. C-Cm-Ab-Fn
PLPLRPLP
63. C-Em-E-Cm-A-
PLPLRPLP
83. C-Em-G-Bm-Dm-F-Am-A-F-#-Fm-B#-Bbm-B-Gm-Eb-Ebm-B-Abm-E-C#-C#-Fm-Ab-Cm-
PLPLRPLPRLPRLPRLPRLPRL

20. C-Cm-Ab-Fn
PLPLRPLP
64. C-Em-G-Gm-Eb-
PLPLRPLP
84. C-Em-G-Bm-D-F#-A-C#-E-Abm-B-Ebm-F#-Bbm-C#-Fm-Ab-Cm-Eb-Gm-Bb-Dm-F-Am-
PLPLRPLPRLPRLPRLPRL

21. C-Cm-Ab-Fn
PLPLRPLP
65. C-Em-G-Gm-Eb-
PLPLRPLP
85. C-Am-E-C#-Cm-F-Fm-D-F#-Fm-B#-Bbm-B-Gm-B-Bm-B-Ebm-Cm-Ab-Abm-E-Em-
PLPLRPLPRLPRLPRL

22. C-Cm-Ab-Fn
PLPLRPLP
66. C-Em-G-Gm-Eb-
PLPLRPLP
86. C-Am-E-C#-Cm-F-Fm-D-F#-Fm-B#-Bbm-B-Gm-Eb-Ebm-B-Bm-G-Em-E-Abm-Ab-Cm-
PLPLRPLPRLPRLPRLPRL

23. C-Cm-Ab-Fn
PLPLRPLP
67. C-Em-E-Cm-A-
PLPLRPLP
87. C-Am-E-C#-Cm-F-Fm-D-Bb-Bbm-F#-Fm-D-Bm-B-Ebm-B-Gm-E-Abm-Ab-Cm-
PLPLRPLPRLPRLPRLPRL

24. C-Cm-Ab-Fn
PLPLRPLP
68. C-Em-G-Gm-B-
PLPLRPLP
88. C-Am-E-C#-B-Bbm-Bd-Bm-F-Am-Cm-B-Gm-B-D-F#-Fm-B-Ebm-B-Abm-E-Em-
PLPLRPLPRLPRLPRLPRLPRL

25. C-Cm-Ab-Fn
PLPLRPLP
69. C-Em-G-Gm-B-
PLPLRPLP
89. C-Am-E-C#-B-Bbm-F#-Fm-D-Bm-G-Gm-Bb-Dm-F-Fm-Ab-Cm-B-Ebm-B-Abm-E-Em-
PLPLRPLPRLPRLPRLPRL

26. C-Cm-Ab-Eb
PLPLRPLP
70. C-Em-G-Gm-B-
PLPLRPLP
90. C-Am-E-C#-B-Bbm-F#-Fm-D-Bm-G-Em-E-Abm-B-Ebm-E-Gm-Bb-Dm-F-Fm-Ab-Cm-
PLPLRPLPRLPRLPRL

27. C-Cm-Ab-Eb
PLPLRPLP
71. C-Em-G-Gm-B-
PLPLRPLP
91. C-Am-E-C#-E-Em-G-Bm-D-F#-Fm-B#-Bbm-C#-Fm-F-Dm-Bb-Gm-Eb-Ebm-B-Abm-Ab-Cm-
PLPLRPLPRLPRLPRLPRL

28. C-Cm-Ab-Eb
PLPLRPLP
72. C-Em-G-Gm-B-
PLPLRPLP
92. C-Am-E-C#-E-Abm-Cm-B-Ebm-B-Bm-D-F#-Fm-B#-Bbm-C#-Fm-F-Dm-Bb-Gm-G-Em-
PLPLRPLPRLPRLPRLPRLPRL

29. C-Cm-Ab-Eb
PLPLRPLP
73. C-Em-G-Gm-B-
PLPLRPLP
93. C-Am-E-C#-E-Abm-Cm-B
PLPLRPLPRLPRLPRLPRL
94. C-Am-A-F#-F#-Ebm-Cb
PLPLRPLP
95. C-Am-A-F#-F#-Ebm-Cb
PLPLRPLP
96. C-Am-A-F#-F#-Ebm-B-Ab
PLPLRPLP
97. C-Am-A-F#-F#-D-Bm-F-Fm-C
PLPLRPLPRLPRLPRLPRL
98. C-Am-A-F#-F#-D-Bm-B-Ebm
PLPLRPLPRLPRLPRL
99. C-Am-A-F#-F#-D-Bm-B-Abm-B
PLPLRPLPRLPRLPRL
100. C-Am-A-F#-M-D-Bm-B-Ab
PLPLRPLP
101. C-Am-A-F#-F#-D-Bm-G-Gm
PLPLRPLP
102. C-Am-A-F#-F#-D-Bm-B-Ab
PLPLRPLP
103. C-Am-F-Fm-C#-C#-Fm-A-
PLPLRPLP
104. C-Am-F-Fm-C#-C#-Fm-A-
PLPLRPLP
105. C-Am-F-Fm-C#-B-Bm-Bb
PLPLRPLP
106. C-Am-F-Fm-C#-B-Bm-Bb
PLPLRPLP
107. C-Am-F-Fm-C#-B-Bm-Bb
PLPLRPLP

116. C-Am-D-Bm-B-Ab-Abm-B-Fm-C#-Bbm-B-Gm-G-E-Em-E-C#-Fm-A-F#-Ebm-B-Cm-
-RPLRPLP

117. C-Am-D-Bm-B-Ab-Abm-B-Fm-C#-Bbm-B-Gm-G-E-Em-E-C#-Fm-A-F#-Ebm-B-Cm-
-RPLRPLP

118. C-Am-D-Bm-B-G-Gm-Bb-Bbm-F#-Fm-A-C#-Fm-A-Em-B-Abm-B-Ebm-B-Cm-
-RPLRPLPRLPRLPRLPRLPRL

119. C-Am-D-Bm-B-G-E-Abm-B-Ebm-B-Gm-Bb-Bbm-F#-Fm-A-C#-Fm-A-Em-B-
-RPLRPLPRLPRLPRLPRL

120. C-Am-D-Bm-B-G-E-Em-E-C#-A-F#-F#-Ebm-B-Abm-B-Fm-C#-Bbm-B-Gm-B-
-RPLRPLPRLPRLPRLPRL

121. C-Am-D-Bm-B-G-E-Em-E-C#-A-F#-F#-Ebm-B-Abm-B-Fm-C#-Bbm-B-Gm-B-
-RPLRPLPRLPRLPRLPRL

122. C-Am-D-Bm-B-G-E-Em-E-C#-A-F#-F#-Ebm-B-Abm-B-Fm-C#-Bbm-B-Gm-B-
-RPLRPLPRLPRLPRLPRL

123. C-Am-D-Bm-B-G-E-Em-E-C#-A-F#-F#-Ebm-B-Abm-B-Fm-C#-Bbm-B-Gm-B-
-RPLRPLPRLPRLPRLPRL

124. C-Am-D-Bm-B-G-E-Em-E-C#-A-F#-F#-Ebm-B-Abm-B-Fm-C#-Bbm-B-Gm-B-
-RPLRPLPRLPRLPRL



Écrire les rues

*La Forme d'une ville change plus vite,
hélas,
que le cœur des humains*

cent-cinquante poèmes 1991-1998

recueil de Jacques ROUBAUD paru en 1999

L'auteur :

Compositeur de poésie, retraité de la mathématique,
membre de l'Oulipo depuis 1966.

L'ouvrage :

Jacques ROUBAUD parcourt les rues de Paris
et leur rend hommage
au travers de poèmes
composés chacun selon une règle différente.

Le titre est emprunté à BAUDELAIRE qui écrivait dans « *Le Cygne* » :

*Le vieux Paris n'est plus (la forme d'une ville
Change plus vite, hélas! que le cœur d'un mortel)*

Mais Roubaud a aussi en tête
le recueil de Raymond QUENEAU :
Courir les rues.

« Ah ! » : une ballade semi-hamiltonienne en compagnie de Jacques Roubaud

4/4 C |

2/4 C | 4/4 Em E | C#m |
Ah ! quel silence Dans la rue de Valence !

A F#m | D |
Mais quel vacarme Dans la rue de Parme !

2/4 Dm Bb | 4/4Gm G | Bm |
Calmé ah ! quel calme Dans la rue des Palmes

B Abm | Ab |
Quelle agitation Dans la rue Bran-cion

Cm | Eb |
Ah ! l'heure sereine Dans la rue de Seine !

Gm G | Bm |
Mais quelle inquiétude Boulevard de Dix-mude !

D Dm Bb Bbm | Db |
Ah ! quel trouble interne Avenue des ternes

Fm F | Am |
Quel repos intérieur Rue Git-le-Cœur.

C Em | E | C#m A | F#m | D Dm | Bb | Gm G | Bm | B Abm Ab Cm
Ah ! etc.

| Eb | Gm G Bm D | Dm | Bb Bbm | Db | Fm F | Am |

2/4 C | 4/4 Em E | C#m |
Ah ! quel silence Dans la rue de Valence !

A F#m | D |
Mais quel vacarme Dans la rue de Parme !

2/4 Dm Bb | 4/4Gm G | Bm |
Calmé ah ! quel calme Dans la rue des Palmes

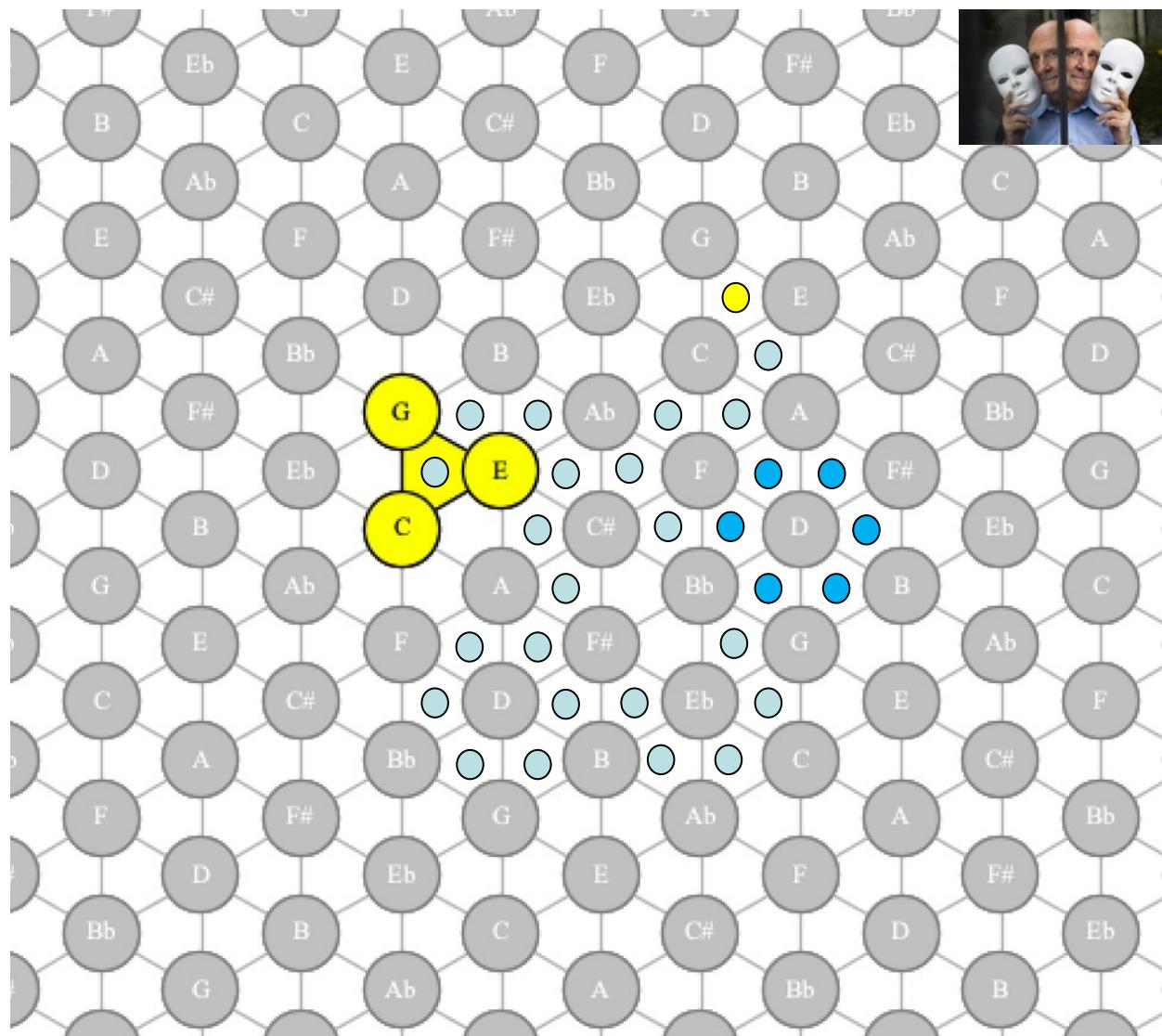
B Abm | Ab |
Quelle agitation Dans la rue Bran-cion

Cm | Eb |
Ah ! l'heure sereine Dans la rue de Seine !

Gm G | Bm |
Mais quelle inquiétude Boulevard de Dix-mude !

D Dm Bb Bbm | Db |
Ah ! quel trouble interne Avenue des ternes

Fm F | Am | C |
Quel repos intérieur Rue Git-le-Cœur.



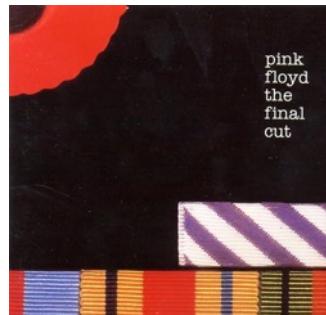
→ http://repmus.ircam.fr/_media/moreno/ah_jacquesroubaudhamilton.mp3

The Gunner's Hamiltonian Dream (une expérience *oumupienne* autour de Pink Floyd)

The Gunner's dream (R. Waters, 1983 / M. Andreatta, 2018)

(C) C+
Floating down through the clouds
Am F
Memories come rushing up to meet me now.
Fm
In the space between the heavens C#m
and in the corner of some foreign field
A F+ Bbm
I had a dream.
F# F#m D Dm
I had a dream.
Bb
Good-bye Max.
D+
Good-bye Ma.
Ebm B
After the service when you're walking slowly to the car
Bm G
And the silver in her hair shines in the cold November air

Gm
You hear the tolling bell Eb
And touch the silk in your lapel G+ Em E G#m
And as the tear drops rise to meet the comfort of the band
G# Cm
You take her frail hand
(C)
And hold on to the dream.

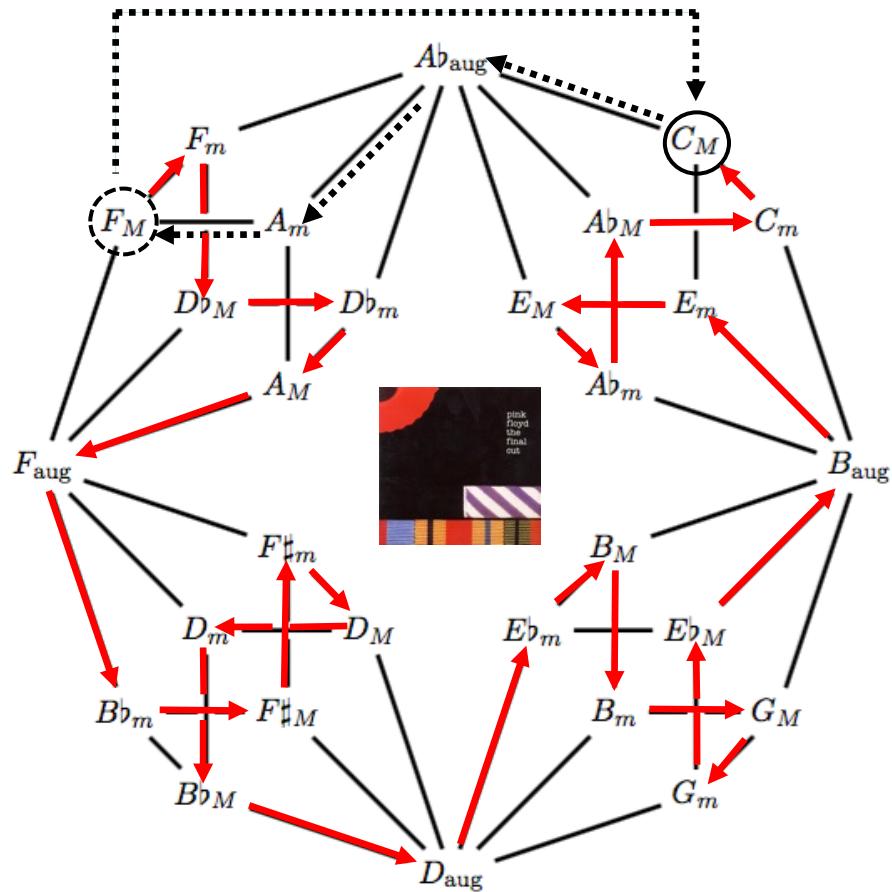


Le rêve du canonnier

Flottant parmi les nuages
Des souvenirs se ruent à ma rencontre.
Dans l'espace entre les cieux
Et dans un recolin d'un lointain champ de bataille
J'ai fait un rêve,
J'ai fait un rêve.
Au revoir Max
Au revoir maman
Après le service, quand tu marches lentement vers la voiture
Et l'argent dans ses cheveux luit dans l'air froid de novembre
Tu entends sonner le glas
Et touche la soie sur ton revers
Et tandis que les larmes versées s'élèvent pour se fondre dans le confort du groupe
Tu prends sa frêle main
Et tu t'accroches au rêve.



The Gunner's Hamiltonian Dream (une expérience oumupienne autour de Pink-Floyd)



The three Hamiltonian Cycles ($C_M = C$, $C_m = Cm$, $C_{aug} = C+$)

$C \rightarrow C+ \rightarrow Am \rightarrow F \rightarrow Fm \rightarrow C\# \rightarrow C\#m \rightarrow A \rightarrow F+ \rightarrow Bbm \rightarrow F\# \rightarrow F\#m \rightarrow D \rightarrow Dm \rightarrow Bb \rightarrow D+ \rightarrow Ebm \rightarrow B \rightarrow Bm \rightarrow G \rightarrow Gm \rightarrow Eb \rightarrow G+ \rightarrow Em \rightarrow E \rightarrow G\#m \rightarrow G\# \rightarrow Cm \rightarrow C$

$C \rightarrow C+ \rightarrow Am \rightarrow F \rightarrow Fm \rightarrow C\# \rightarrow C\#m \rightarrow A \rightarrow F+ \rightarrow F\#m \rightarrow F\# \rightarrow Bbm \rightarrow Bb \rightarrow Dm \rightarrow D \rightarrow D+ \rightarrow Ebm \rightarrow B \rightarrow Bm \rightarrow G \rightarrow Gm \rightarrow Eb \rightarrow G+ \rightarrow Em \rightarrow E \rightarrow G\#m \rightarrow G\# \rightarrow Cm \rightarrow C$

$C \rightarrow C+ \rightarrow Am \rightarrow F \rightarrow Fm \rightarrow C\# \rightarrow C\#m \rightarrow A \rightarrow F+ \rightarrow F\#m \rightarrow D \rightarrow Dm \rightarrow Bb \rightarrow Bbm \rightarrow F\# \rightarrow D+ \rightarrow Ebm \rightarrow B \rightarrow Bm \rightarrow G \rightarrow Gm \rightarrow Eb \rightarrow G+ \rightarrow Cm \rightarrow G\# \rightarrow G\#m \rightarrow E \rightarrow Em \rightarrow C$

The Gunner's dream (R. Waters, 1983 / M. Andreatta, 2018)

(C)

C+

Floating down through the clouds

Am

F

Memories come rushing up to meet me now.

Fm

In the space between the heavens

C#

and in the corner of some foreign field

C#m

A I had a dream.

F#

F#m D Dm

I had a dream.

Bb

Good-bye Max.

D+

Good-bye Ma.

Ebm

B

After the service when you're walking slowly to the car

Bm

G

And the silver in her hair shines in the cold November air

Gm

You hear the tolling bell

Eb

And touch the silk in your lapel

G+

Em

And as the tear drops rise to meet the comfort of the band

G#

Cm

You take her frail hand

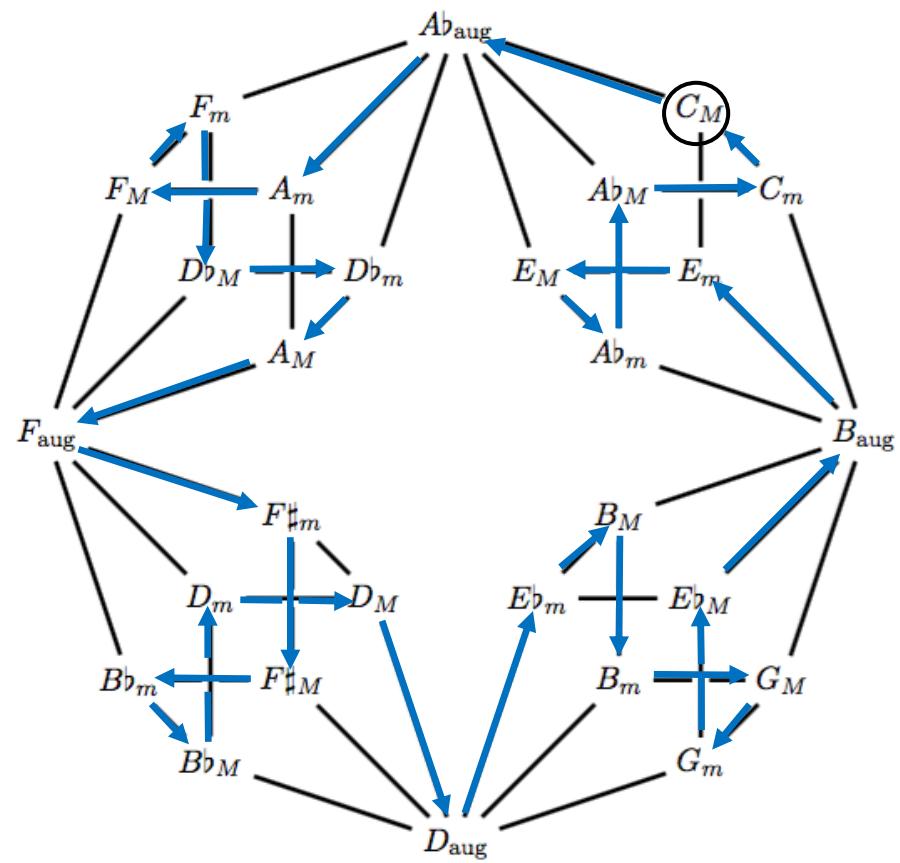
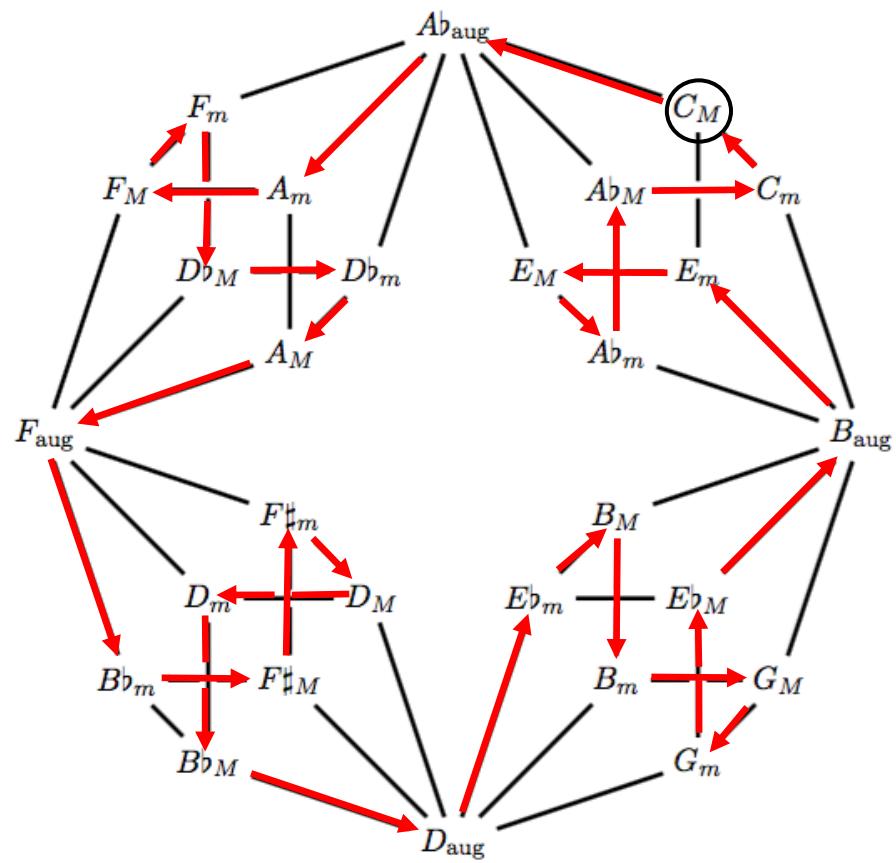
(C)

E G#m

And hold on to the dream.



The Gunner's Hamiltonian Dream (une expérience oumupienne autour de Pink-Floyd)

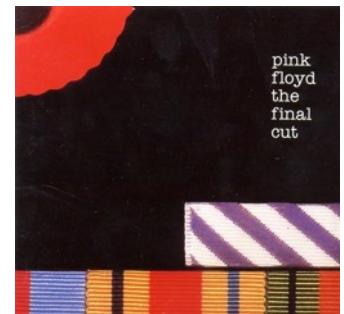


Les trois cycles hamiltoniens ($C_M = C$, $C_m = Cm$, $C_{aug} = C+$)

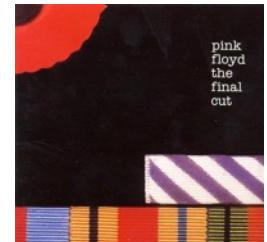
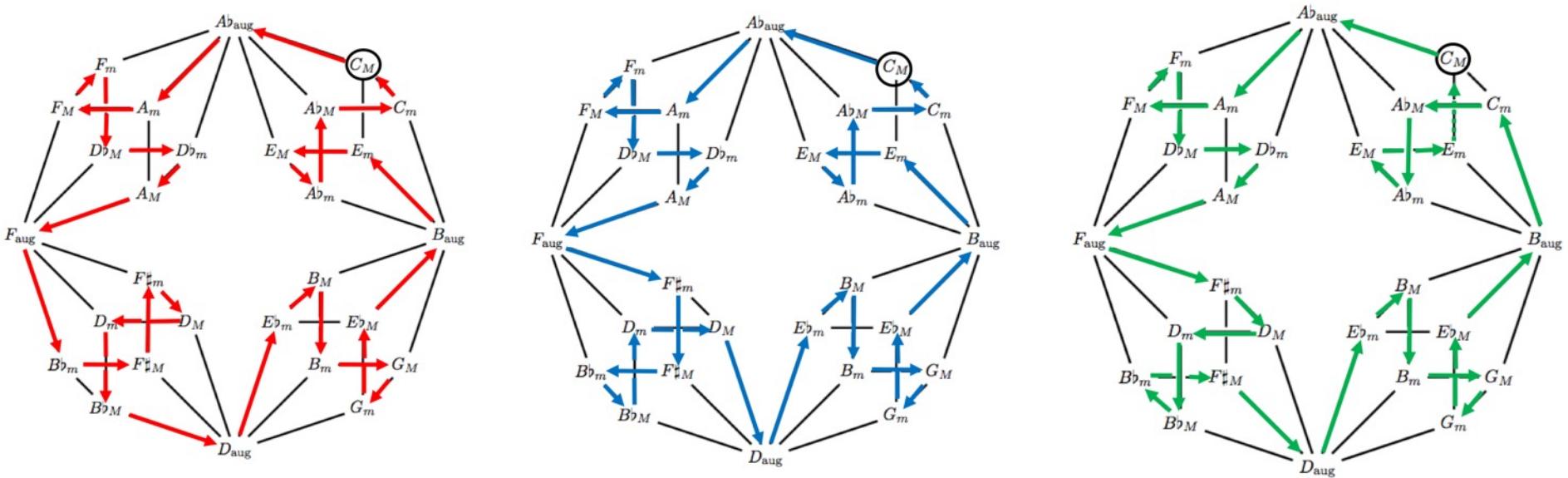
$C \rightarrow C+ \rightarrow Am \rightarrow F \rightarrow Fm \rightarrow C\# \rightarrow C\#m \rightarrow A \rightarrow F+ \rightarrow Bbm \rightarrow F\# \rightarrow F\#m \rightarrow D \rightarrow Dm \rightarrow Bb \rightarrow D+ \rightarrow Ebm \rightarrow B \rightarrow Bm \rightarrow G \rightarrow Gm \rightarrow Eb \rightarrow G+ \rightarrow Em \rightarrow E \rightarrow G\#m \rightarrow G\# \rightarrow Cm \rightarrow C$

$C \rightarrow C+ \rightarrow Am \rightarrow F \rightarrow Fm \rightarrow C\# \rightarrow C\#m \rightarrow A \rightarrow F+ \rightarrow F\#m \rightarrow F\# \rightarrow Bbm \rightarrow Bb \rightarrow Dm \rightarrow D \rightarrow D+ \rightarrow Ebm \rightarrow B \rightarrow Bm \rightarrow G \rightarrow Gm \rightarrow Eb \rightarrow G+ \rightarrow Em \rightarrow E \rightarrow G\#m \rightarrow G\# \rightarrow Cm \rightarrow C$

$C \rightarrow C+ \rightarrow Am \rightarrow F \rightarrow Fm \rightarrow C\# \rightarrow C\#m \rightarrow A \rightarrow F+ \rightarrow F\#m \rightarrow D \rightarrow Dm \rightarrow Bb \rightarrow Bbm \rightarrow F\# \rightarrow D+ \rightarrow Ebm \rightarrow B \rightarrow Bm \rightarrow G \rightarrow Gm \rightarrow Eb \rightarrow G+ \rightarrow Cm \rightarrow G\# \rightarrow G\#m \rightarrow E \rightarrow Em \rightarrow C$



The Gunner's Hamiltonian Dream (an *oumouopian* experiment on a song by Pink-Floyd)



Les trois cycles hamiltoniens ($C_M = C$, $C_m = Cm$, $C_{aug} = C+$)

C-->C+-->Am-->F-->Fm-->C#-->C#m-->A-->F+->Bbm-->F#-->F#m-->D-->Dm-->Bb-->D+->Ebm-->B-->Bm-->-->G-->Gm-->Eb-->G+->Em-->E-->G#m-->G#-->Cm-->C

C-->C+-->Am-->F-->Fm-->C#-->C#m-->A-->F+->F#m-->F#-->Bbm-->Bb-->Dm-->D-->D+->Ebm-->B-->Bm-->-->G-->Gm-->Eb-->G+->Em-->E-->G#m-->G#-->Cm-->C

C-->C+-->Am-->F-->Fm-->C#-->C#m-->A-->F+->F#m-->D-->Dm-->Bb-->Bbm-->F#-->D+->Ebm-->B-->Bm-->-->G-->Gm-->Eb-->G+->Cm-->G#-->G#m-->E-->Em-->C

HamilFloyd

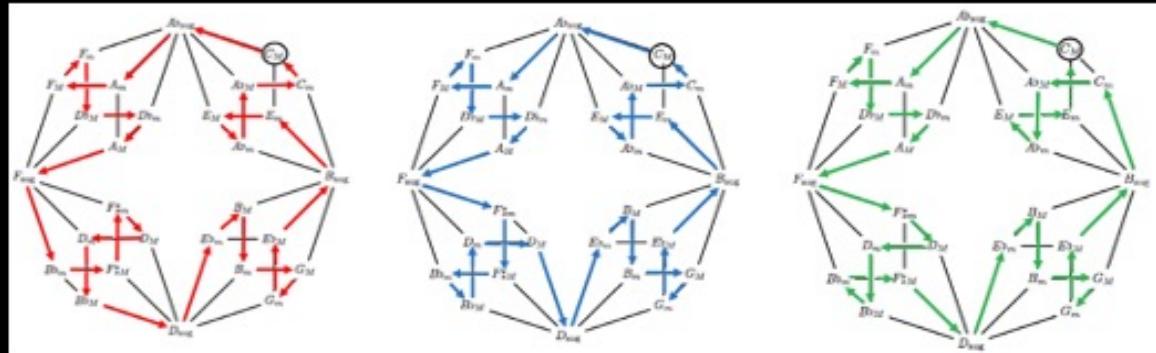
The Gunner's Hamiltonian Dream



Moreno Andreatta
Gilles Baroin 2022



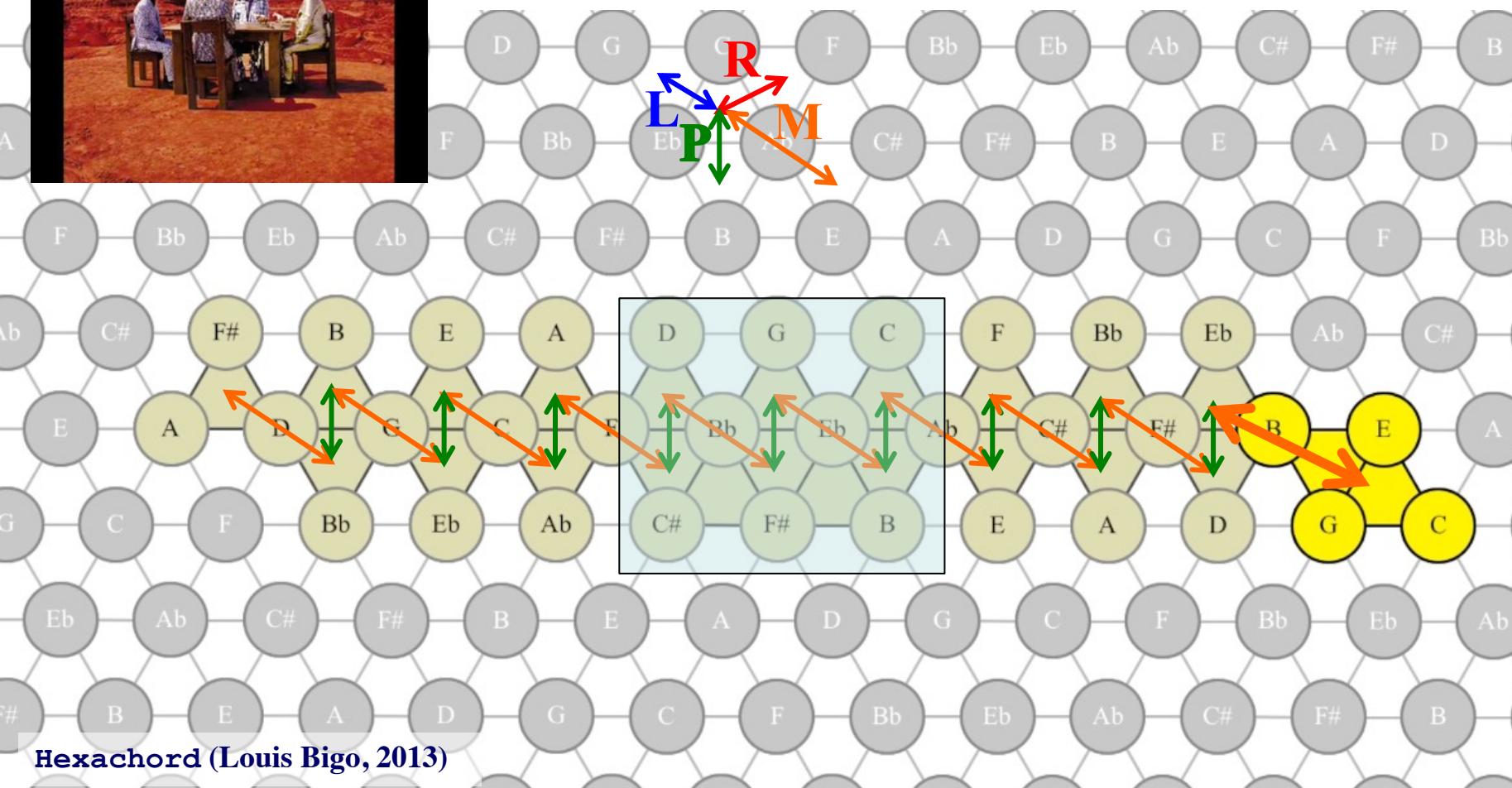
→ https://www.youtube.com/watch?v=nz5TYob02B4&ab_channel=MatheMusic4D



Symétries et procédés algorithmiques chez Muse



“Take a bow” (*Black Holes and Revelations*, 2006)

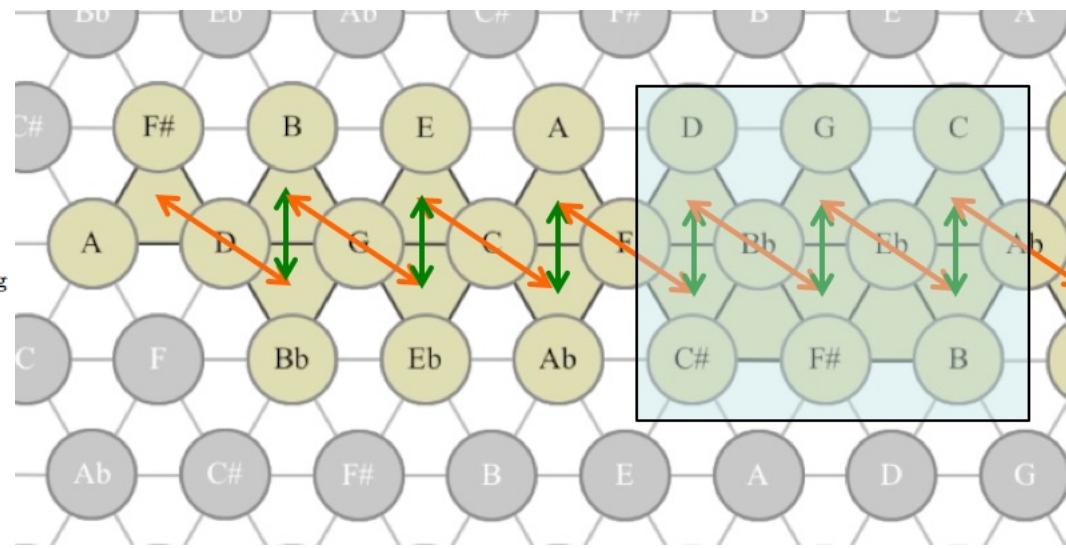
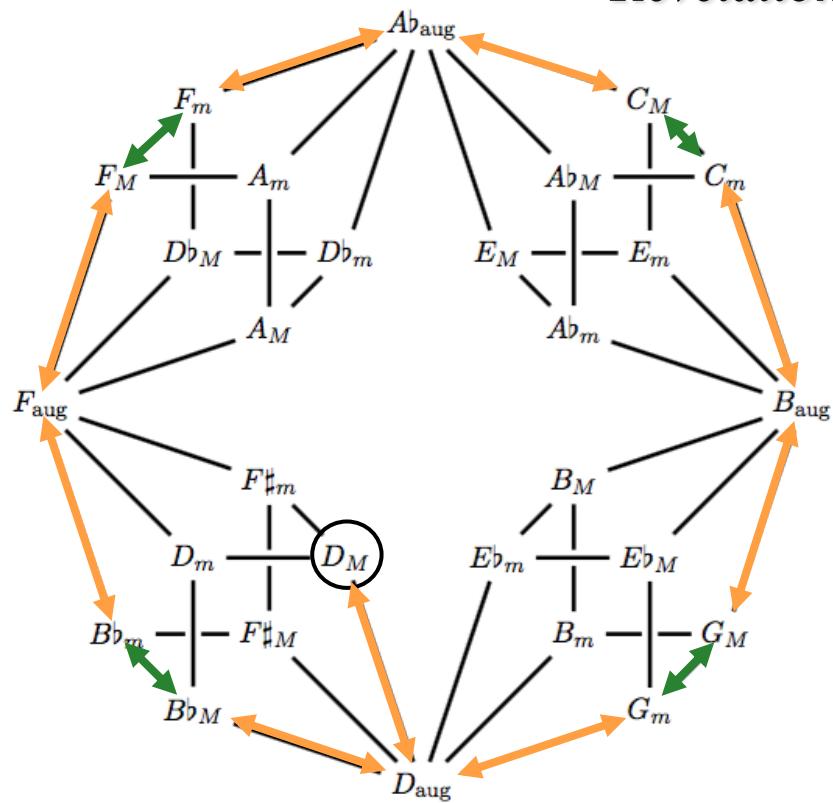


Hexachord (Louis Bigo, 2013)

axe temporel

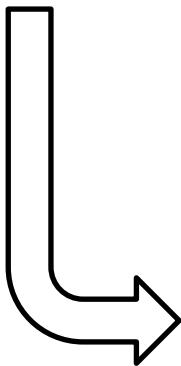
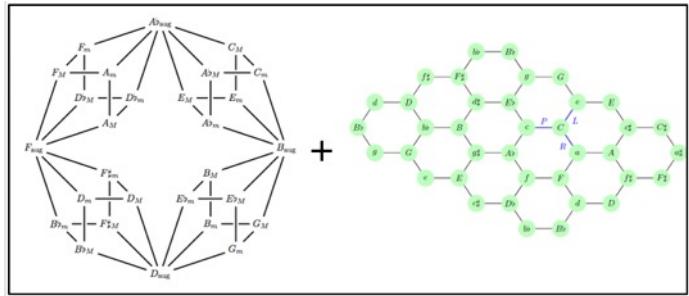
Autres espaces de représentations pour les progressions harmoniques

“Take a bow” (*Black Holes and Revelations*, 2006)

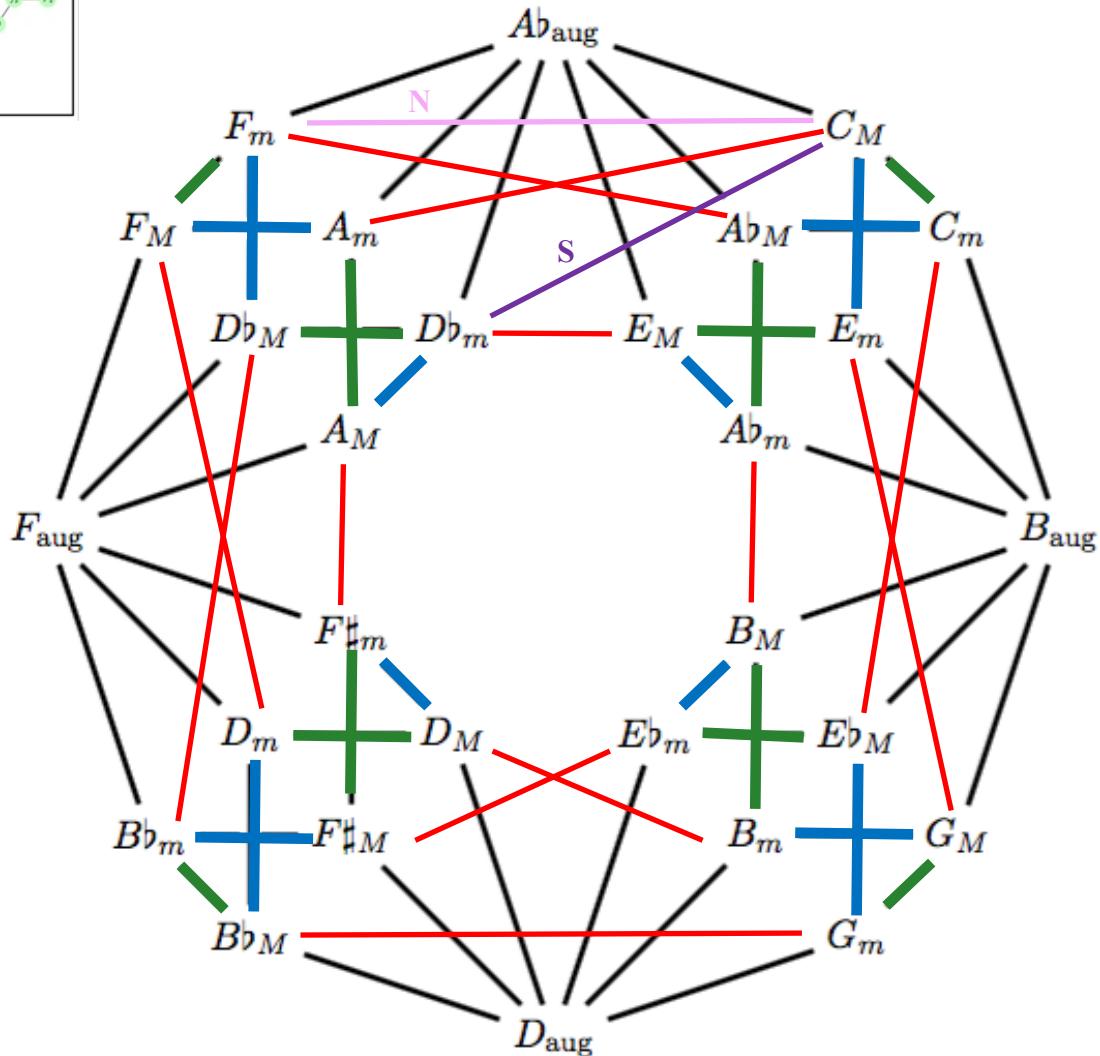


J. Douthett, P. Steinbach, **Parsimonious Graphs: A Study in Parsimony, Contextual Transformation, and Modes of Limited Transposition**, *Journal of Music Theory*, 42/2, 1998.

Cube-Dance et Tonnetz : à vous de jouer !



→ <http://repmus.ircam.fr/media/moreno/cube-dance-tonnetz.pdf>
https://alexpoft.github.io/interactive_mathmusic/Pmn_graphs/pmn_graphs.html



LPR = SLIDE

RLP = NEBENVERWANDT

PRL = X